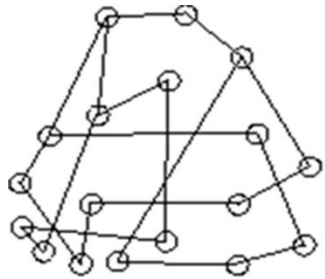


# Network Science and Applications

Epidemics, Parkinson, Fake News, Traffic, Climate, Physiology, Cascading failures etc.

Shlomo Havlin

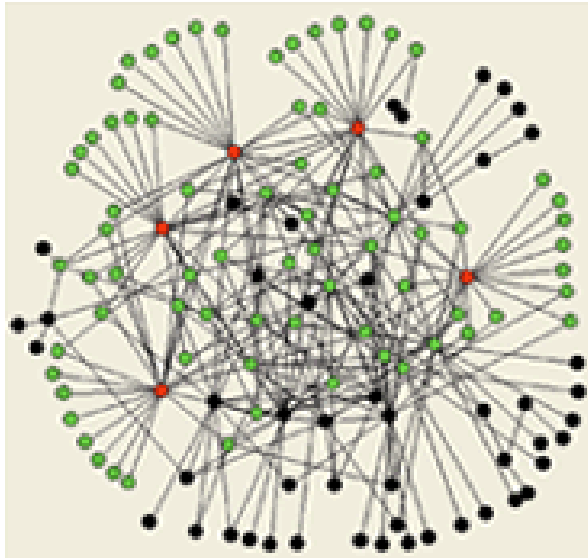
<2000  
Poissonian



2000

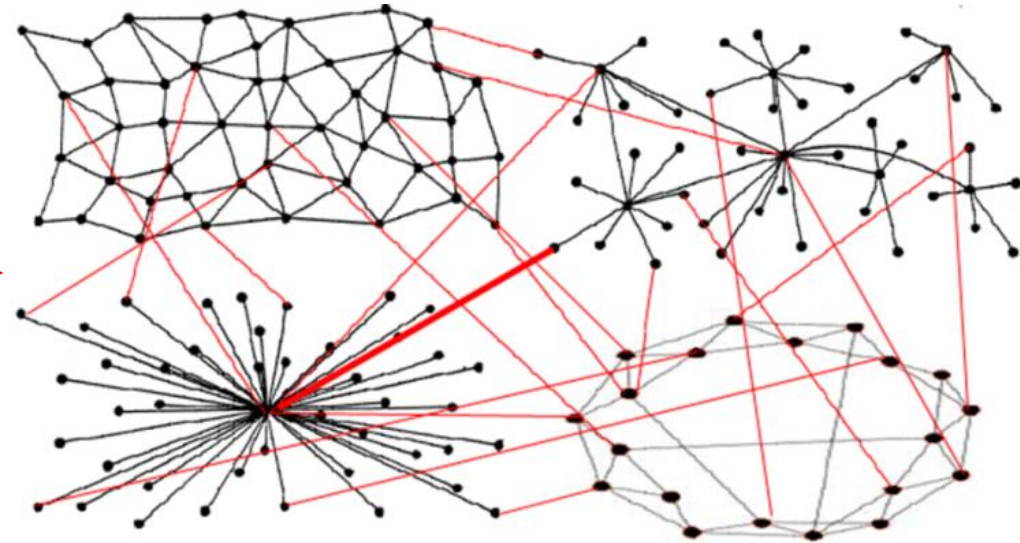
Scale free – real networks

$$p(k) \sim k^{-\lambda}$$



2010

Interacting networks: multilayer, multiplex ...



Electric grid,  
Communication  
Transportation  
Services  
Two types of  
links-novel  
phenomena

**Covid-19:** Bnaya Gross et al *EPL* (2020); Cohen et al *PRL* (2003); Yangyang Liu et al, *National Science Review* (2020);

**Traffic:** Daqing Li et al, *PNAS* 112, 669 (2015); G. Zeng et al, *PNAS* 116, 23 (2019); Shida et al *Sci. Rep.* 1, 10 (2020);

**Parkinson:** E. Asher, R. Bartsch et al, *Nature Communications Biology*, 4, 1 (2021);

**Network Physiology:** Bashan, Bartsch, Ivanov *Nature Communications*, 3 702 (2012); **Climate, Brain :** Jurgen Kurths *Lecture today*

**Interdependent Networks:** Buldyrev et al *Nature* **464, 1025** (2010); Gao et al *Nat. Phys.* 8, 40 (2012), Danziger et al *Nat. Phys.* (2020)

**Interdependent Superconducting Networks:** I. Bonamassa et al, *arXiv:2207.01669* (2022)

# Percolation of Single networks

- Percolation theory
- Remove  $1-p$  fraction of nodes
- Functioning – existence of giant component
- Network resilience

- Second order phase transition
- Critical behaviour
- Universality classes

## Scaling relations

$$n_s \sim s^{-\tau}$$

$$d\nu = 2\beta + \gamma$$

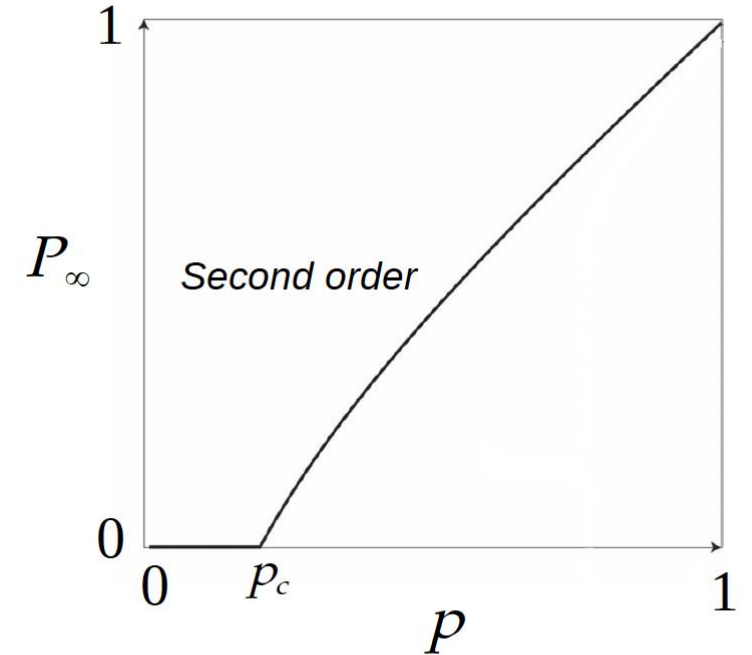
$$\delta - 1 = \gamma/\beta$$

## Critical exponents

$$P_\infty \sim (p - p_c)^\beta$$

$$\xi \sim |p - p_c|^{-\nu}$$

$$\chi \sim |p - p_c|^{-\gamma}$$



$p < p_c$



$p = p_c$



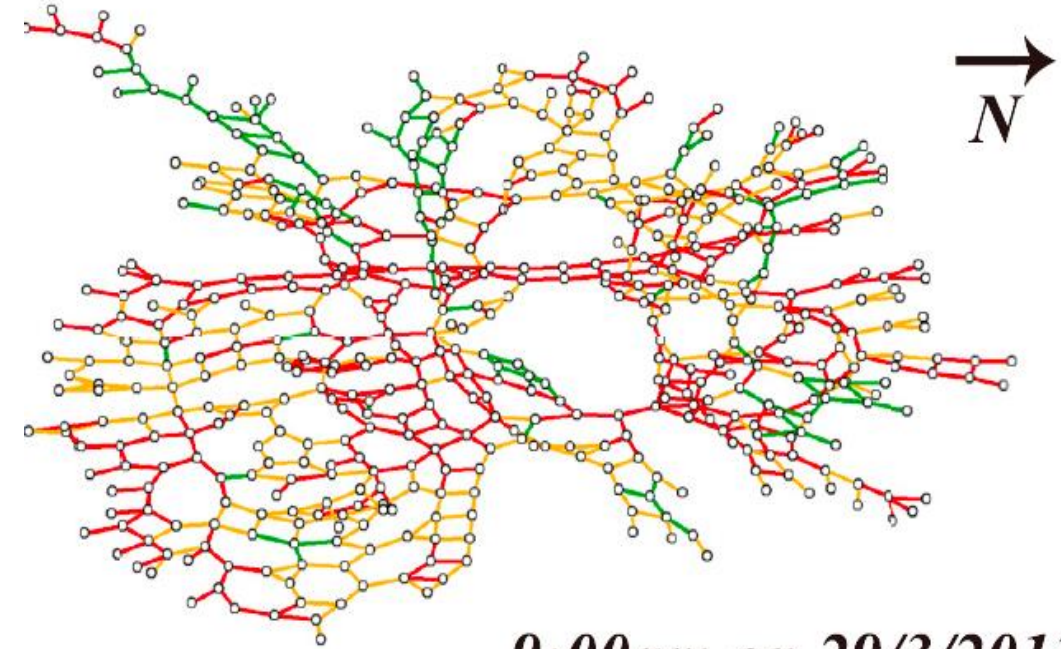
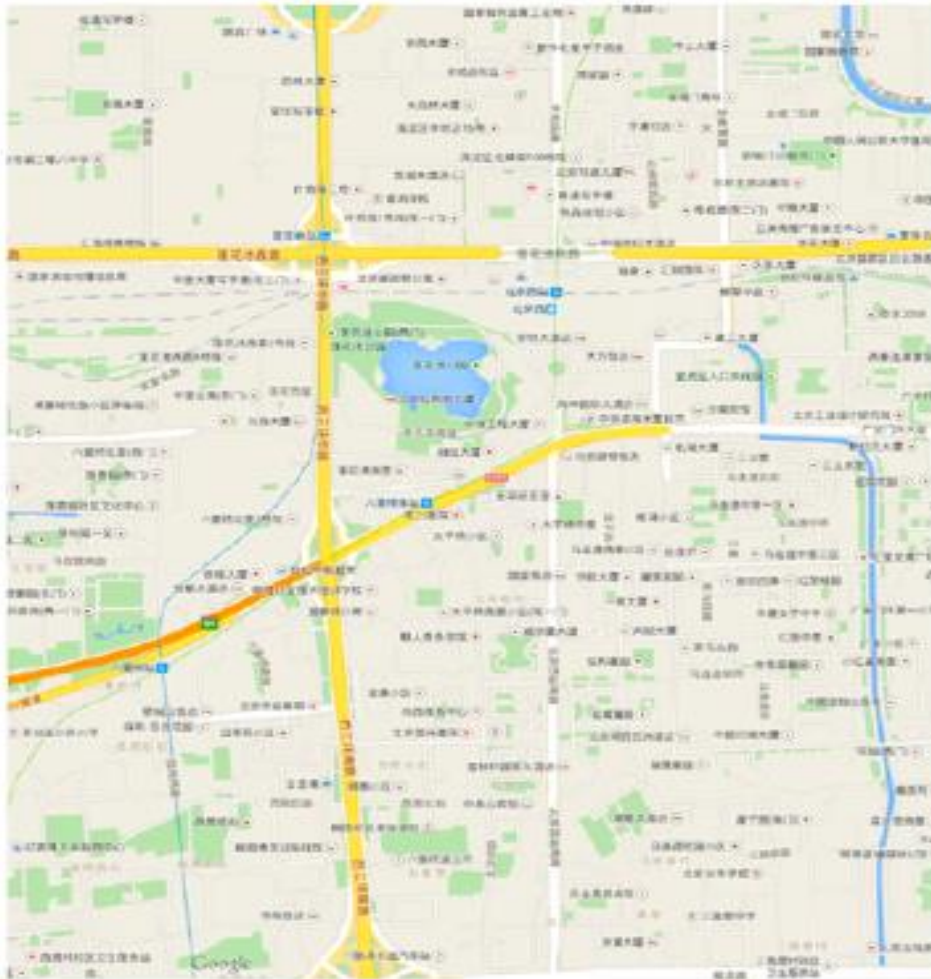
$p > p_c$



# Traffic and Network Theory

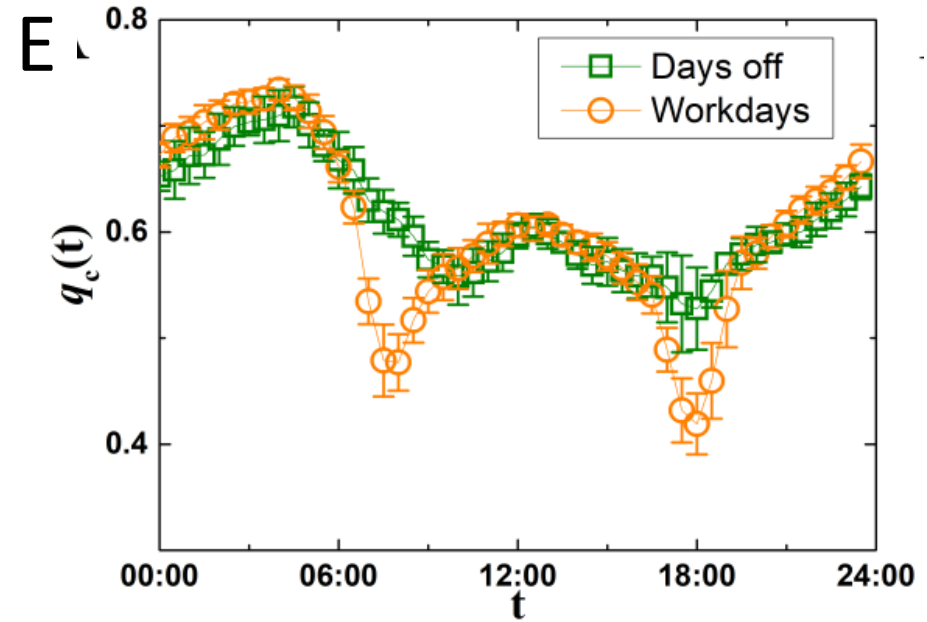
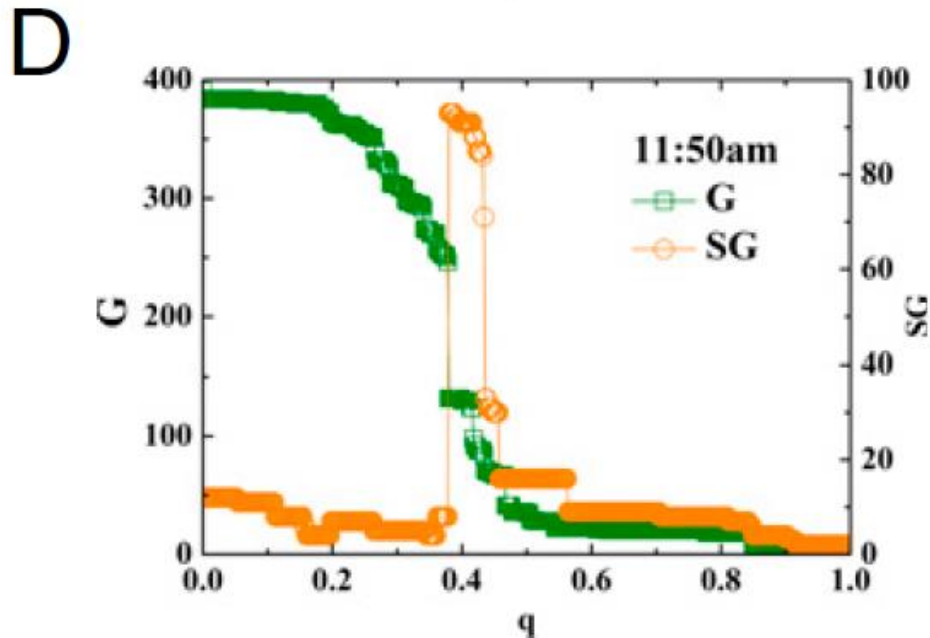
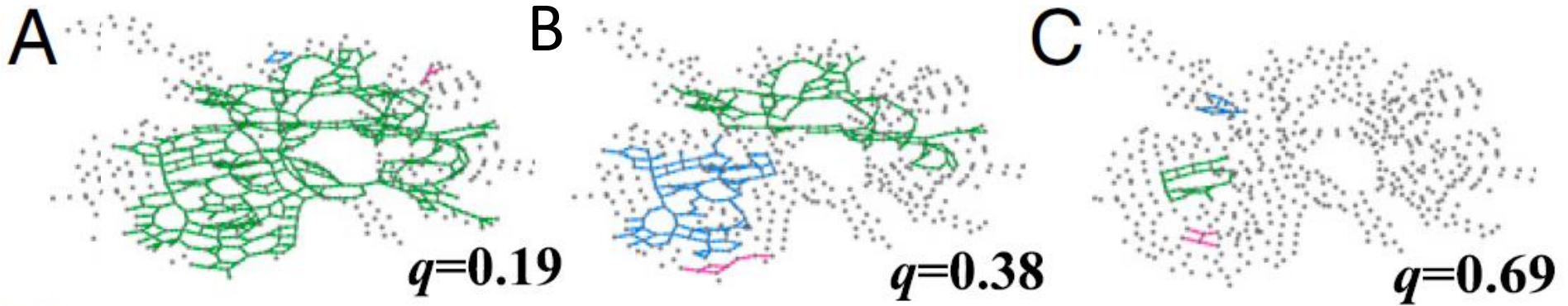
1. Mapping traffic in Beijing as a dynamic network
2. Percolation theory identify bottlenecks

A



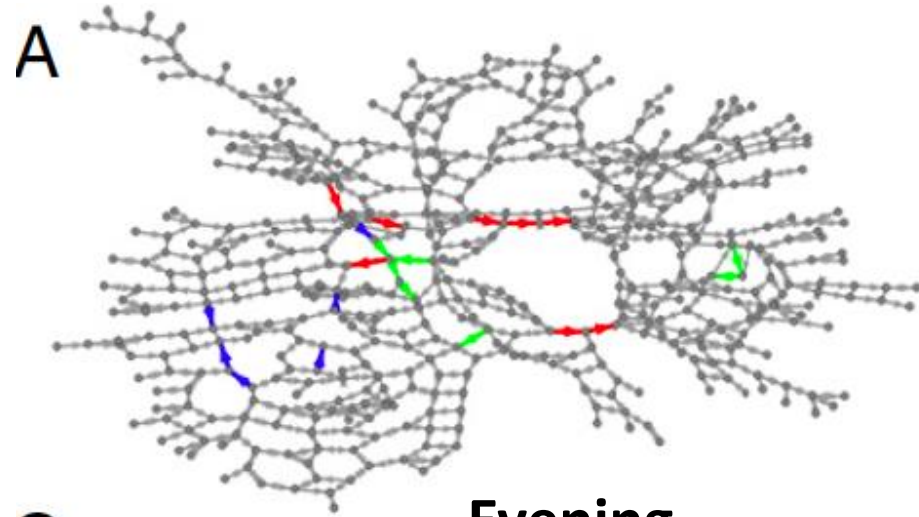
*9:00am on 29/3/2013*

# NETWORK, PERCOLATION AND TRAFFIC

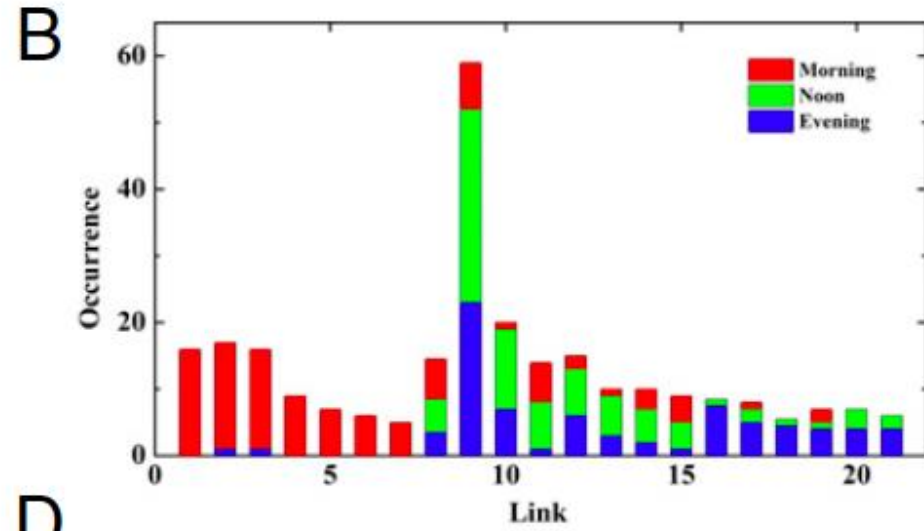


$q=1-p$

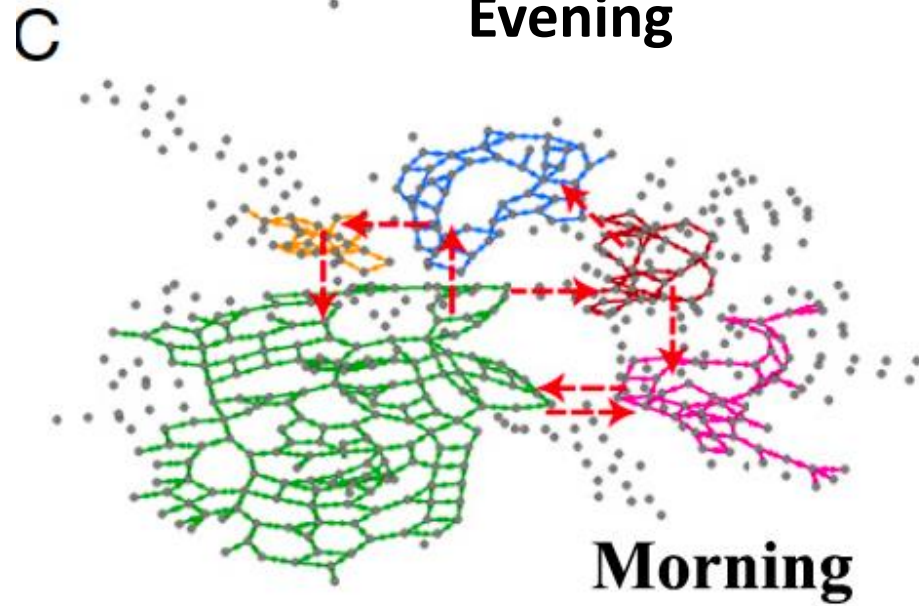
# DIFFERENT HOURS DIFFERENT BOTTLENECKS



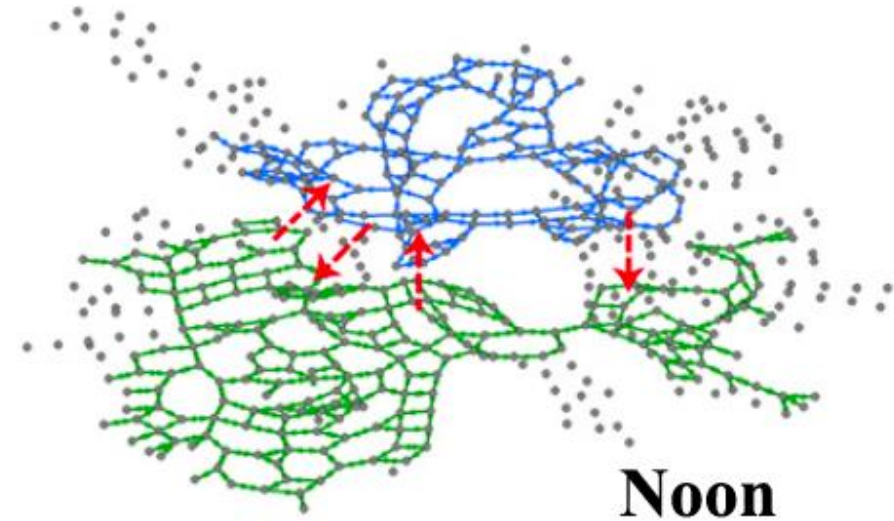
**Evening**



**D**



**Morning**

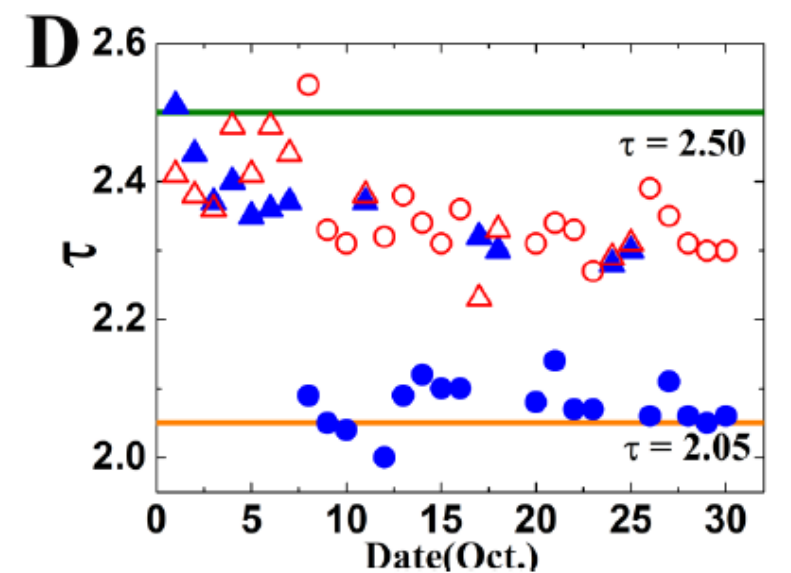
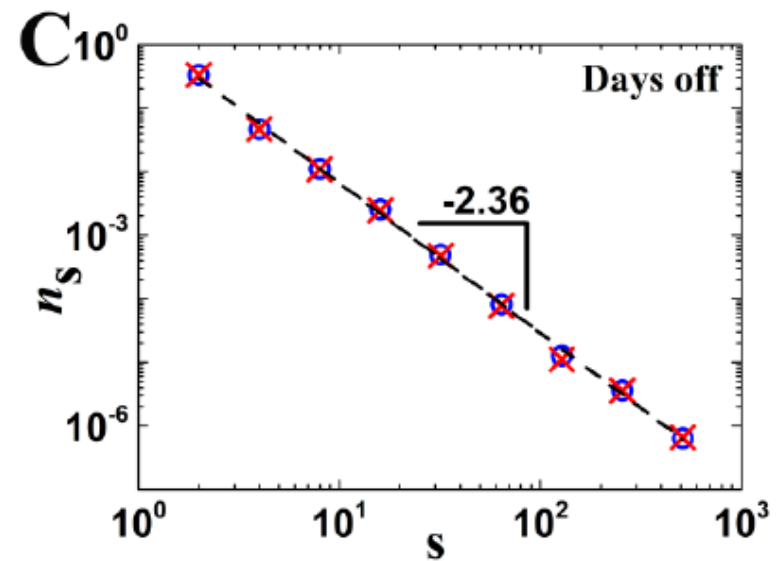
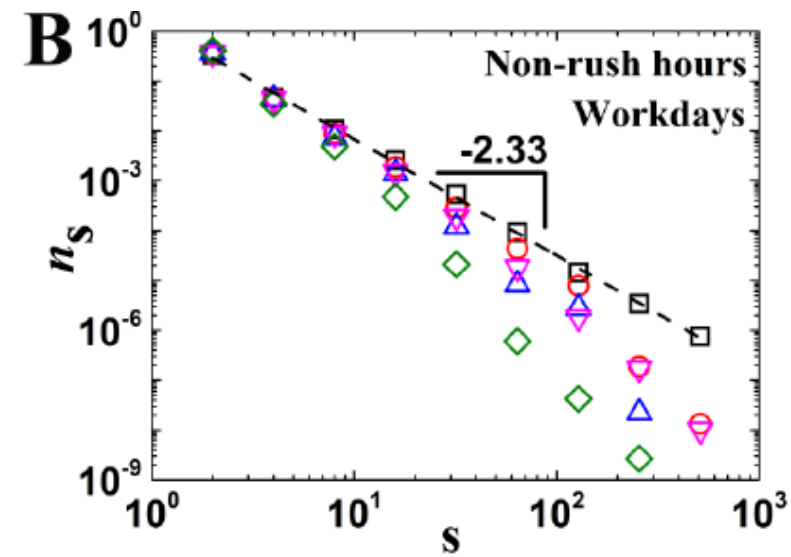
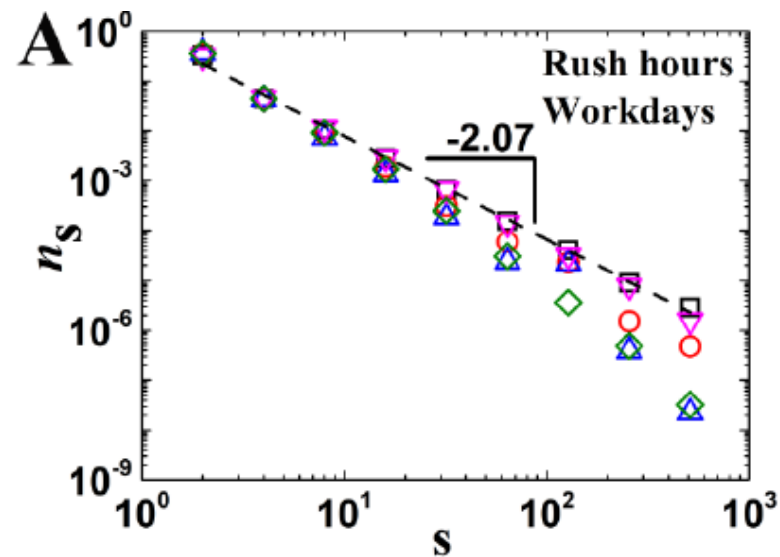


**Noon**

# Percolation critical exponents

2015

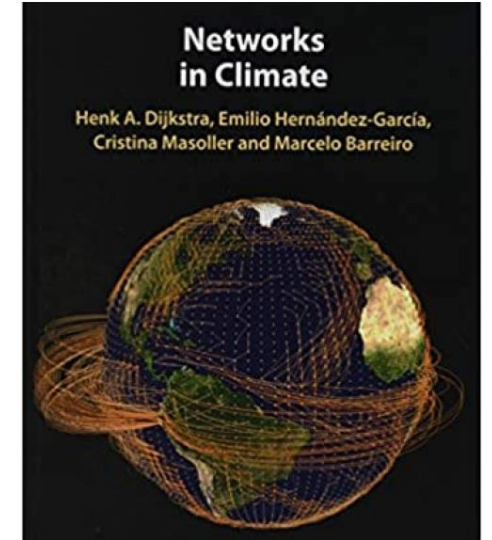
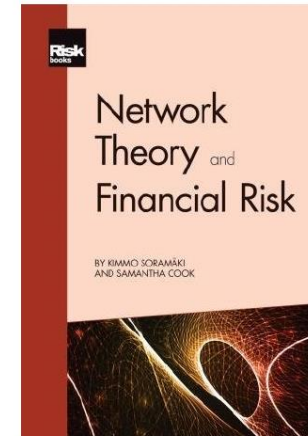
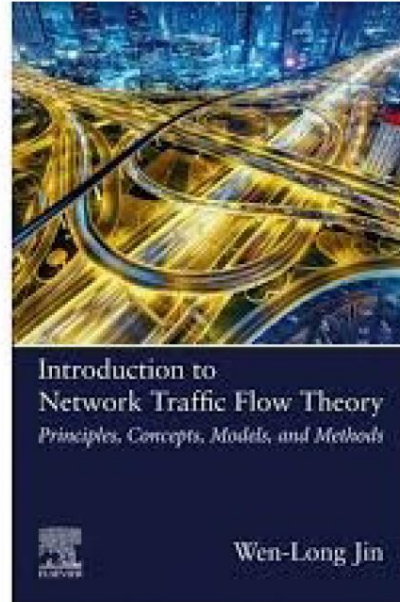
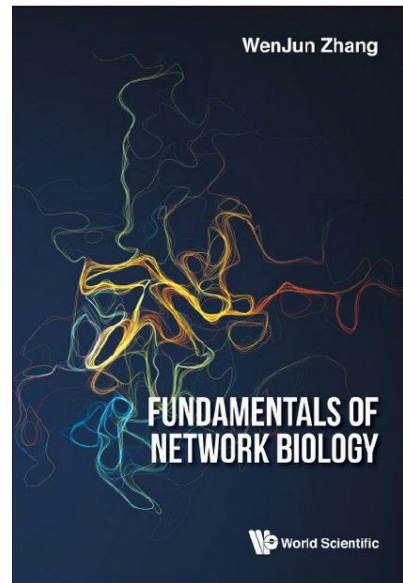
8:00AM, Oct. 15th



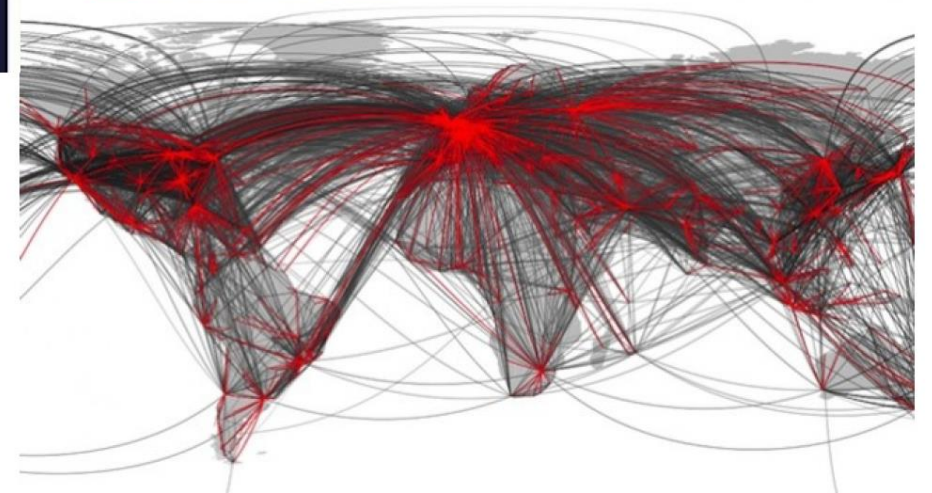
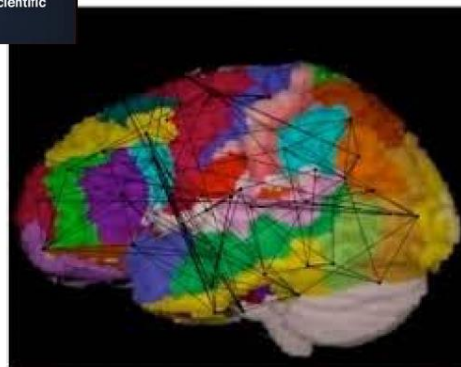
G. Zeng et al, PNAS 116, 23 (2019)

# Multidisciplinary field

- Climate
- Earthquakes
- Traffic
- Biology
- Brain
- Finance
- Infrastructures



New concepts emerge!



# From network theory back to physics: interdependent physical networks

## Single networks

- Percolation theory
- Remove  $1-p$  fraction of nodes
- Functioning – existence of giant component
- Network resilience

- Second order phase transition
- Critical behaviour
- Universality classes

Scaling relations

$$d\nu = 2\beta + \gamma$$

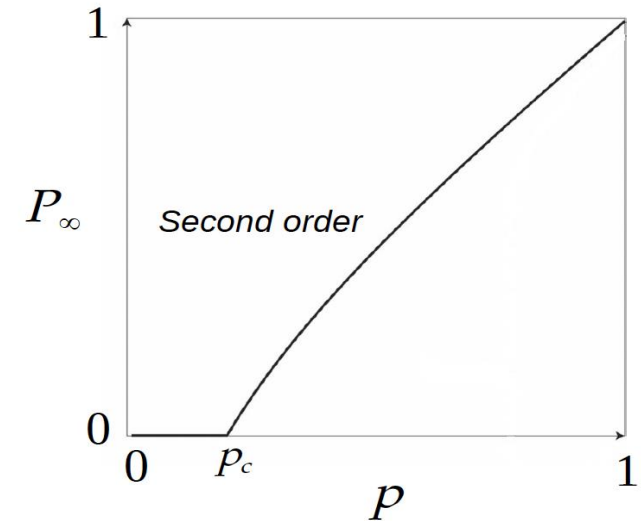
$$\delta - 1 = \gamma/\beta$$

Critical exponents

$$P_\infty \sim (p - p_c)^\beta$$

$$\xi \sim |p - p_c|^{-\nu}$$

$$\chi \sim |p - p_c|^{-\gamma}$$





# Blackout in Italy, September 2003

**3:21 am:** a tree too close to a power station recieves the discharge of a line

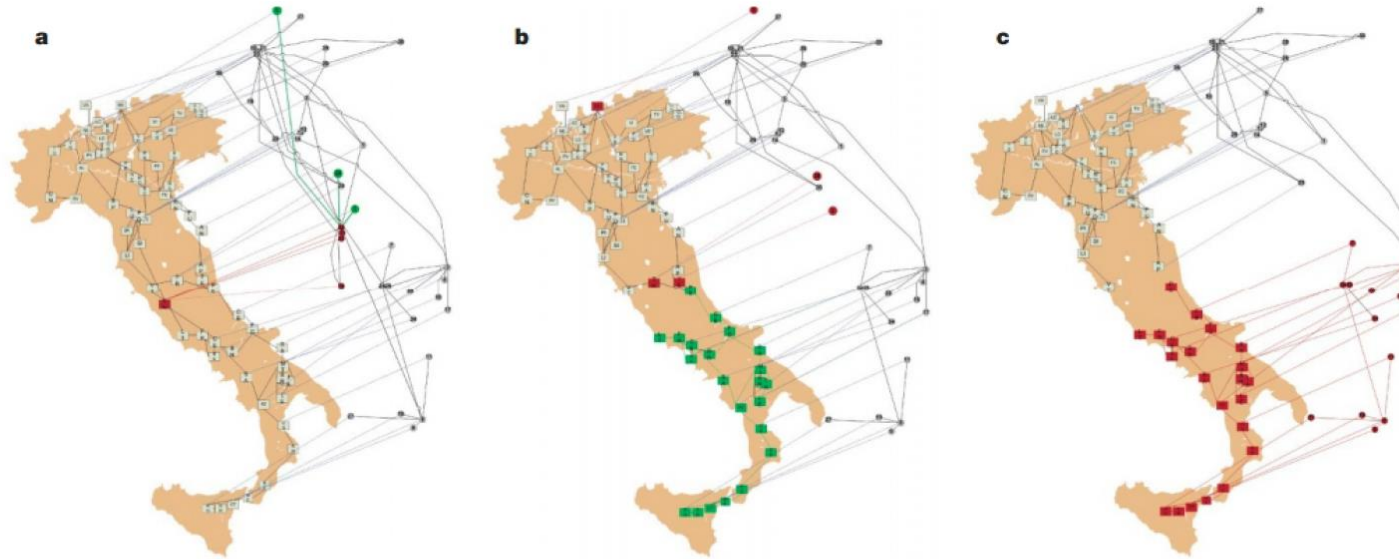


# Blackout in Italy, September 2003

3:23 am: the power outage extends to the whole country

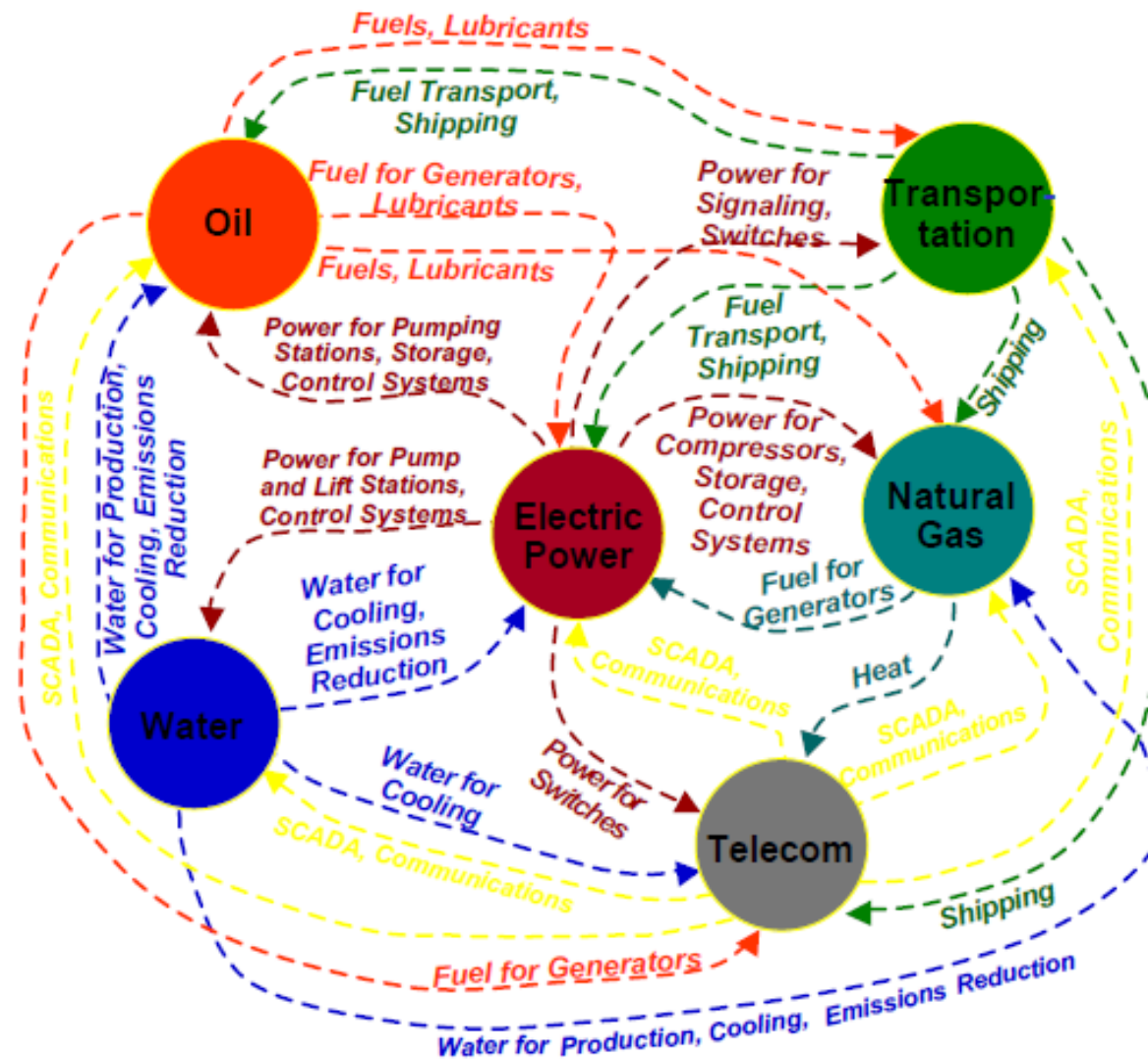


# Interdependent networks

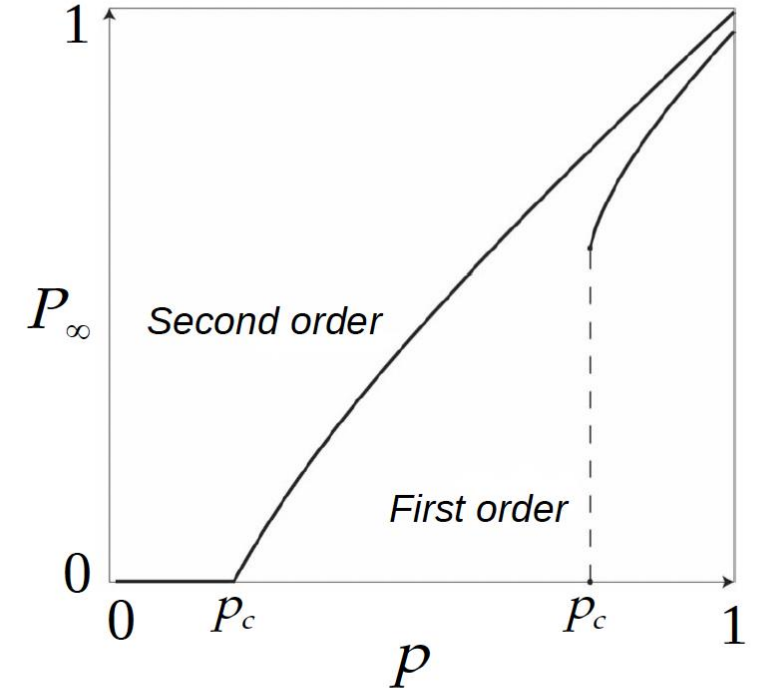
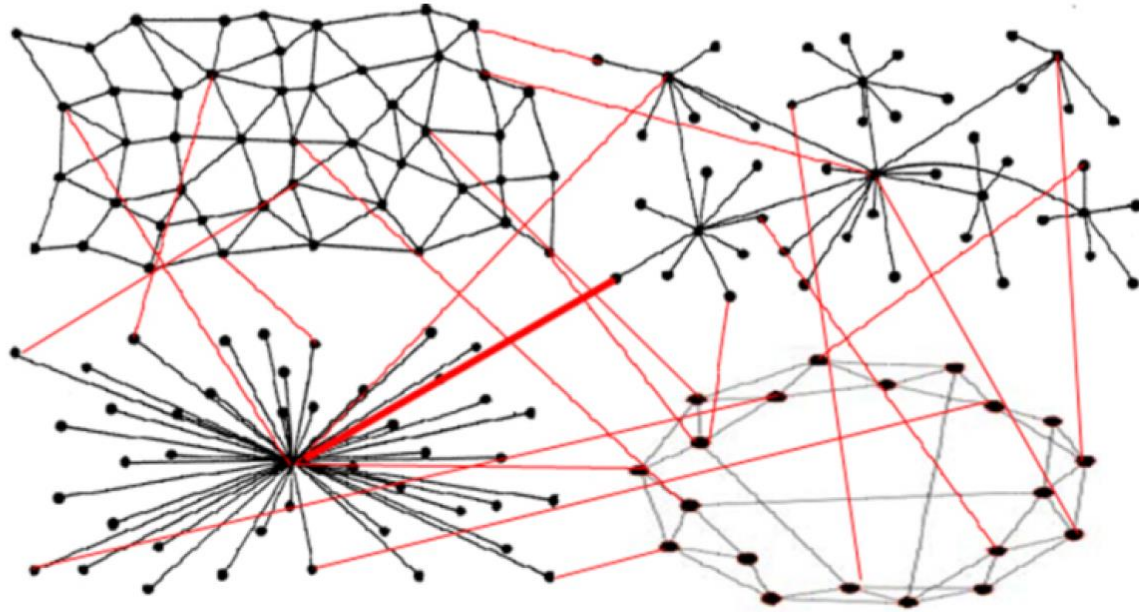


- Two networks: **Communication** network and **power-grid** network
- Two types of links: **Connectivity** within each network and **dependency** between the networks
- **Dependency**: If a node in one network fails, another node in the other network will fail as well

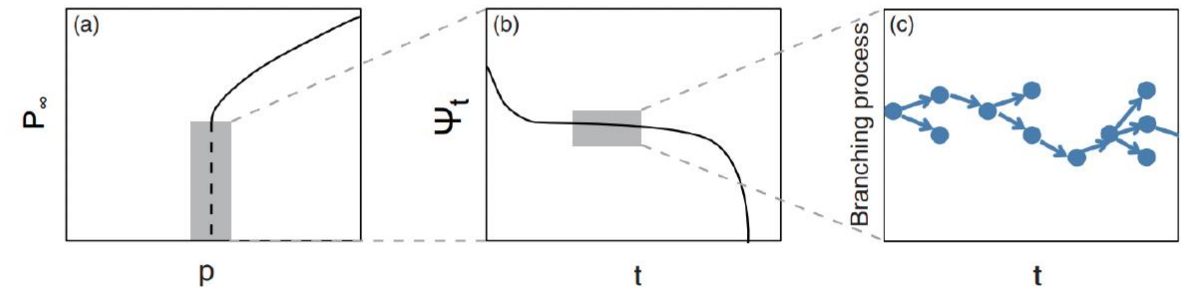
# How interdependent are infrastructures?



# Interdependent networks

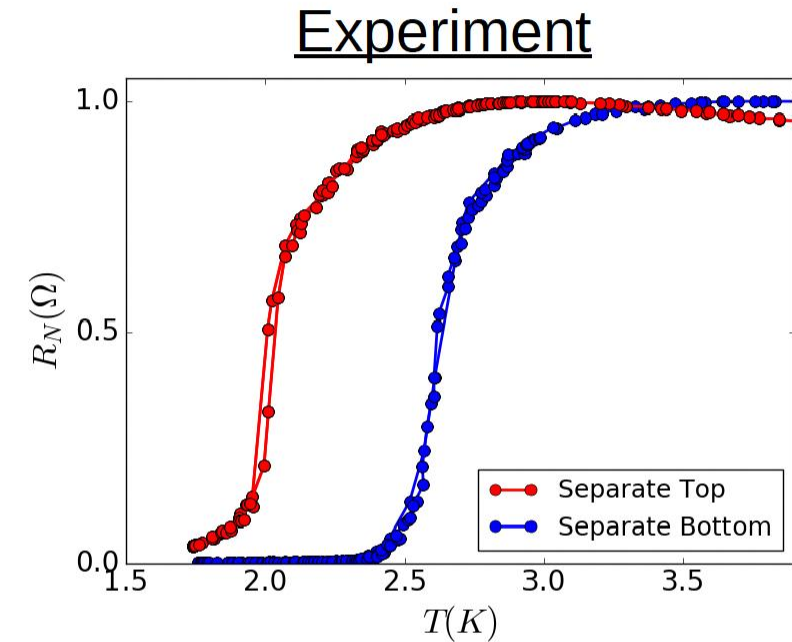
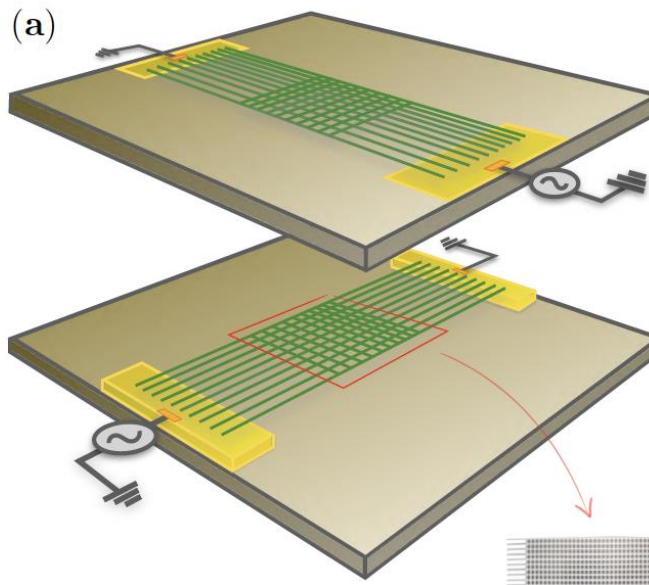
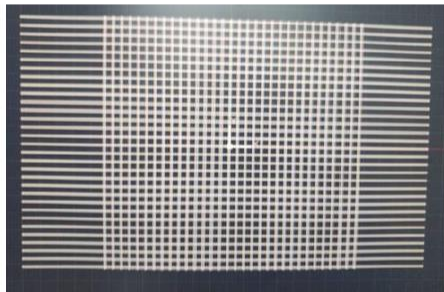
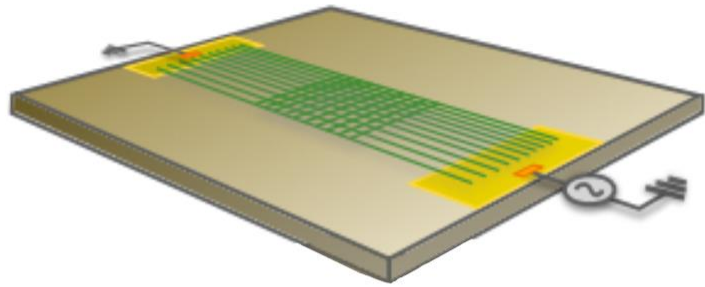


- Cascading failures
- Local failure leads to total collapse

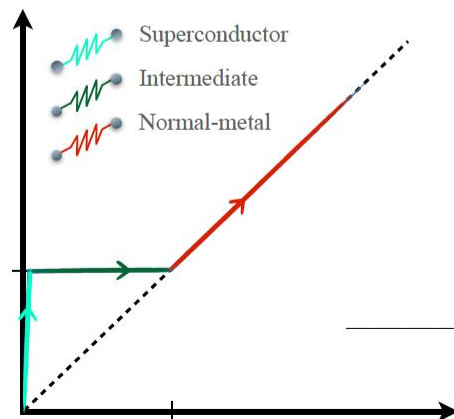


Can we apply the concept of interdependent networks in physical systems?

# Single Superconducting networks

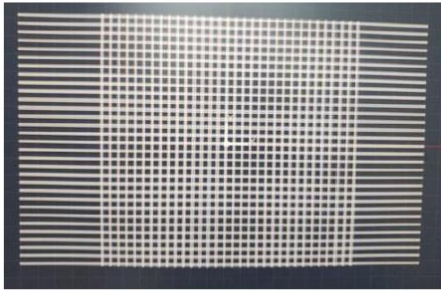
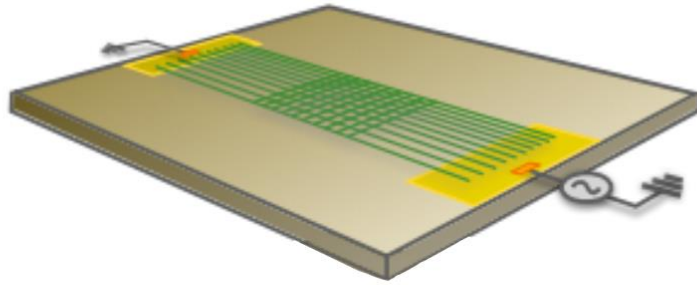


Josephson junction characteristics

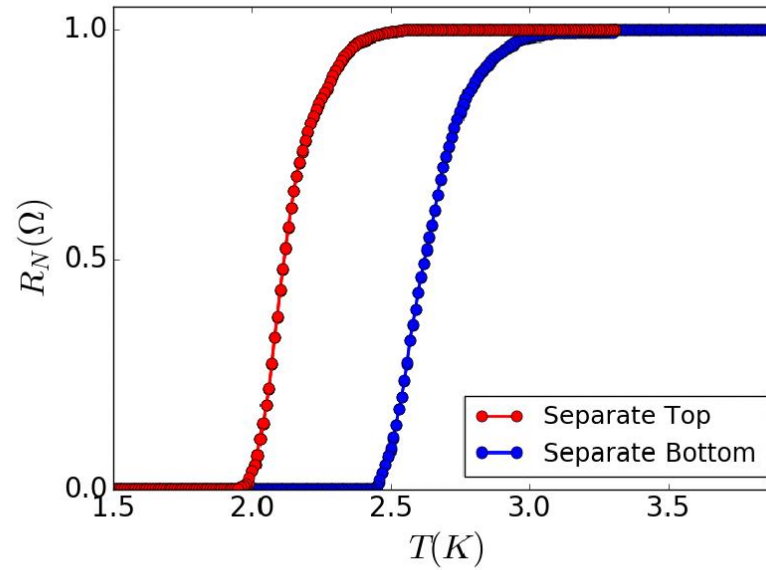


- Second order phase transition
- Superconductor-normal transition

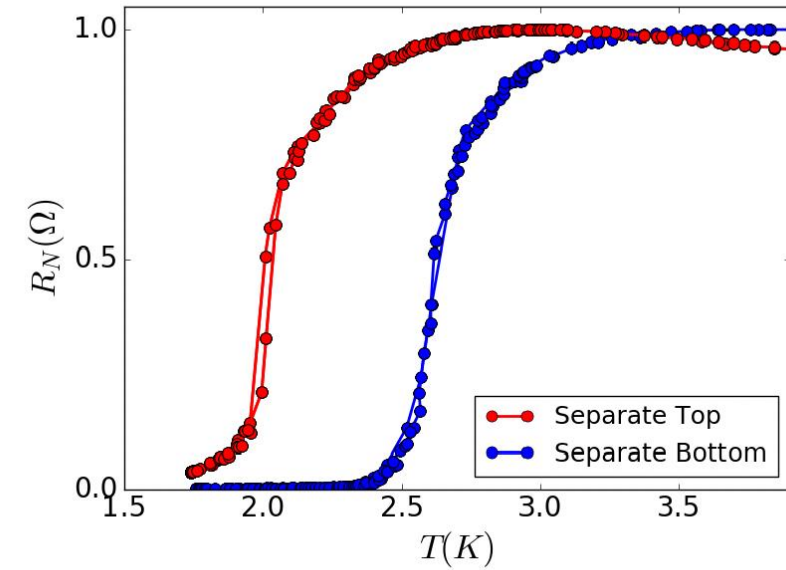
# Single Superconducting networks



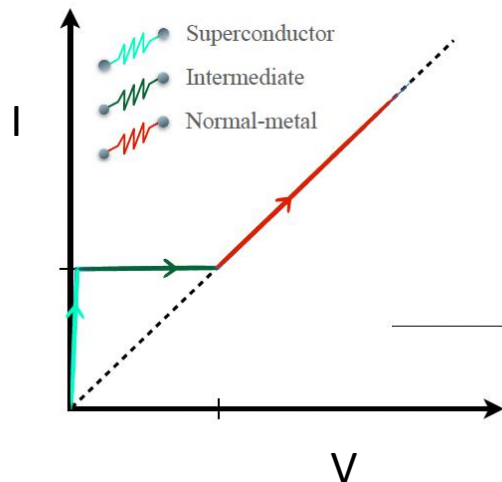
Theory



Experiment



Josephson junction characteristics

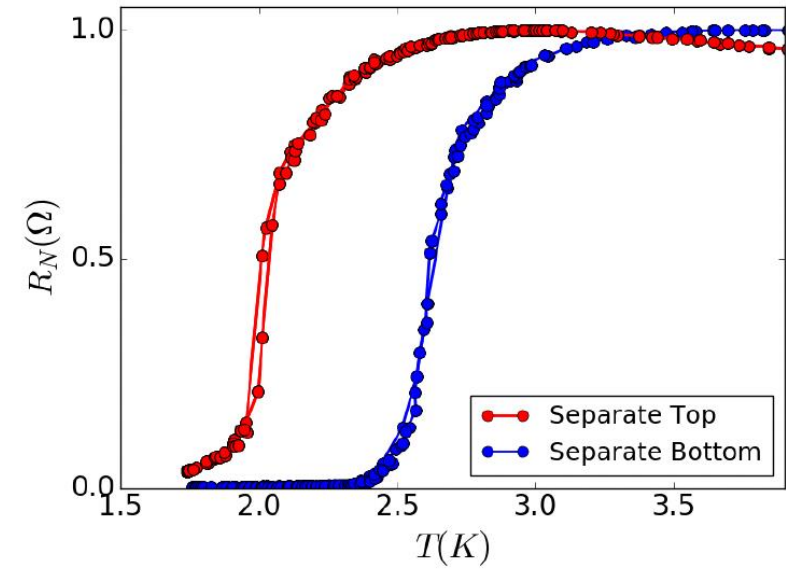
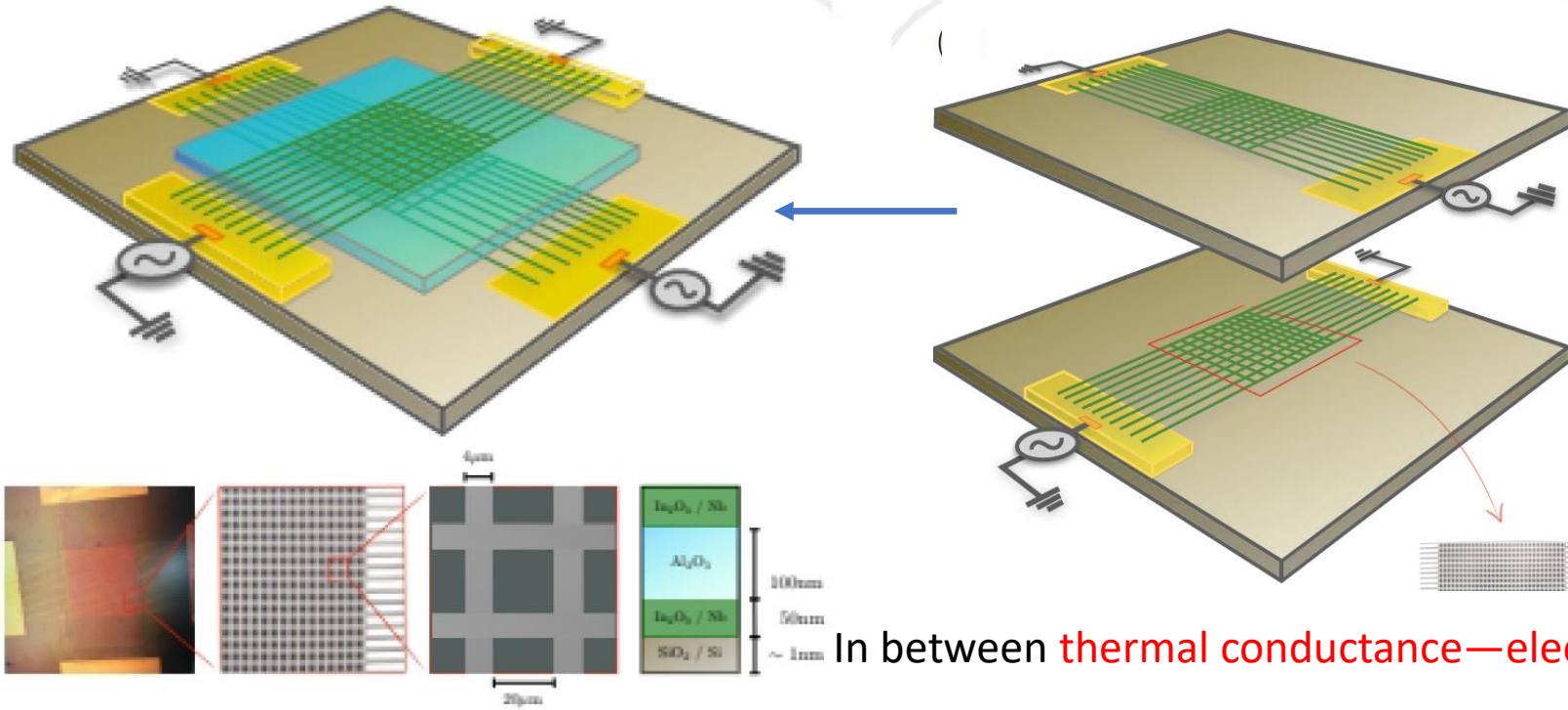


- Second order phase transition
- Superconductor-normal transition

Kirchhoff equations:  $G \cdot W = I_{inj}$

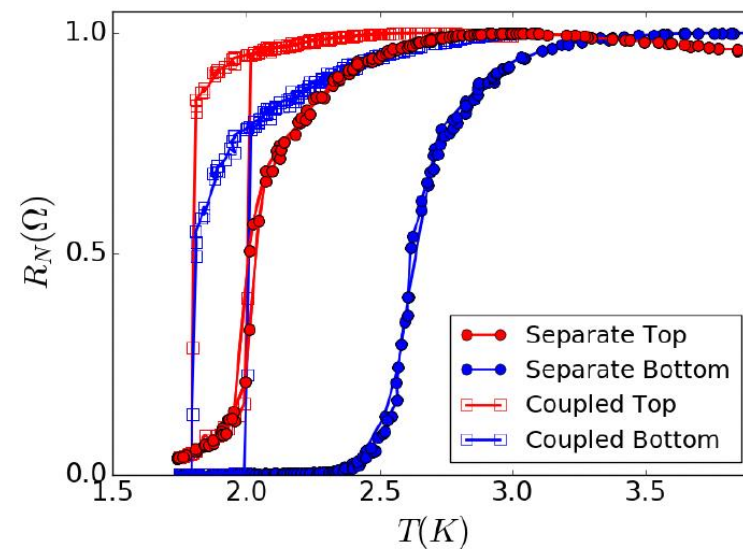
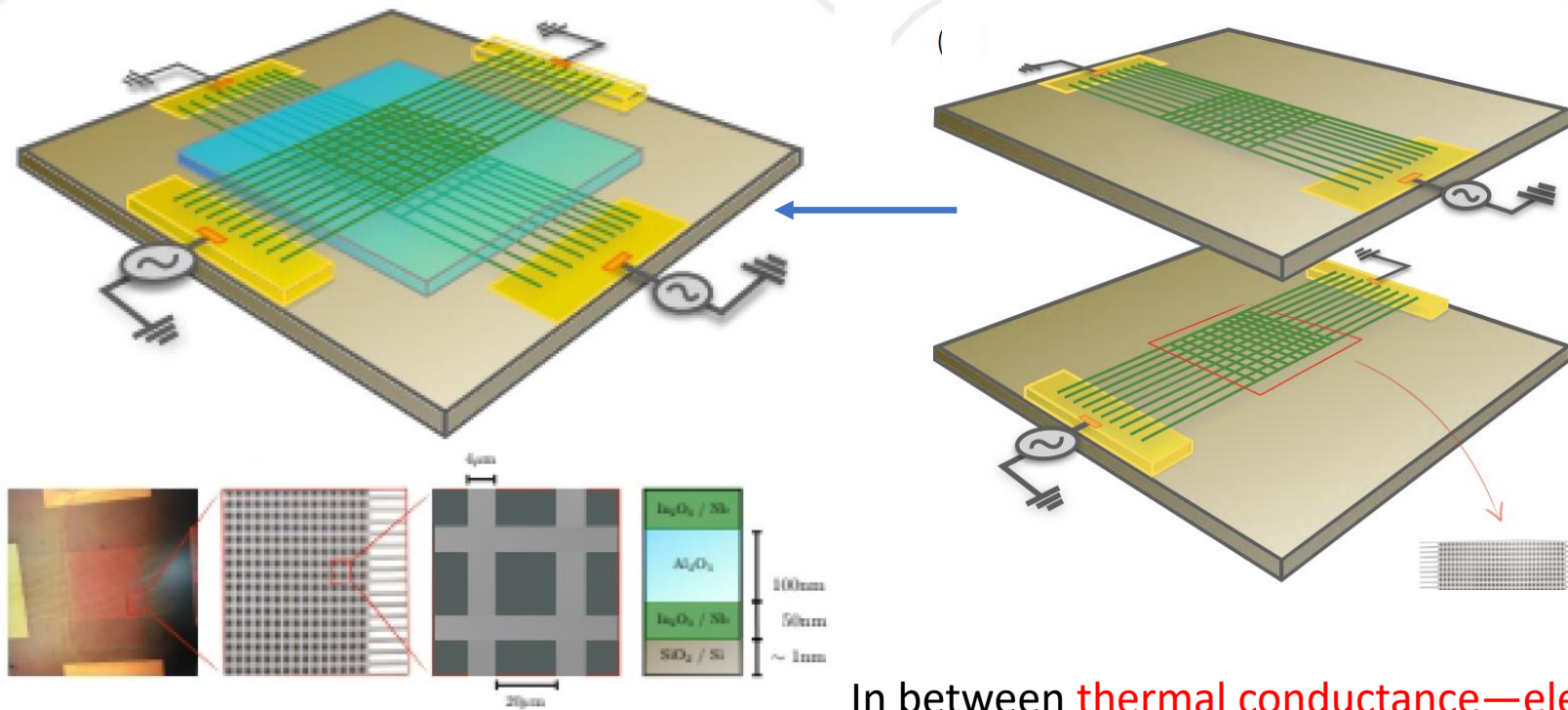


# Interdependent superconducting networks

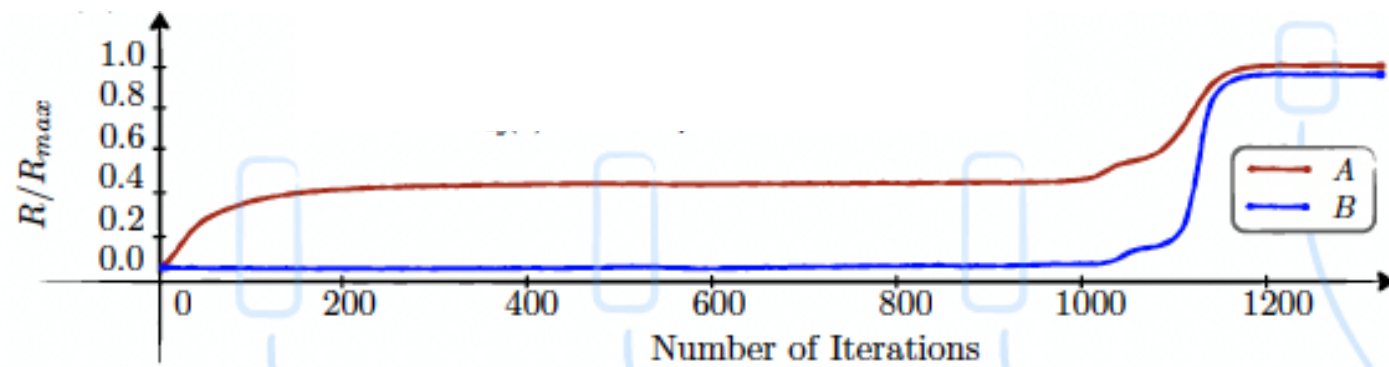


In between thermal conductance—electric insulator

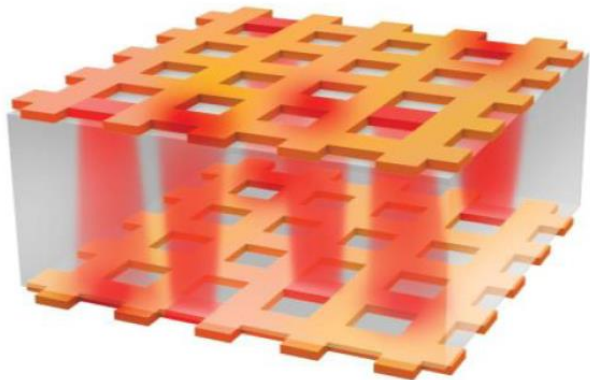
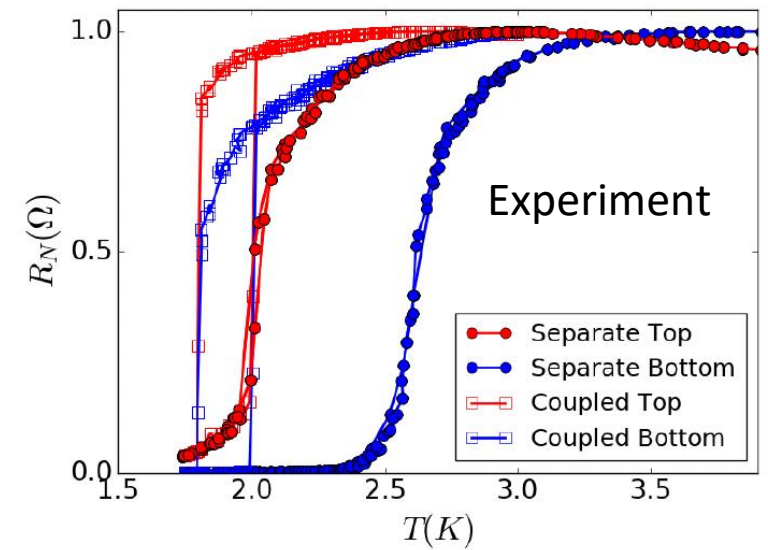
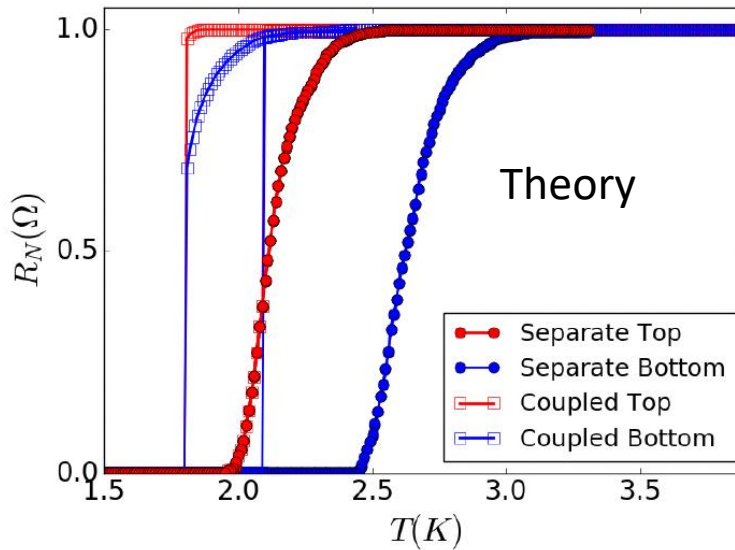
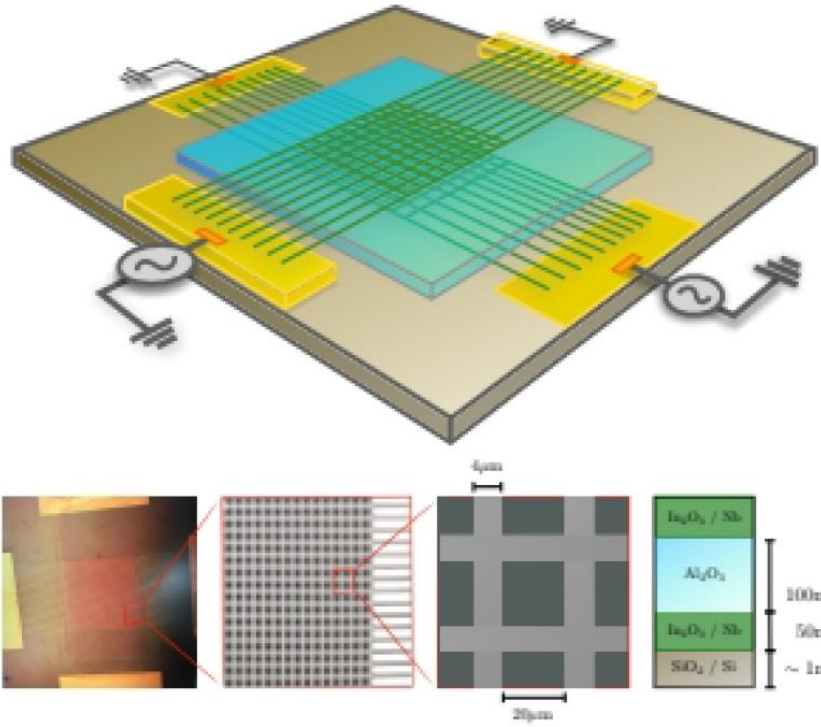
# Interdependent superconducting networks



In between **thermal conductance**—**electric insulator**



# Interdependent superconducting networks



- Dependency – **heat dissipation!**
- Cascade of heat!

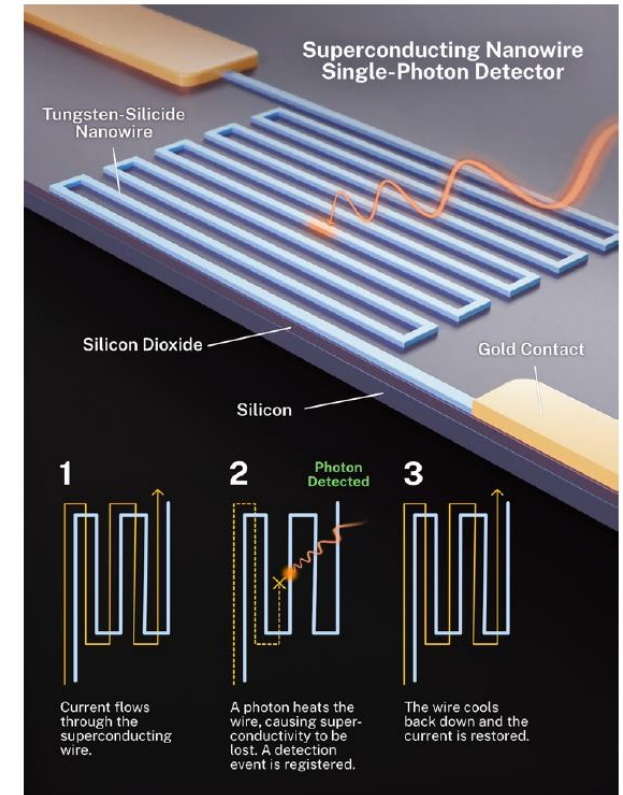
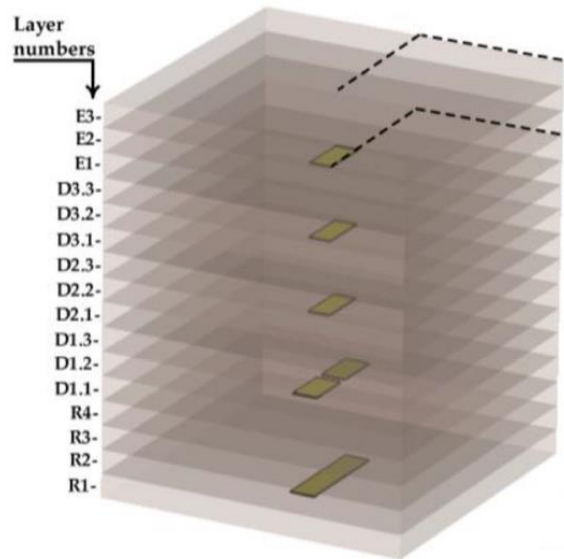
$$G_1 \cdot W_1 = I_{inj,1} \quad G_2 \cdot W_2 = I_{inj,2}$$

$$\begin{pmatrix} T_{eff}^1 \\ T_{eff}^2 \end{pmatrix} = T + \begin{pmatrix} \alpha_{11} & \alpha_{12} \\ \alpha_{21} & \alpha_{22} \end{pmatrix} \begin{pmatrix} R_1 I_{b,1}^2 \\ R_2 I_{b,2}^2 \end{pmatrix}$$

Ivan Bonamassa et al arXiv:2207.01669 (2022)

# Applications

- Single photon detector
- Multilayer materials
- Biological/Chemicals sensors?



# Summary

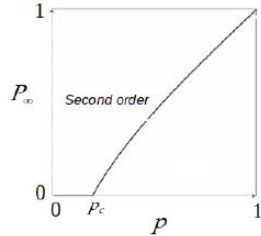
## Physics

### Physics and networks

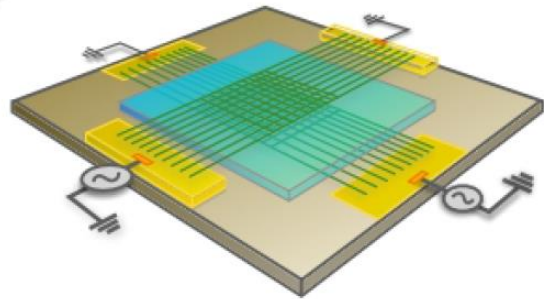
$$P_\infty \sim (p - p_c)^\beta$$

$$\xi \sim |p - p_c|^{-\nu}$$

$$\chi \sim |p - p_c|^{-\gamma}$$



### Interdependent physical networks



## Network theory

### Multidisciplinary field

Climate

Brain

Finance

Traffic

**Network theory**

Biology

Infrastructures

Earthquakes

### Interdependent networks

