

# Network applications in physiology and biology

Shlomo Havlin  
Bar-Ilan University  
Usrael

[1] [Reviving a failed network through microscopic interventions](#)

Sanhedrai, J Gao, A Bashan, M Schwartz, S Havlin, B Barzel  
Nature Physics 18 (3), 338-349 (2022)

[2] [Sustaining a network by controlling a fraction of nodes.](#) H Sanhedrai, S Havlin  
arXiv preprint arXiv:2205.13377 (2022)

[3] [Connectivity of EEG synchronization networks increases for Parkinson's disease patients with freezing of gait](#)

E. Asher, R. Bartcsh, S. Havlin et al  
Communications Biology 4 (1), 1-10 (2022)—By **Ronny Bartsch on Tuesday**

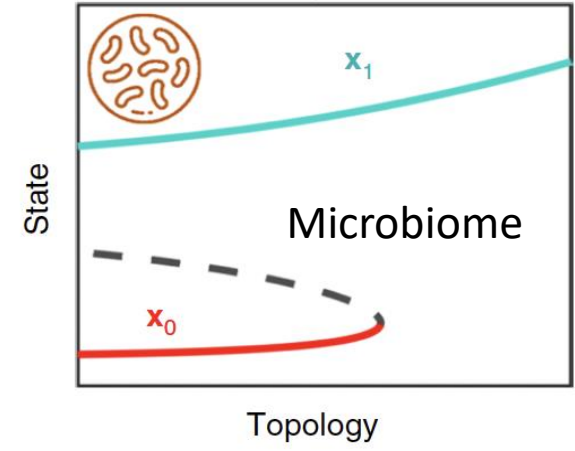
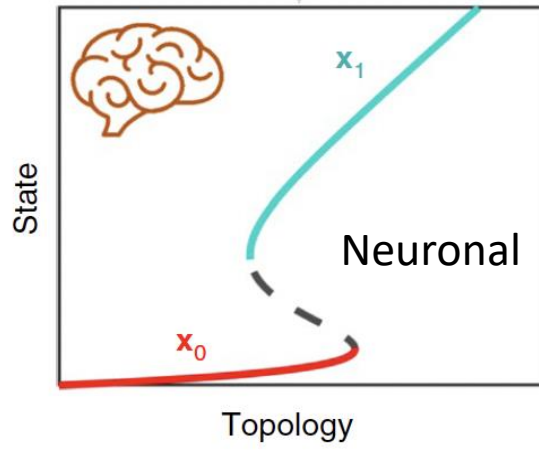
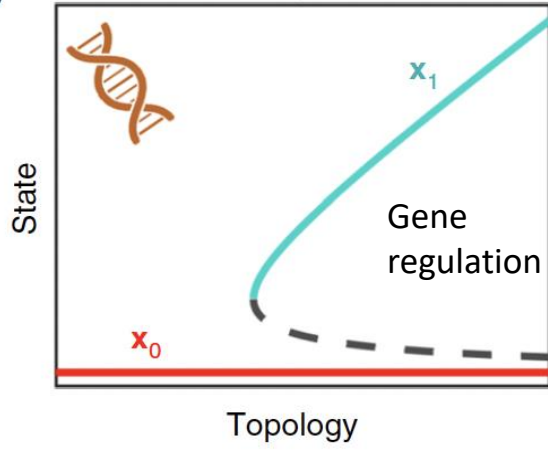
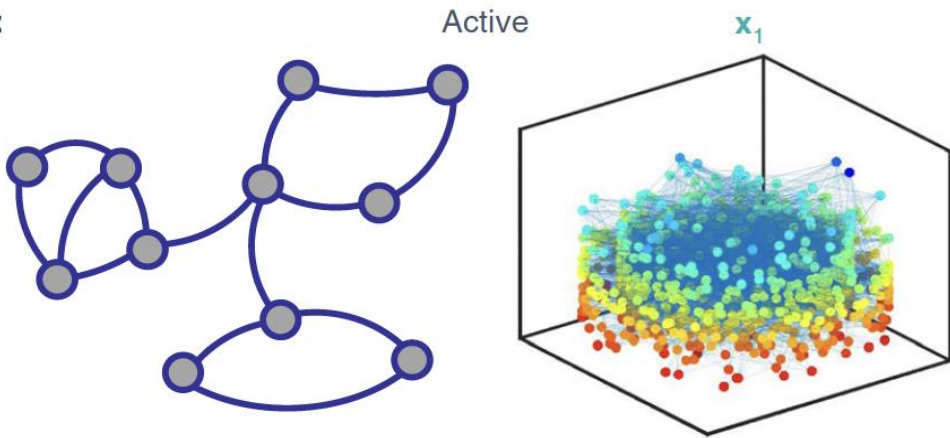
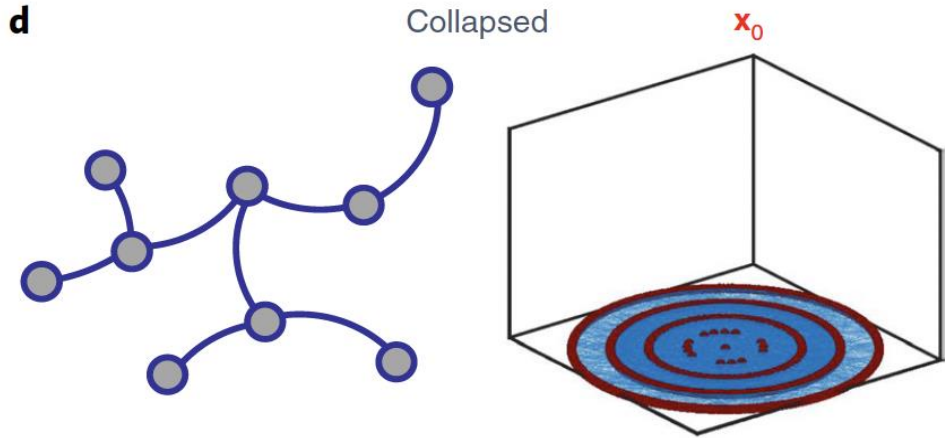
[4] Brain dynamic network during rest and personal performance  
Shu Guo et al, In preparation, 2022

# Reviving a failed network

Sanhedrai et al Nature Physics, 18, 338  
(2022)

**a**

$$\frac{dx_i}{dt} = M_0(x_i) + \sum_{j=1}^N A_{ij} W_{ij} M_1(x_i) M_2(x_j)$$

**b****c****d**

Topology

Topological perturbation

# Example: Gene regulation



$$\frac{dx_i}{dt} = -x_i + \sum_{j=1}^N A_{ij} \frac{x_j^2}{1 + x_j^2}$$

Michaelis-Menten (MM)  
Model for subcellular  
dynamics

# Example: Gene regulation



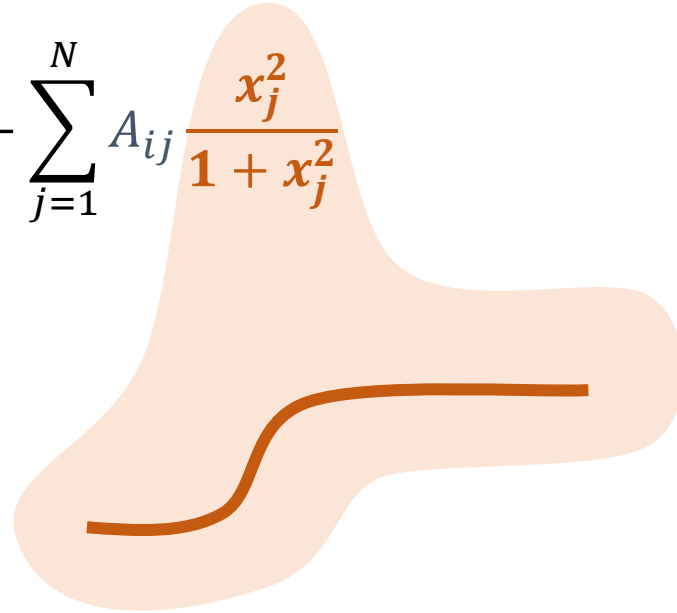
$$\frac{dx_i}{dt} = -x_i + \sum_{j=1}^N A_{ij} \frac{x_j^2}{1 + x_j^2}$$



# Example: Gene regulation



$$\frac{dx_i}{dt} = -x_i + \sum_{j=1}^N A_{ij} \frac{x_j^2}{1 + x_j^2}$$

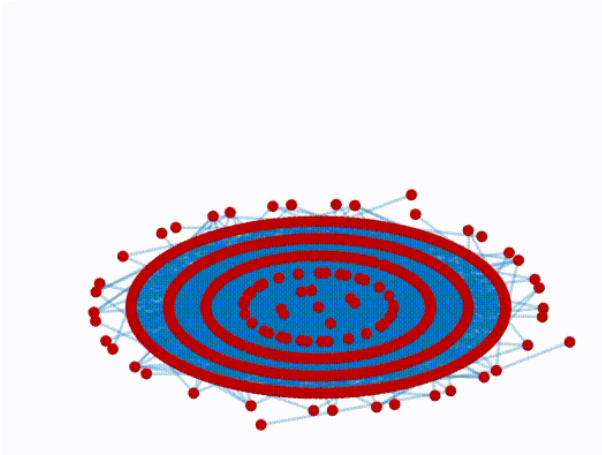


# Example: Gene regulation



$$\frac{dx_i}{dt} = -x_i + \sum_{j=1}^N A_{ij} \frac{x_j^2}{1 + x_j^2}$$

High initial conditions



Low initial conditions

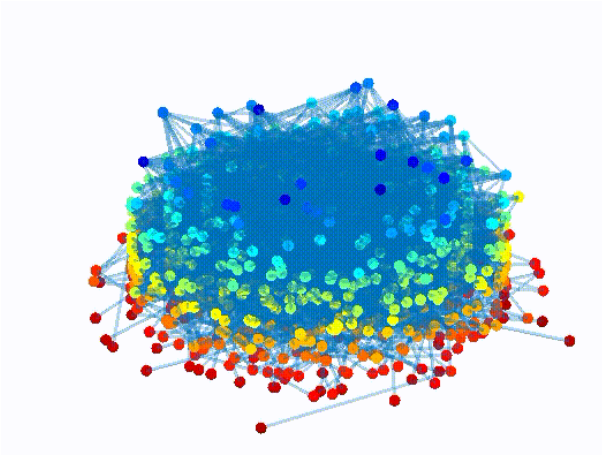
↔  
Bi-stability

# Example: Gene regulation



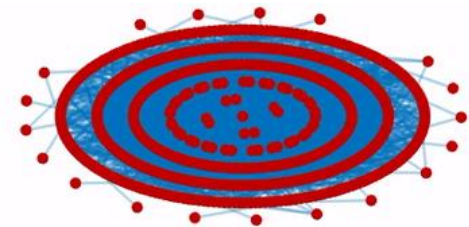
$$\frac{dx_i}{dt} = -x_i + \sum_{j=1}^N A_{ij} \frac{x_j^2}{1 + x_j^2}$$

High initial conditions



↔  
Bi-stability

Low initial conditions

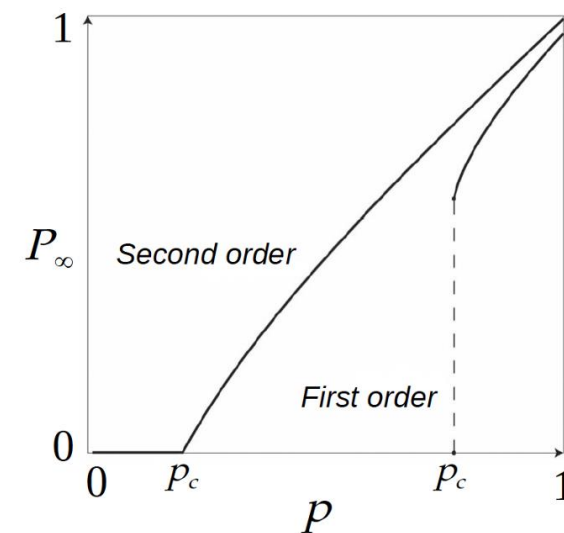
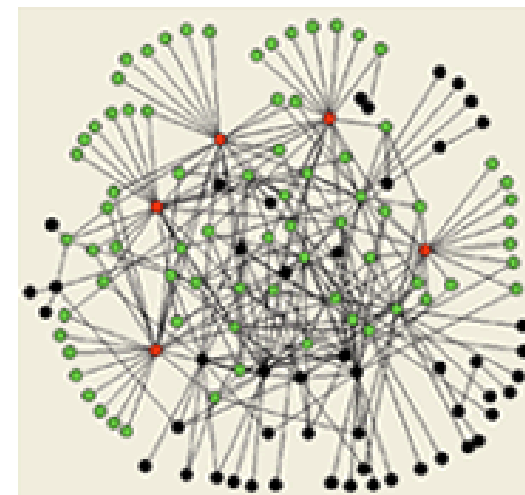
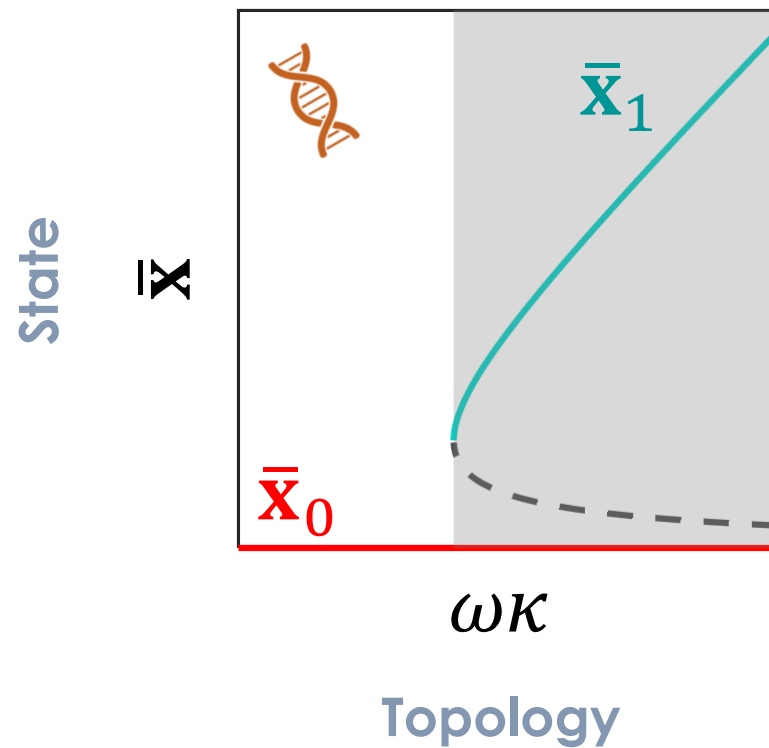




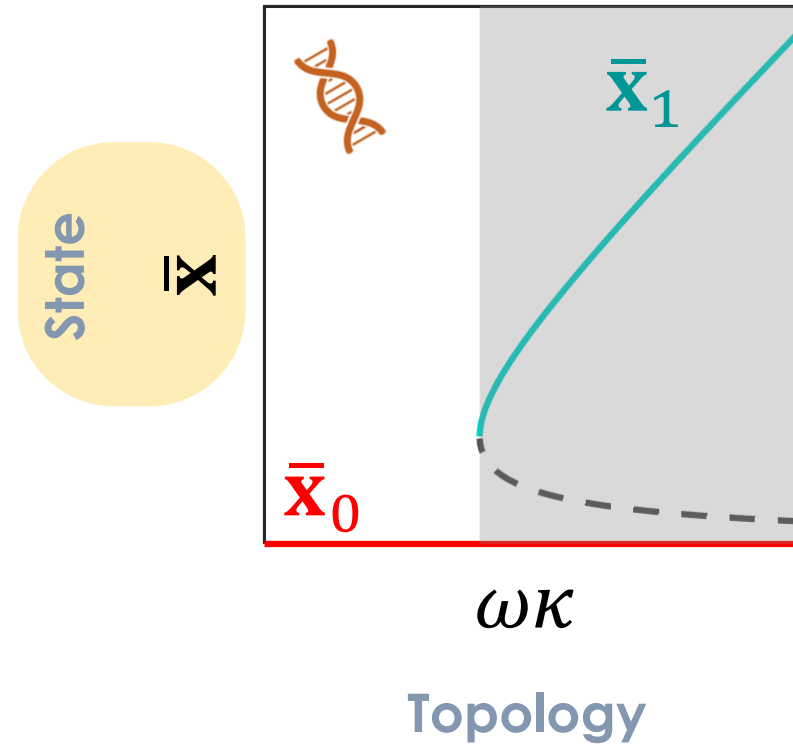
# Dynamic phase diagram

$$A_{ij} = \omega$$

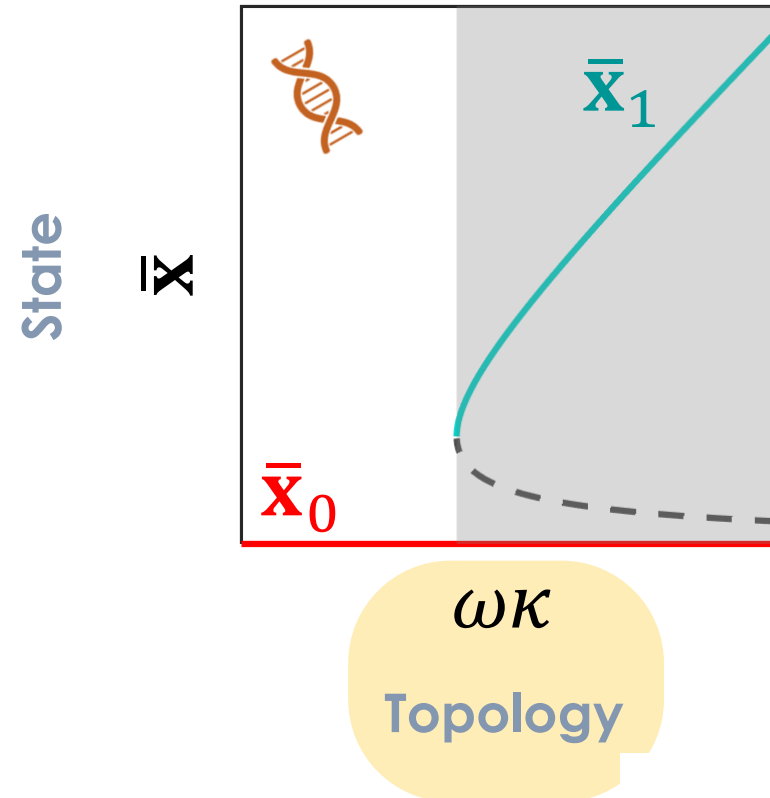
$$\kappa = \langle k^2 \rangle / \langle k \rangle - 1$$



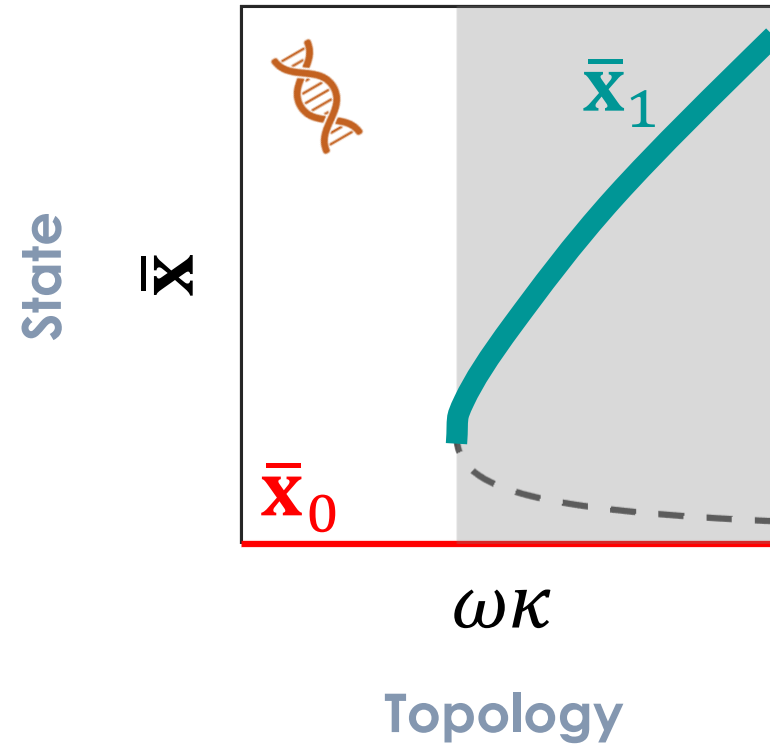
# Dynamic phase diagram



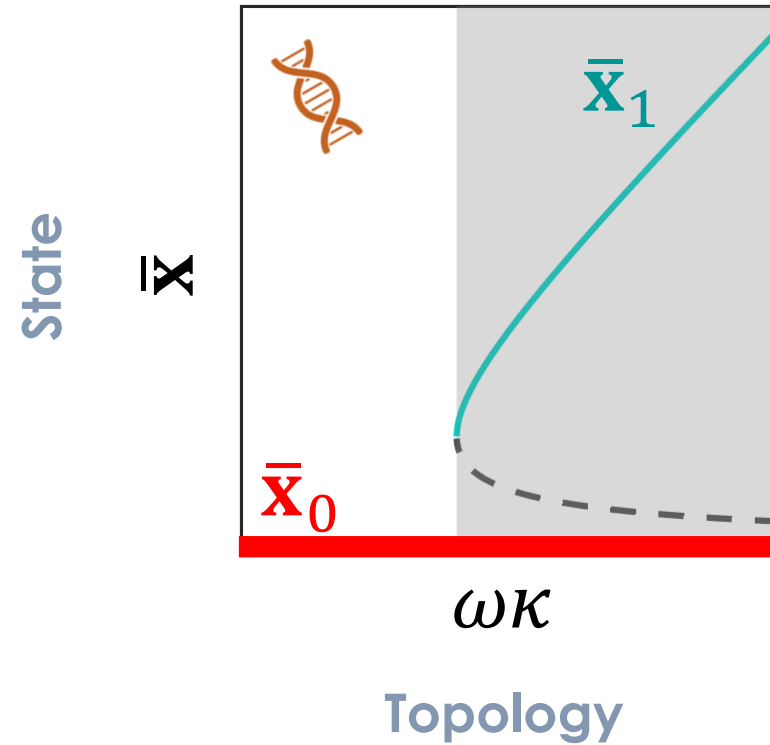
# Dynamic phase diagram



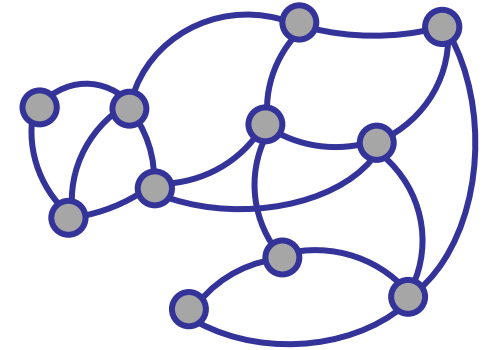
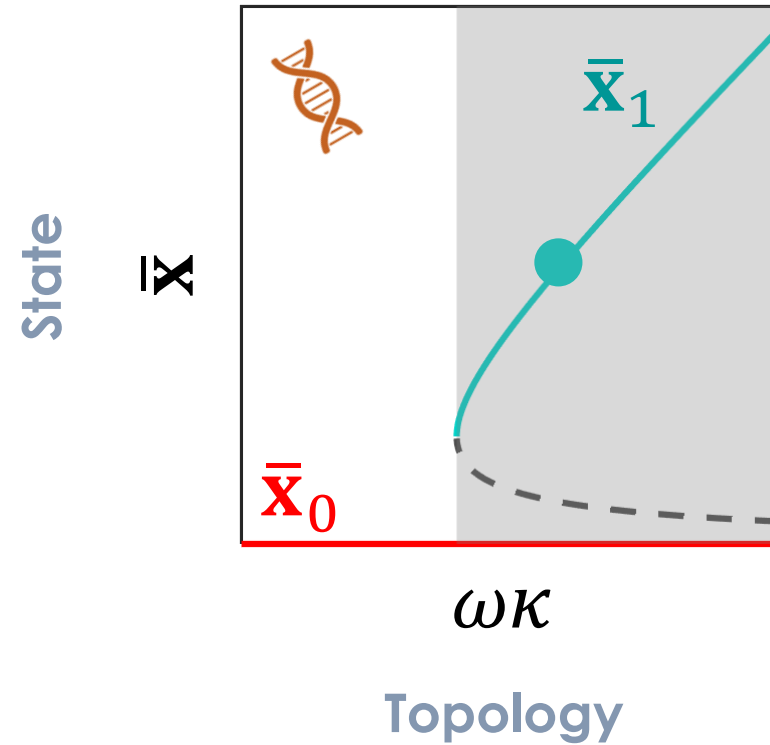
# Dynamic phase diagram



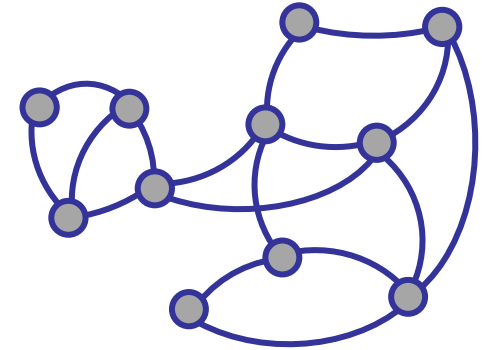
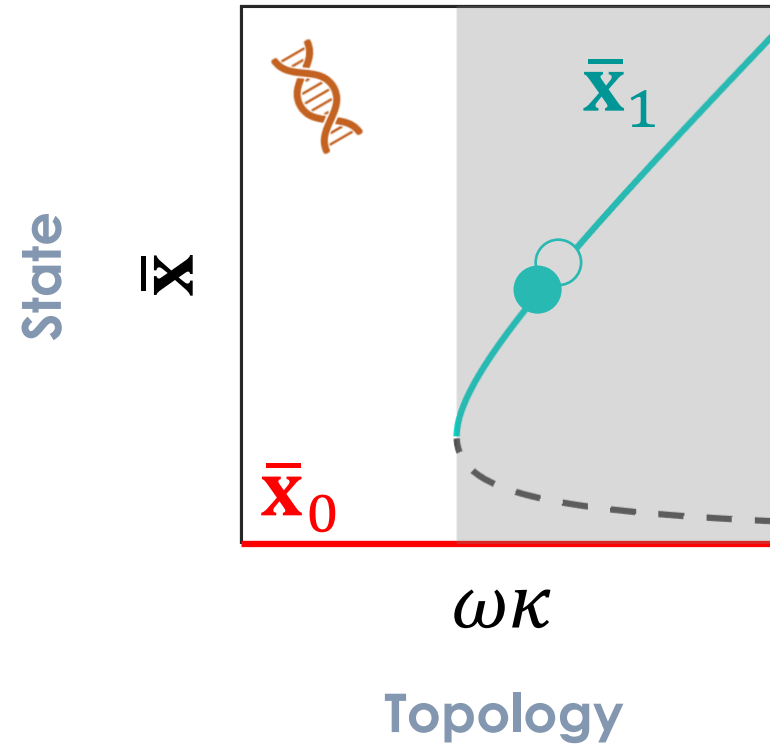
# Dynamic phase diagram



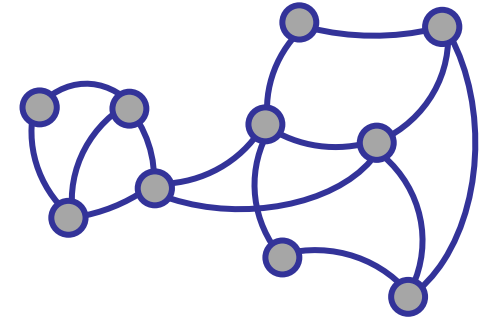
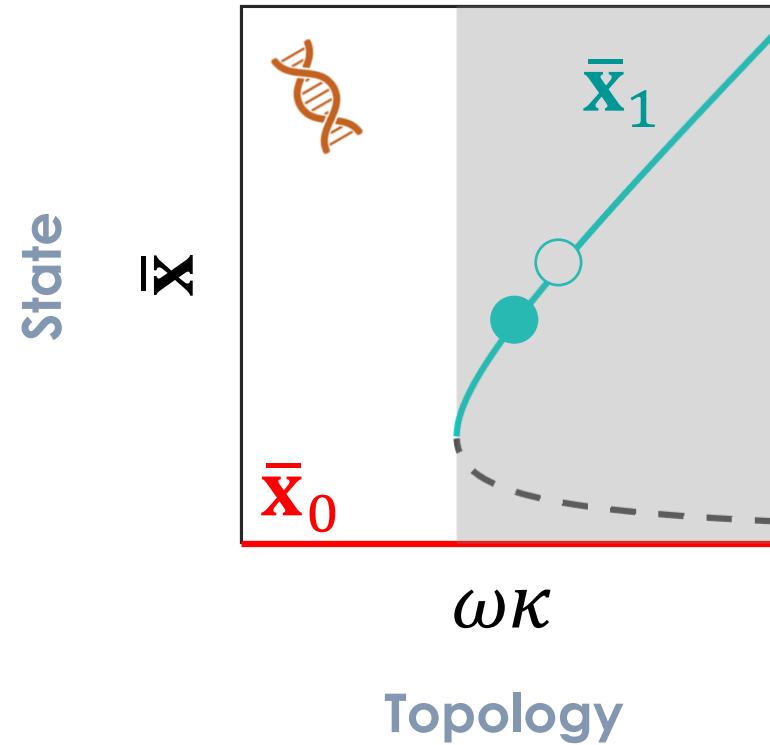
# Failure of a network



# Failure of a network

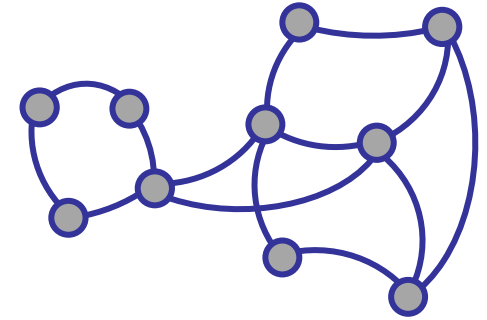
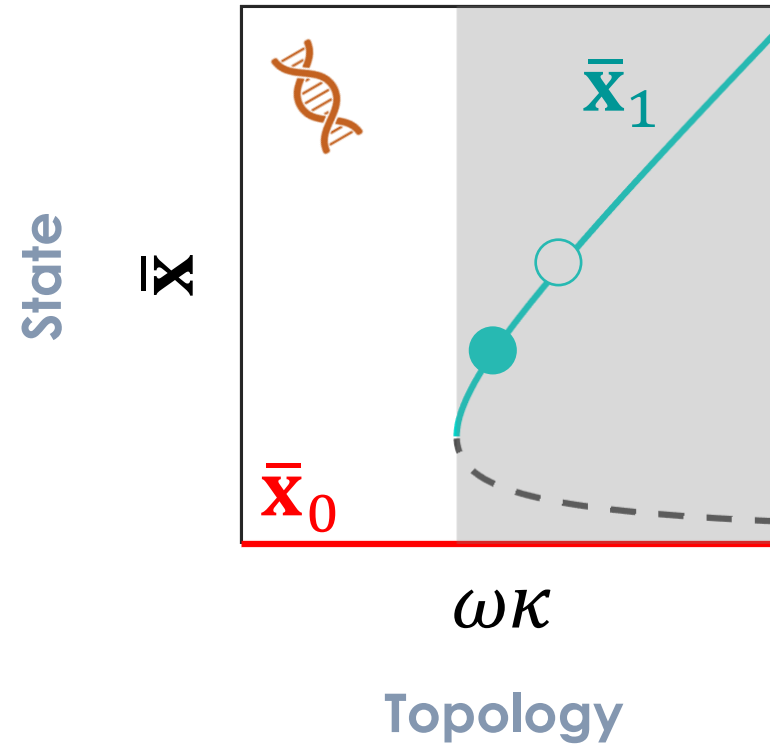


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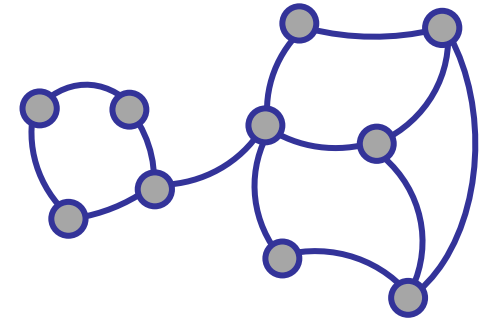
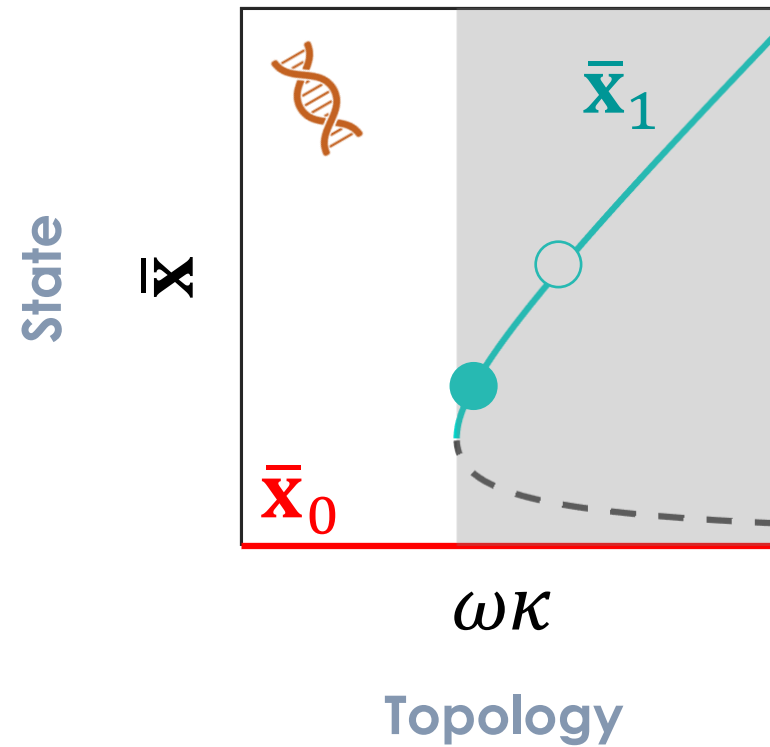




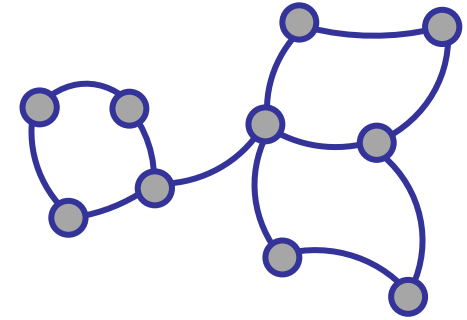
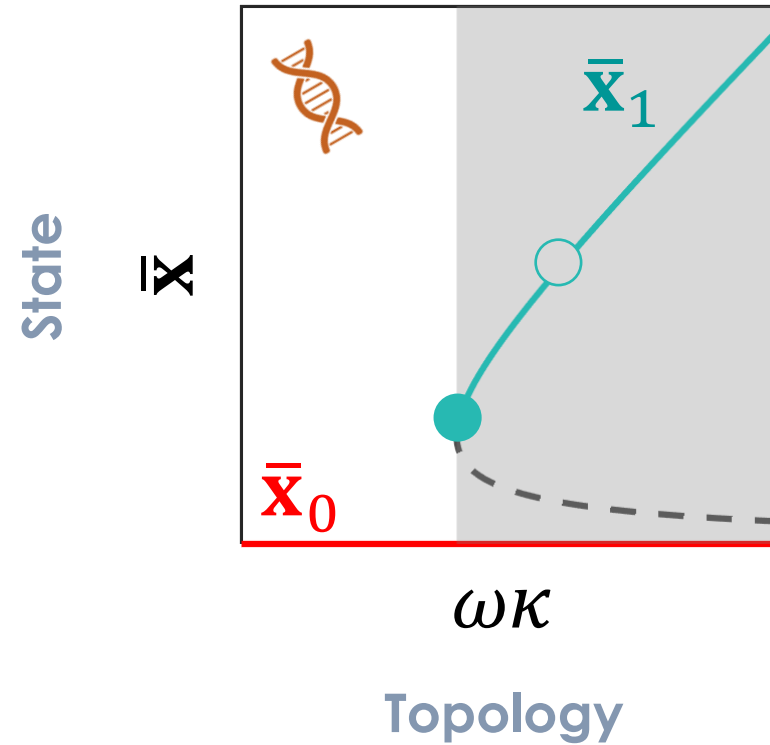
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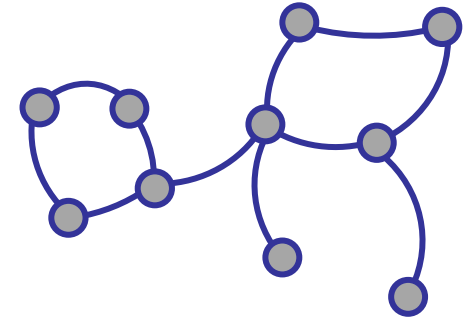
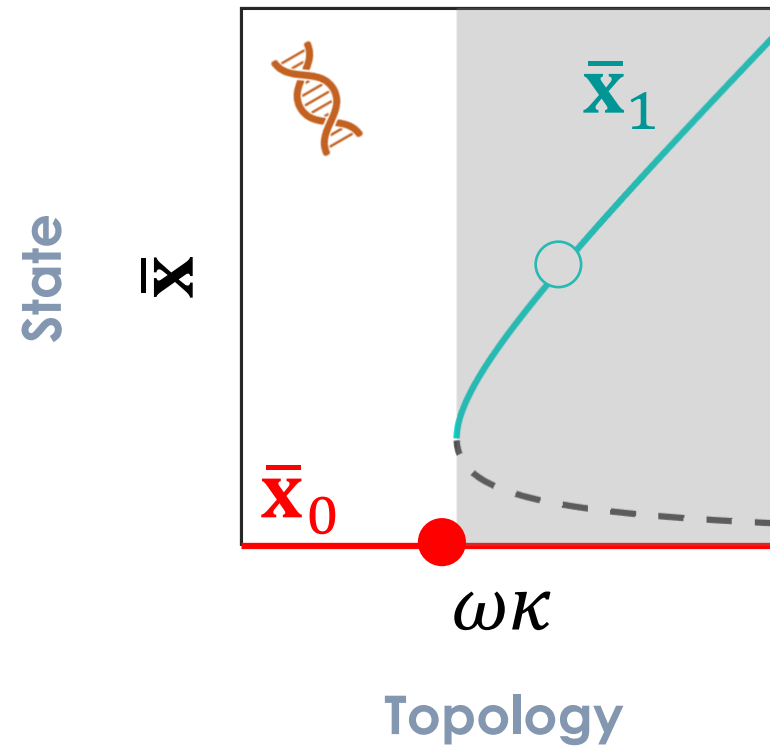
# Failure of a network



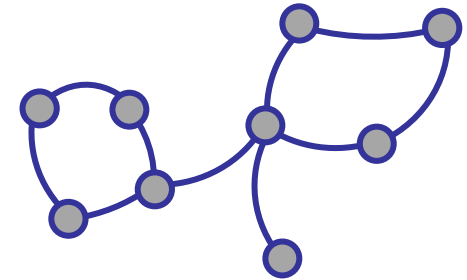
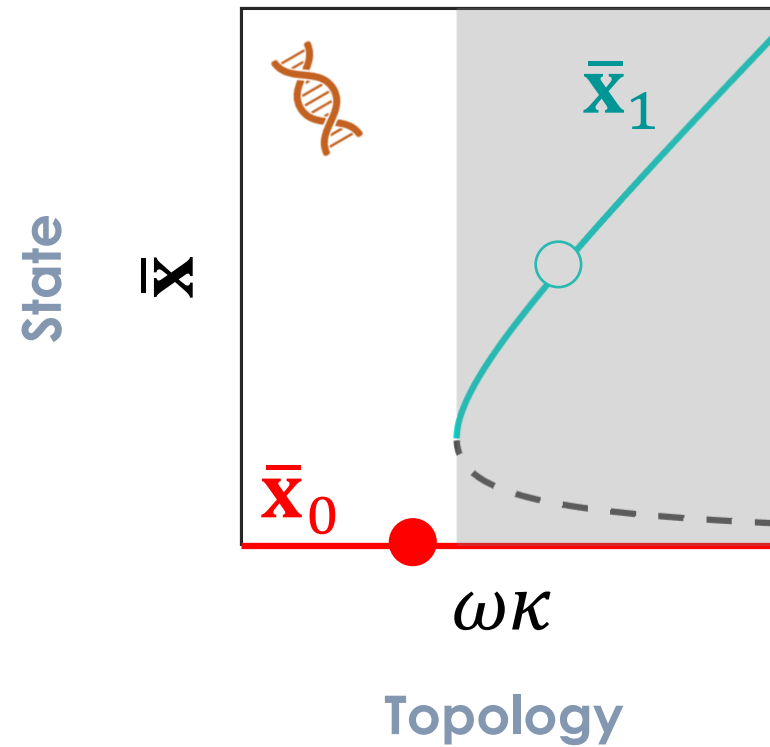
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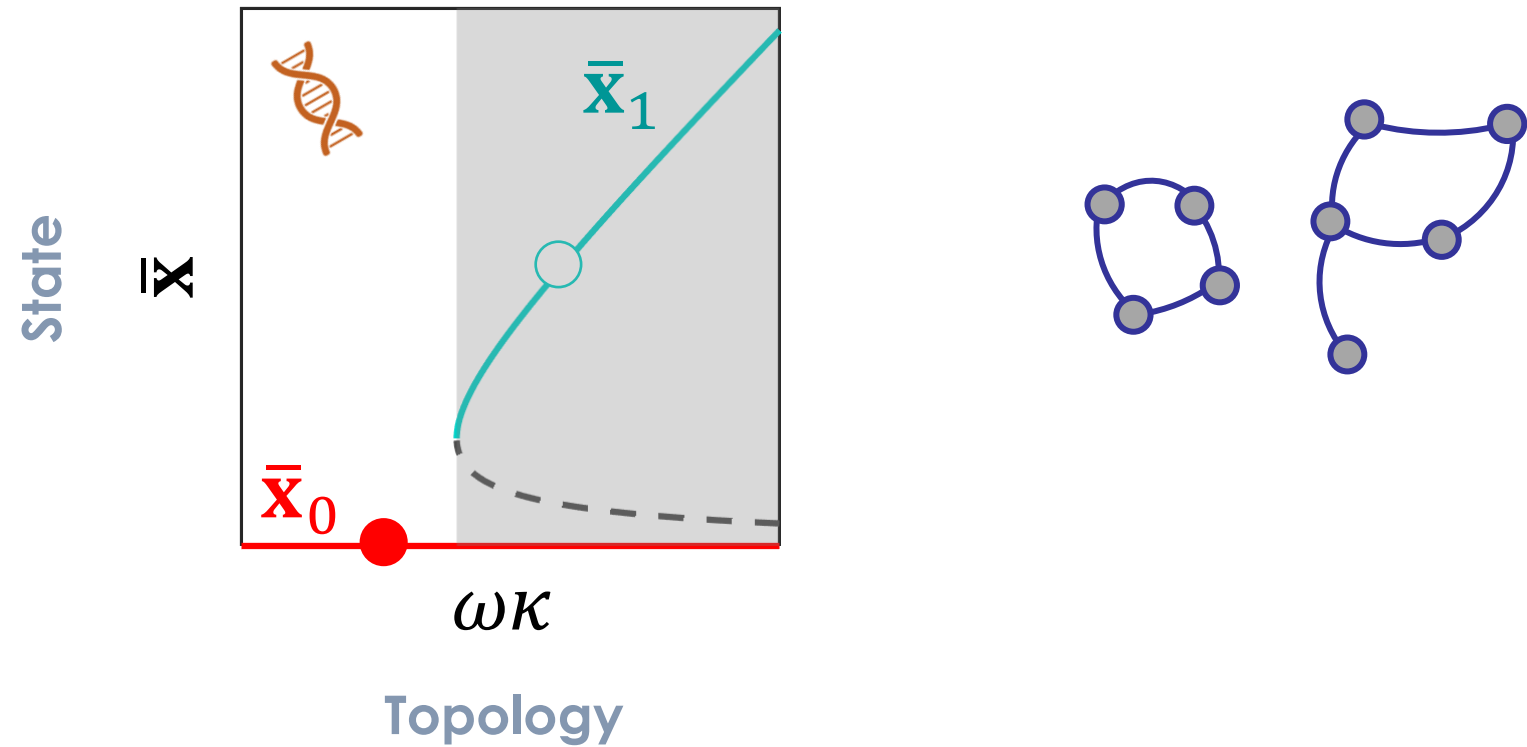
# Failure of a network



# Failure of a network

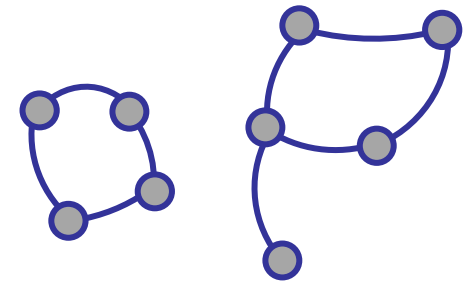
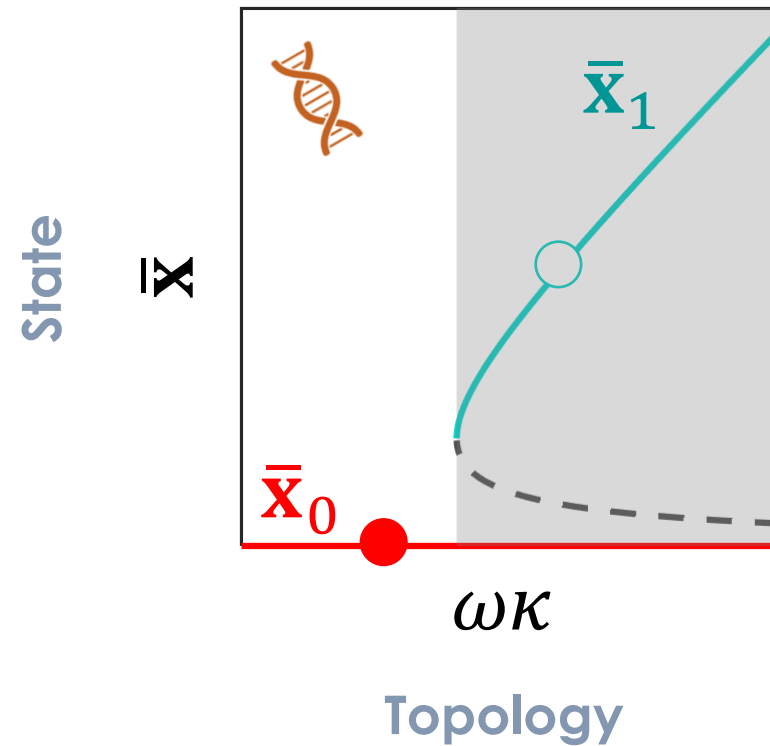


# Failure of a network

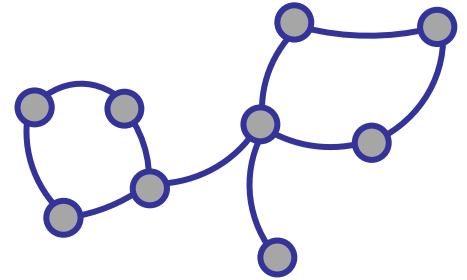
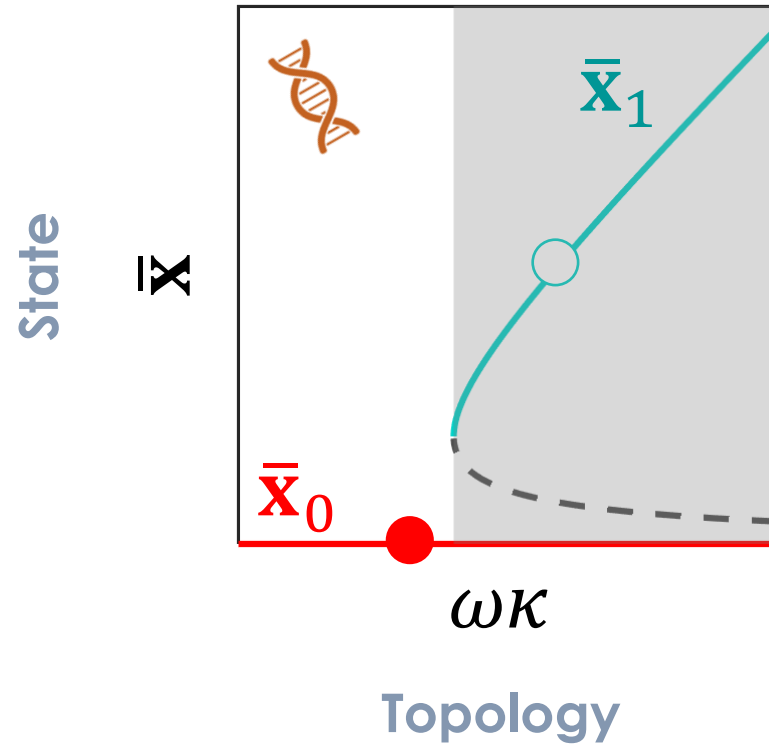


# Failure of a network

How can we revive it?

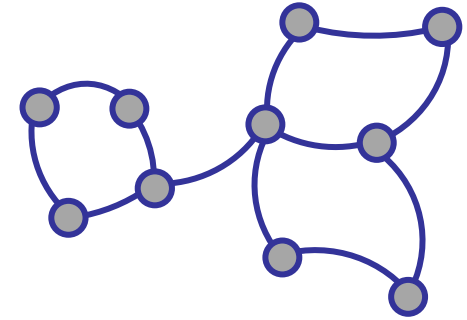
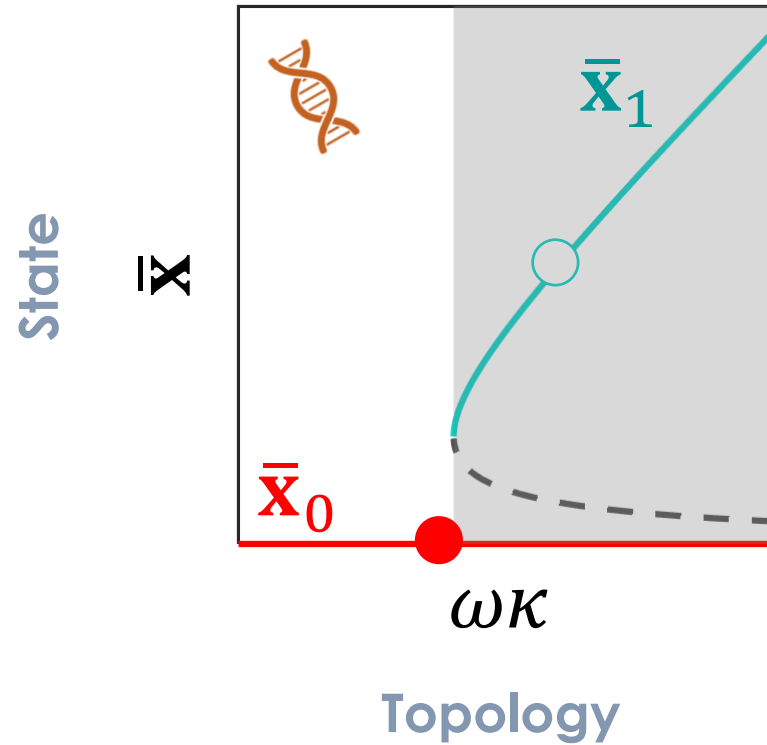


# Restructuring the network

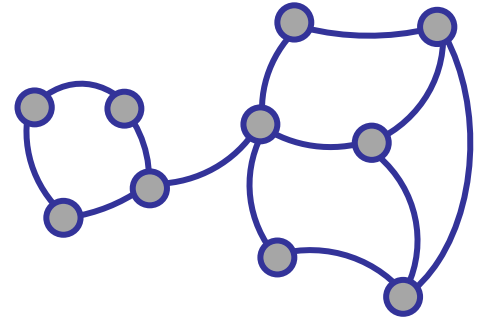
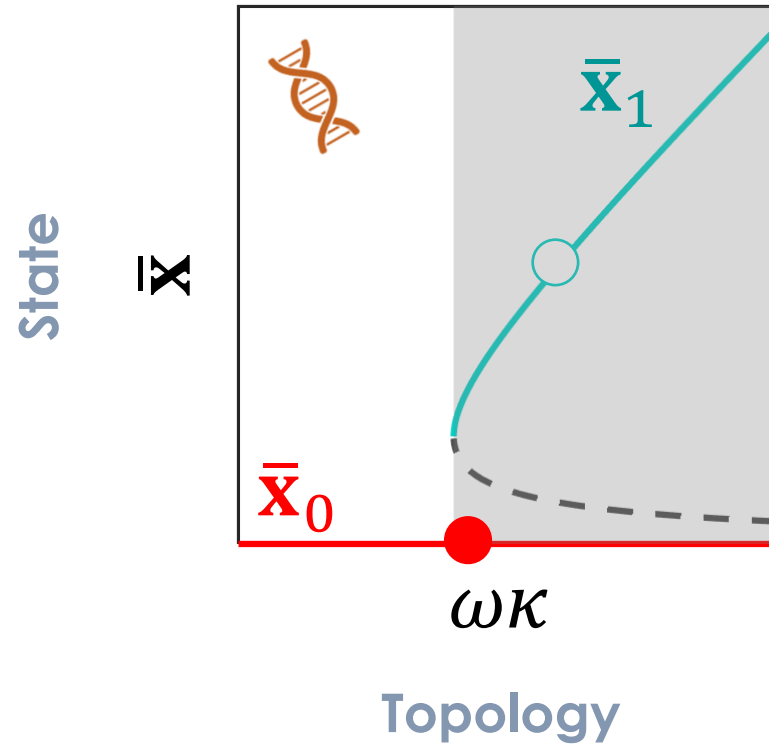




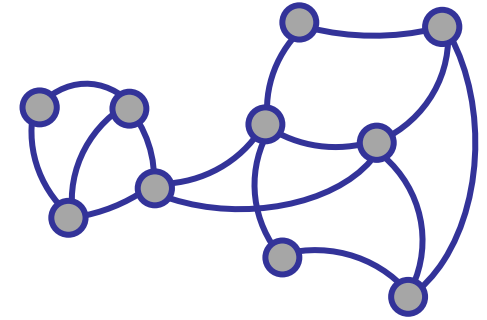
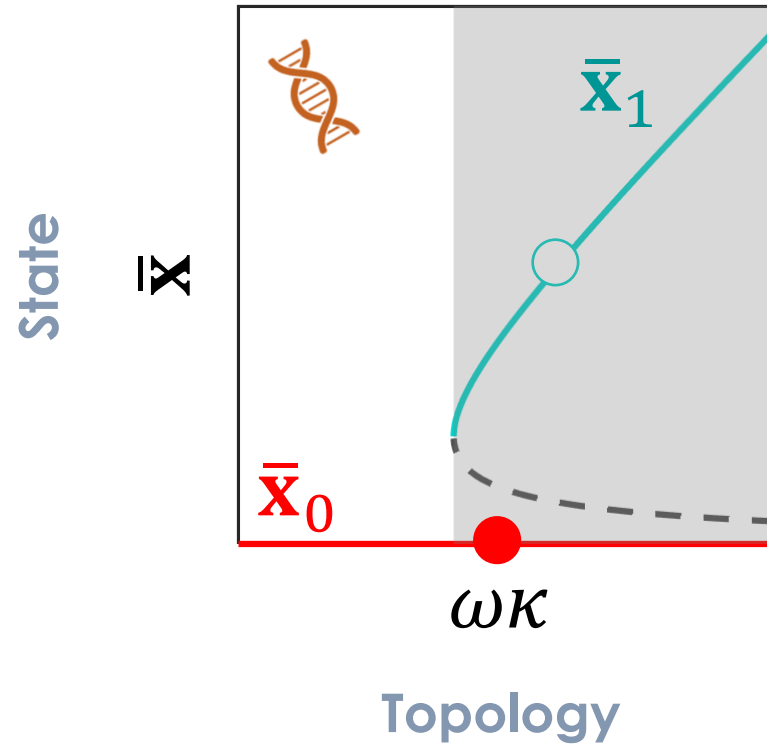
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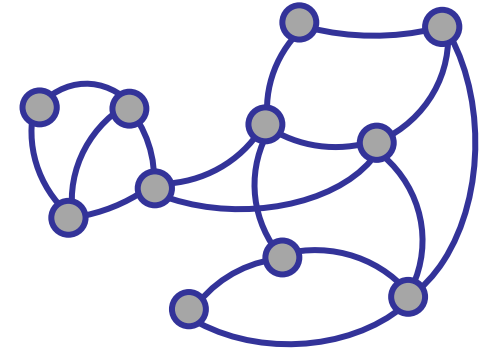
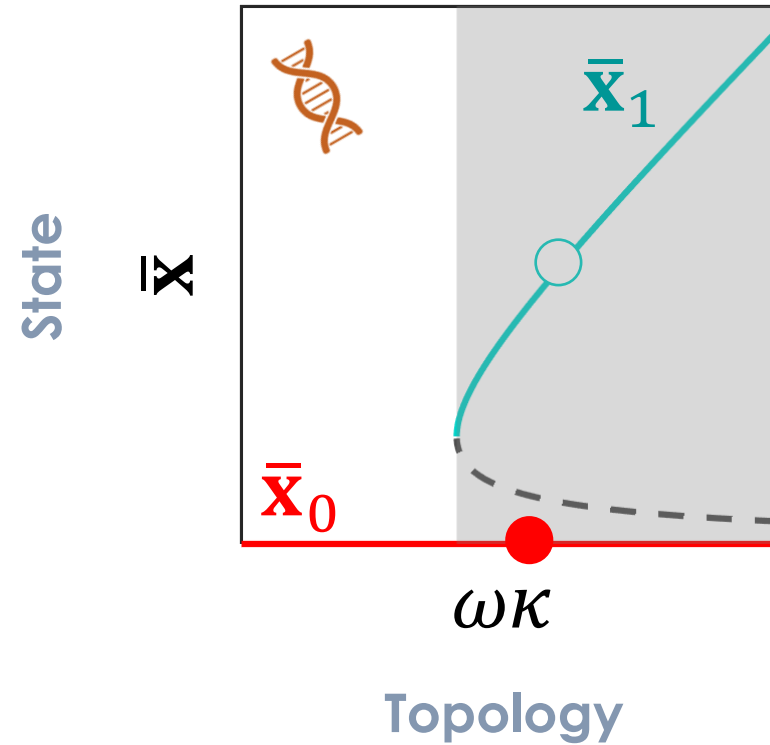
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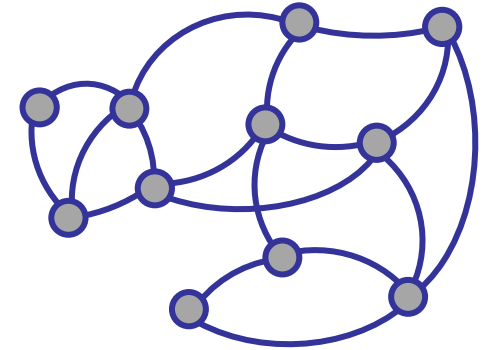
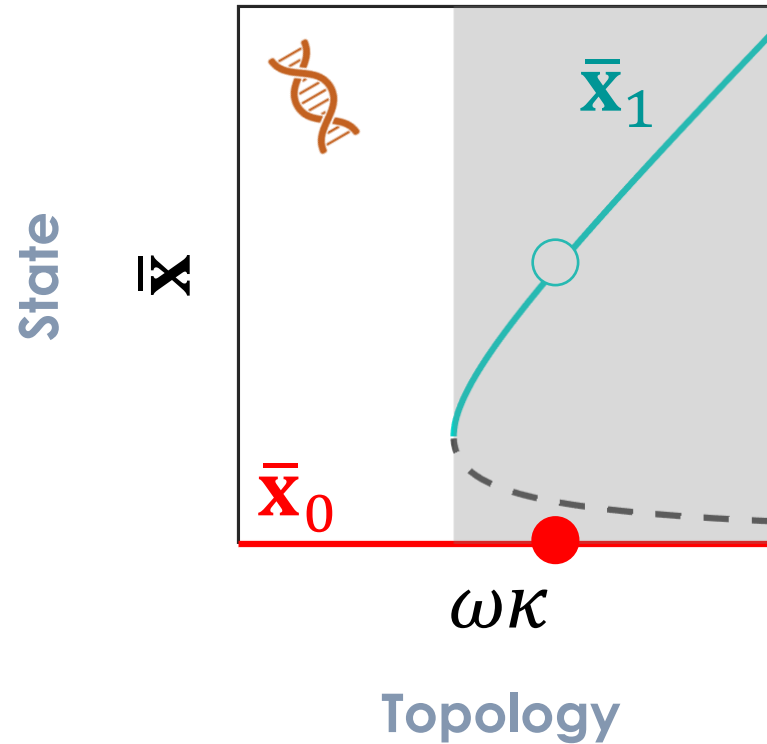
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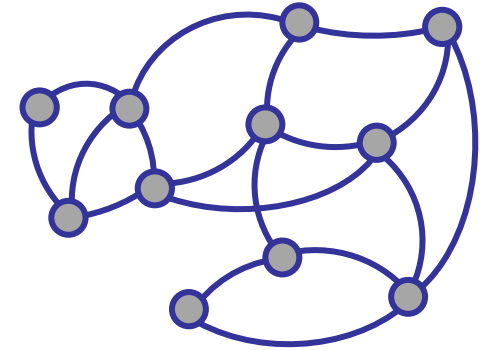
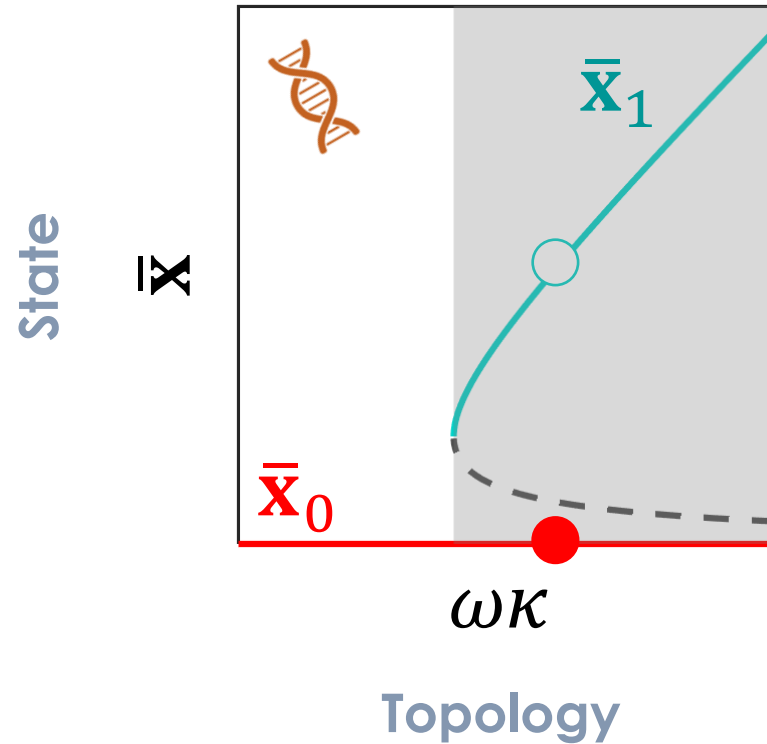


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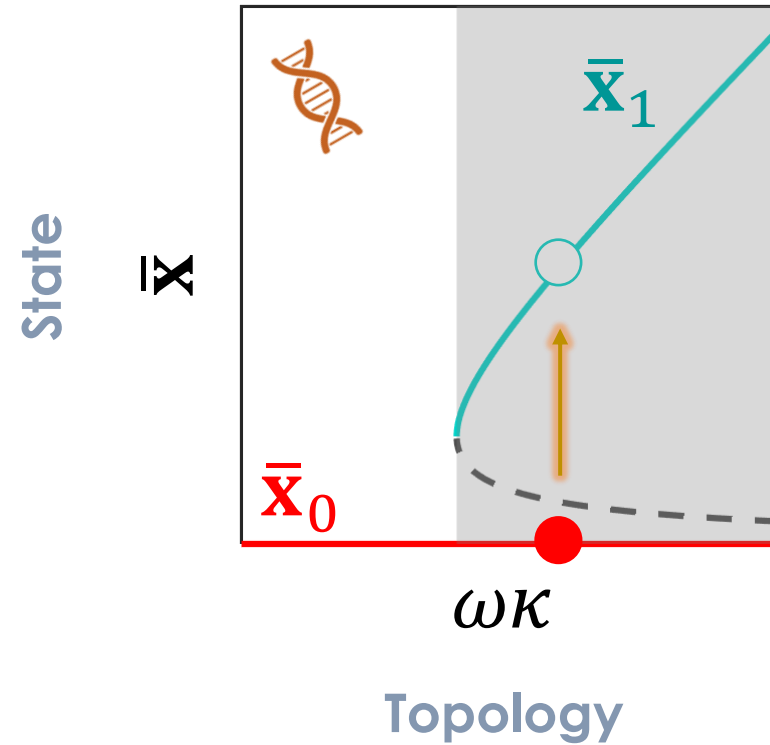


# Restructuring the network

How can we revive it?



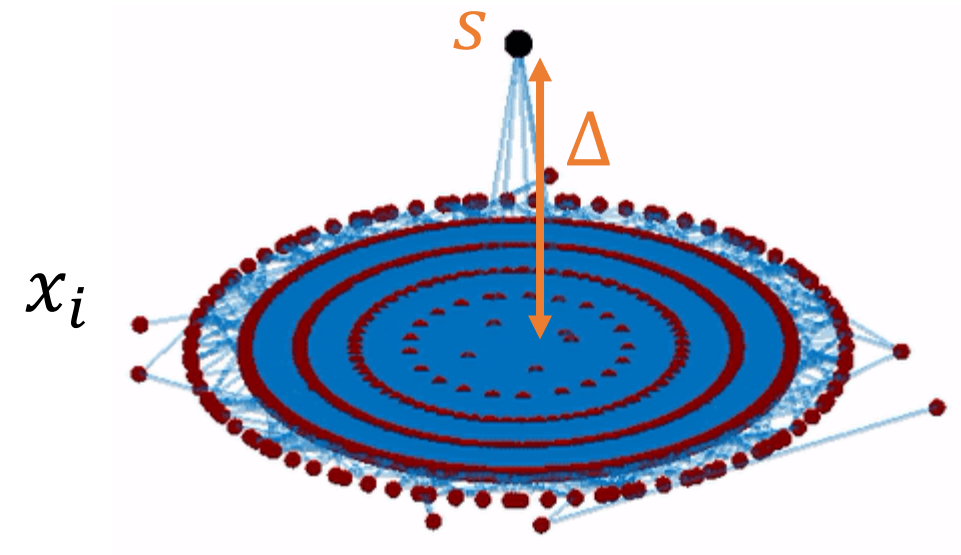
# Reigniting the dynamics



Can we **revive** the system by controlling just  
a **single** node?

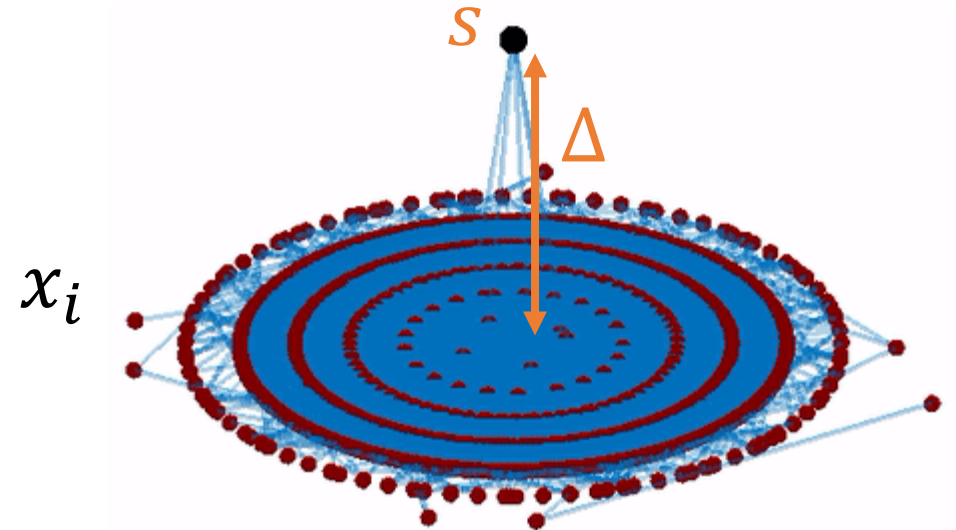


# Single-node reigniting

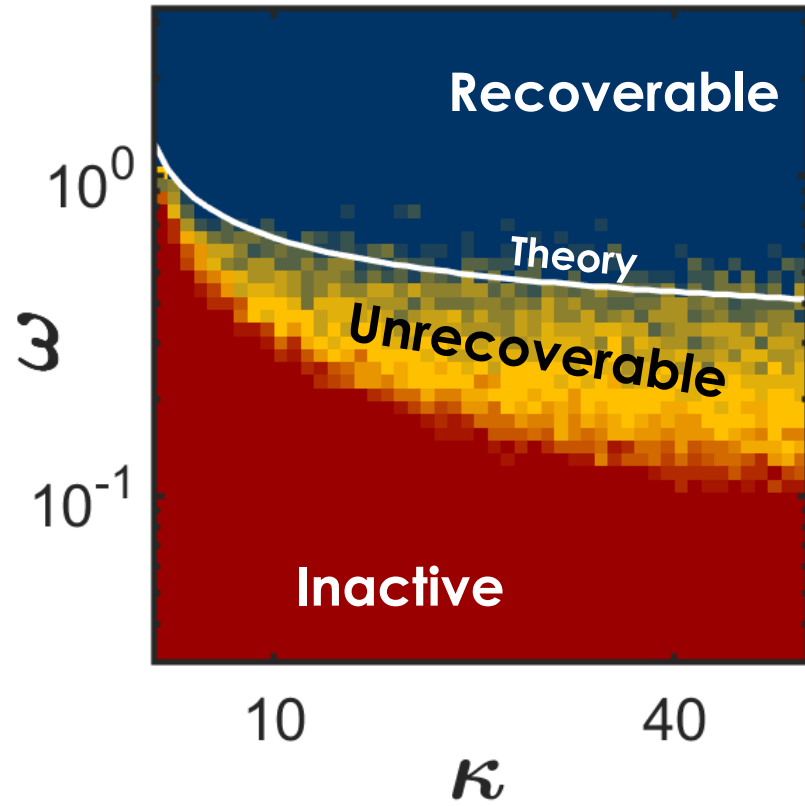


# Single-node reigniting

$$\begin{cases} x_s(t) = \Delta \\ \frac{dx_i}{dt} = -x_i + \sum_{j=1}^N A_{ij} \frac{x_j^2}{1 + x_j^2}, & i \neq s \end{cases}$$

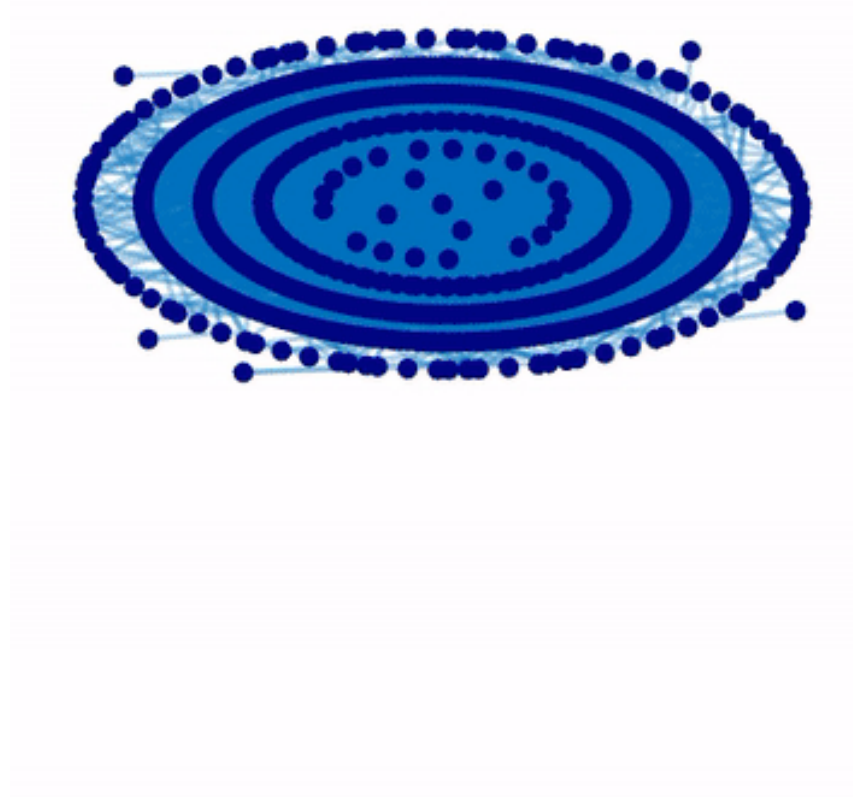
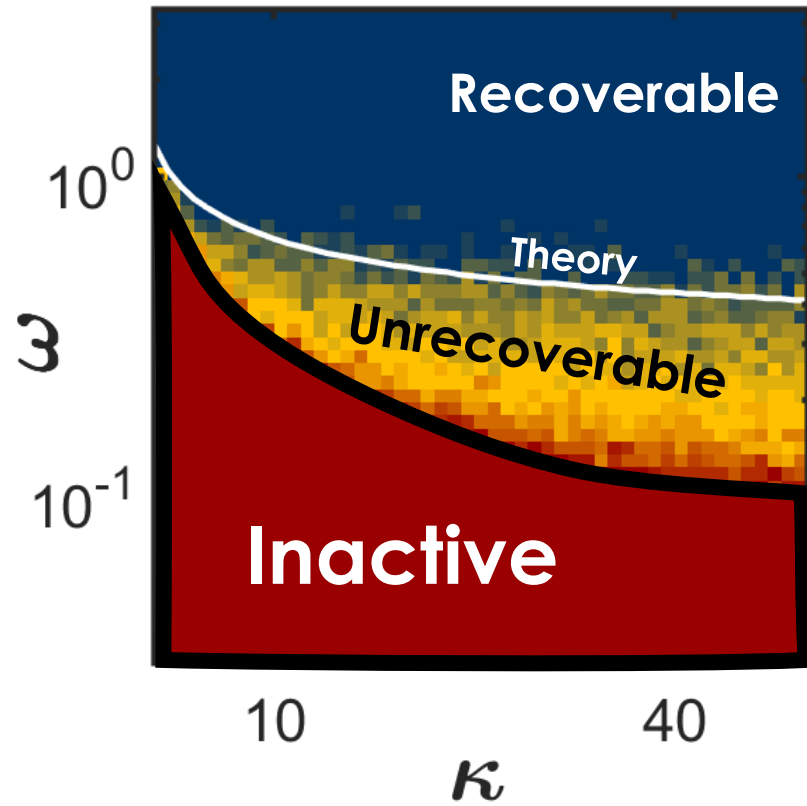


# Recoverability phase diagram

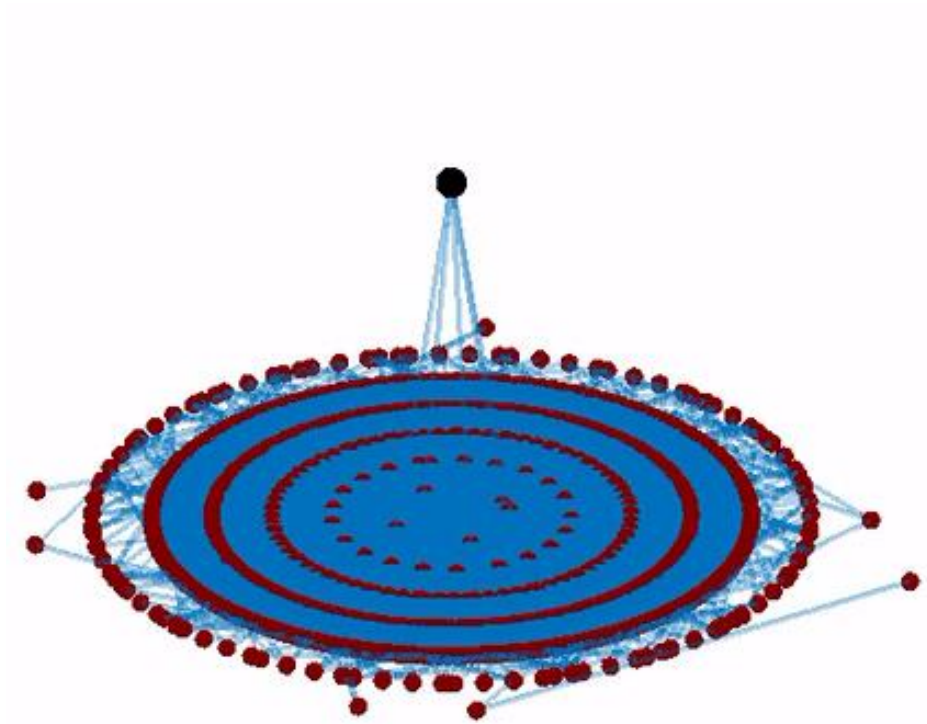
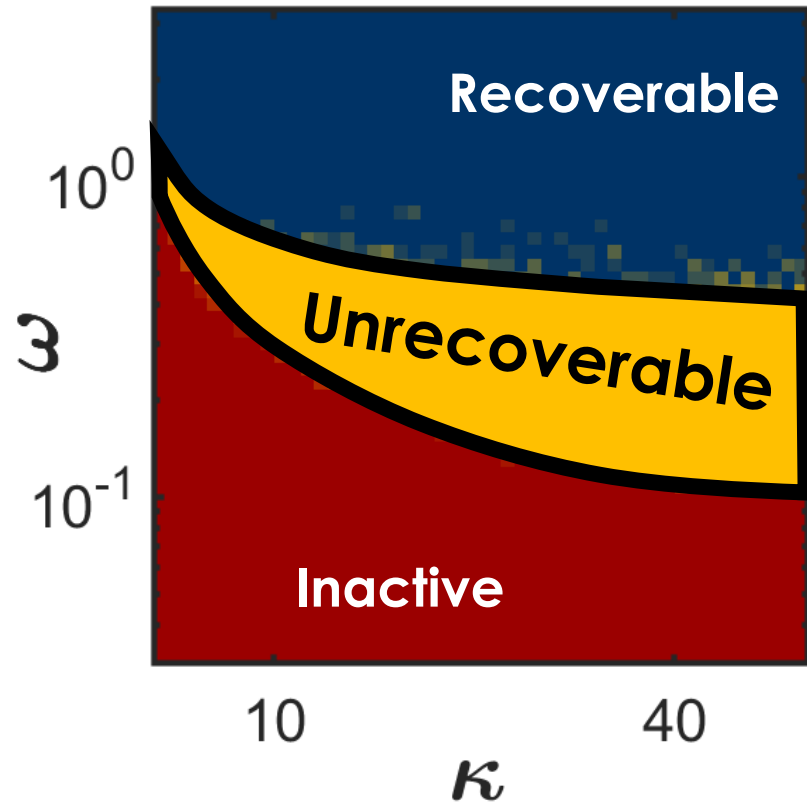


$$A_{ij} = \omega \quad \kappa = \langle k^2 \rangle / \langle k \rangle - 1$$

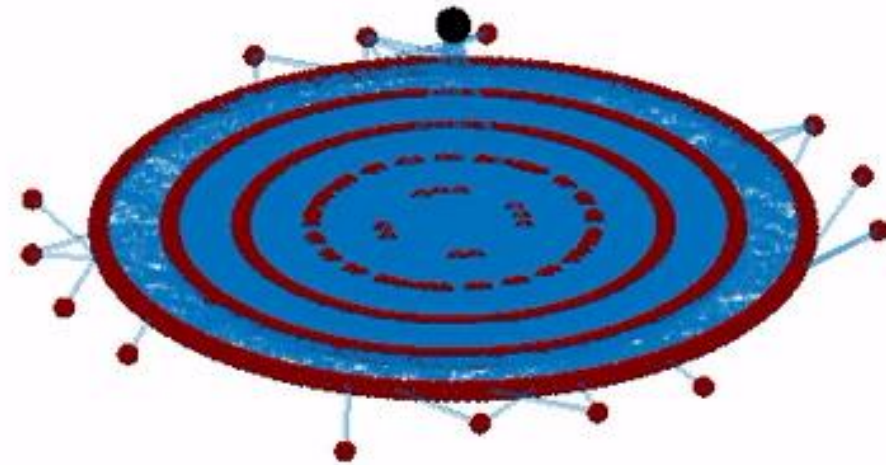
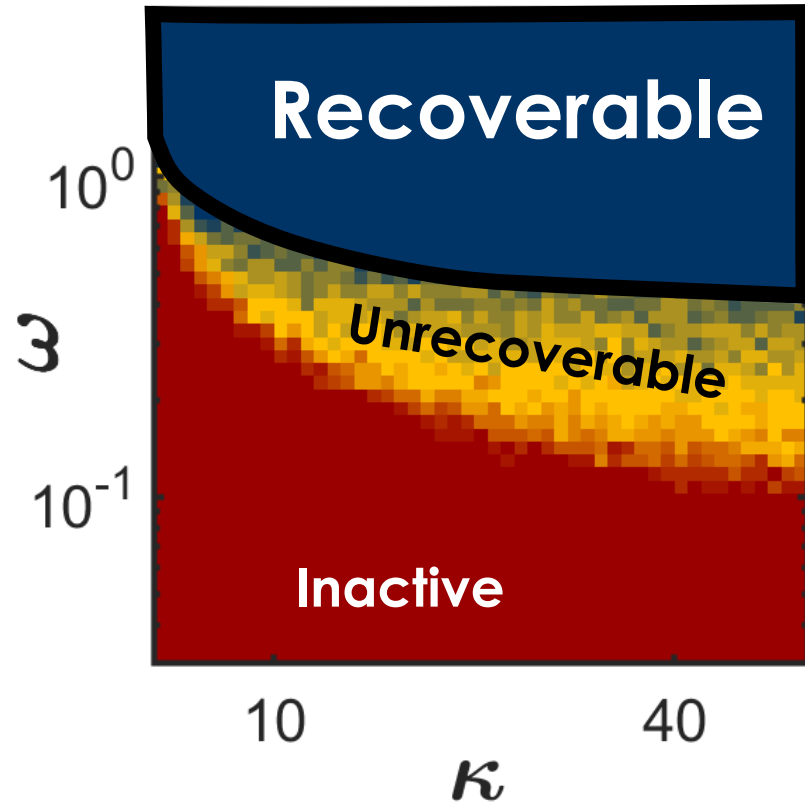
# Recoverability phase diagram



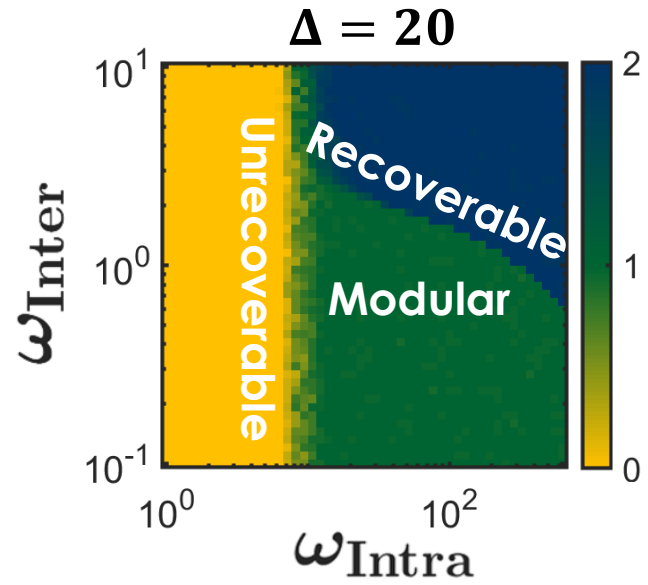
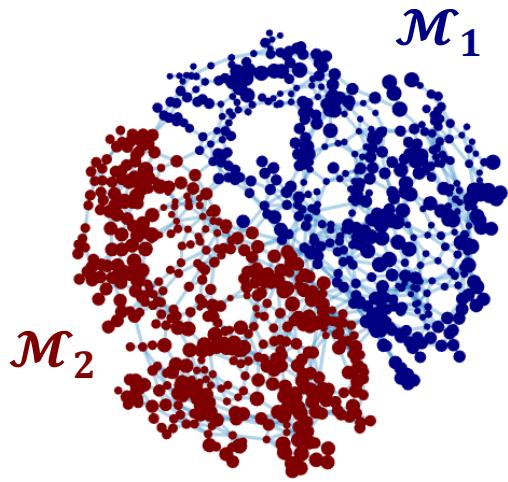
# Recoverability phase diagram



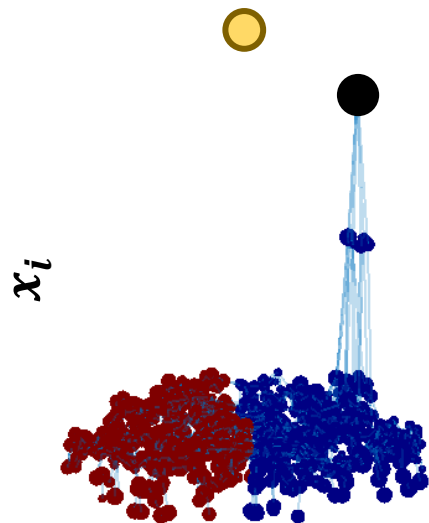
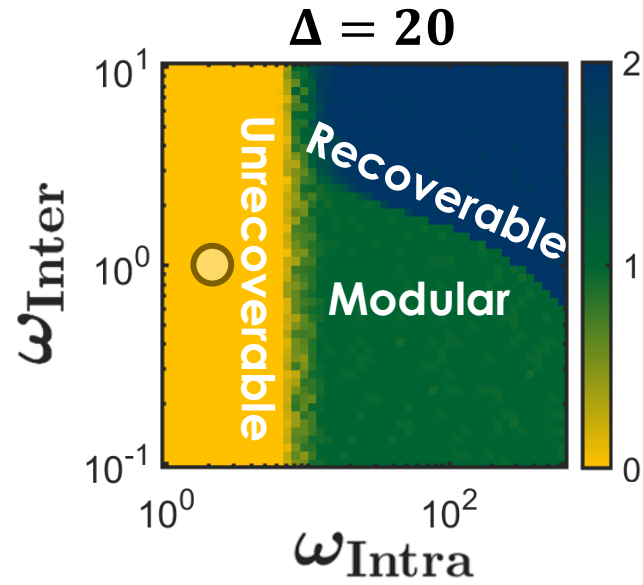
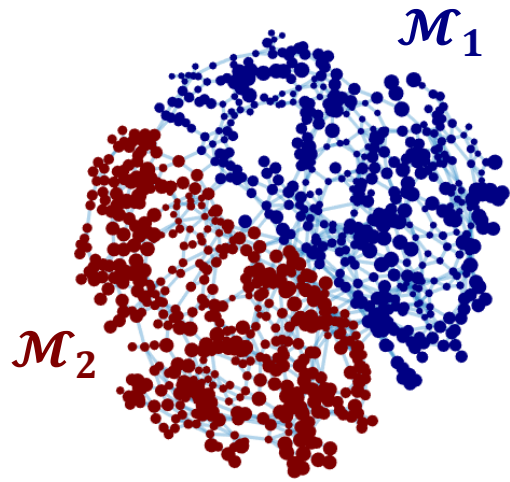
# Recoverability phase diagram



# Modular networks - Brain



# Modular networks - Brain







# Gut-microbiome

We suggest which species are good candidates to revive the whole gut-microbiome system through probiotics



# Reviving a failed network through microscopic interventions

Hillel Sanhedrai<sup>1</sup>, Jianxi Gao<sup>2,3</sup>, Amir Bashan<sup>1</sup>, Moshe Schwartz<sup>4</sup>, Shlomo Havlin<sup>1</sup> and Baruch Barzel<sup>5,6</sup>  

From mass extinction to cell death, complex networked systems often exhibit abrupt dynamic transitions between desirable and undesirable states. These transitions are often caused by topological perturbations (such as node or link removal, or decreasing link strengths). The problem is that reversing the topological damage, namely, retrieving lost nodes or links or reinforcing weakened interactions, does not guarantee spontaneous recovery to the desired functional state. Indeed, many of the relevant systems exhibit a hysteresis phenomenon, remaining in the dysfunctional state, despite reconstructing their damaged topology. To address this challenge, we develop a two-step recovery scheme: first, topological reconstruction to the point where the system can be revived and then dynamic interventions to reignite the system's lost functionality. By applying this method to a

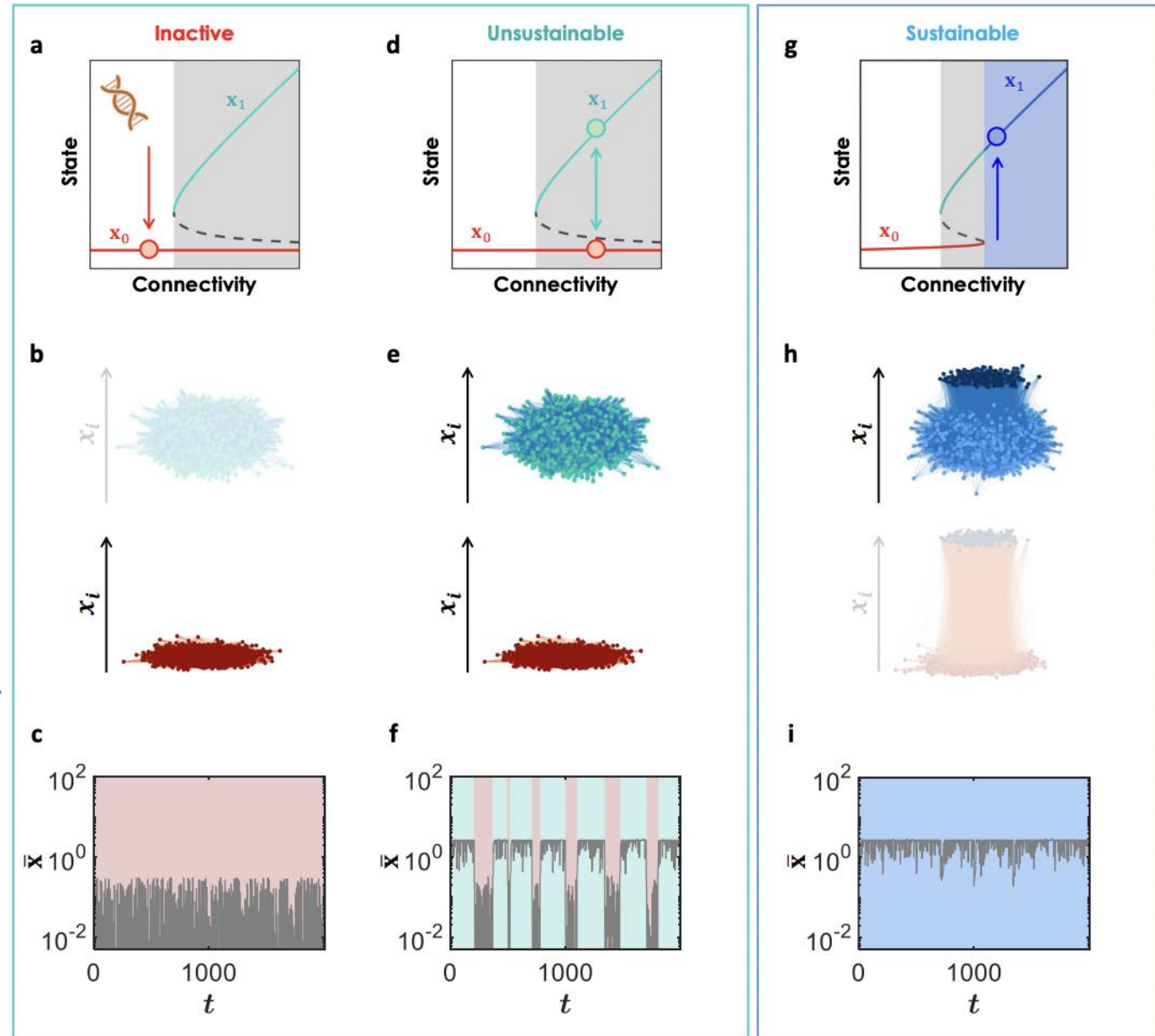
# **Sustaining a network by controlling a fraction of nodes**

Sanhedrai et al arXiv:2205.13377 (2022)

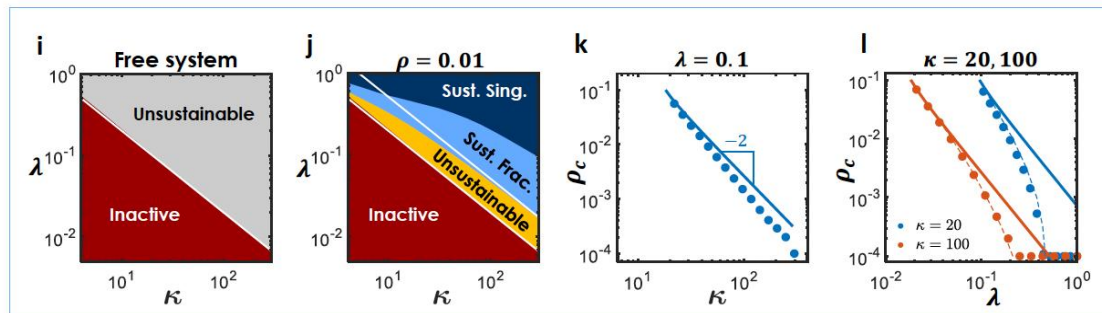
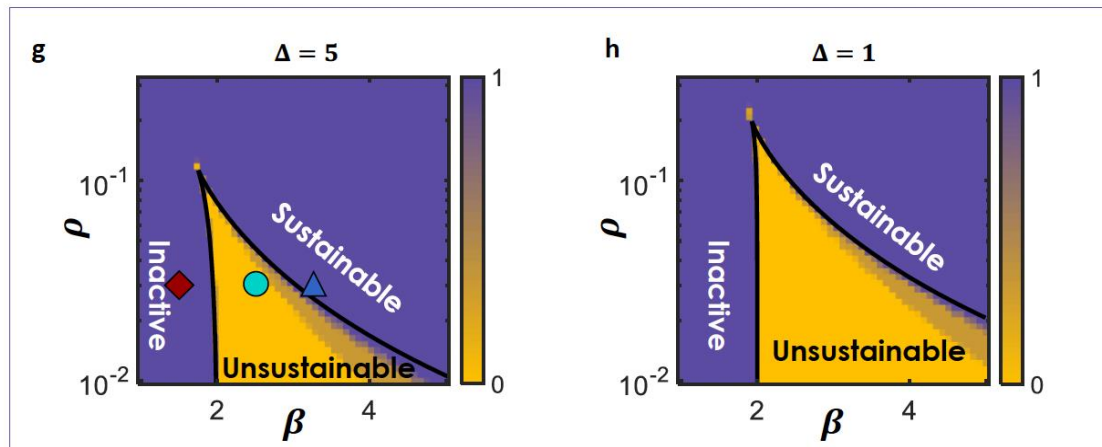
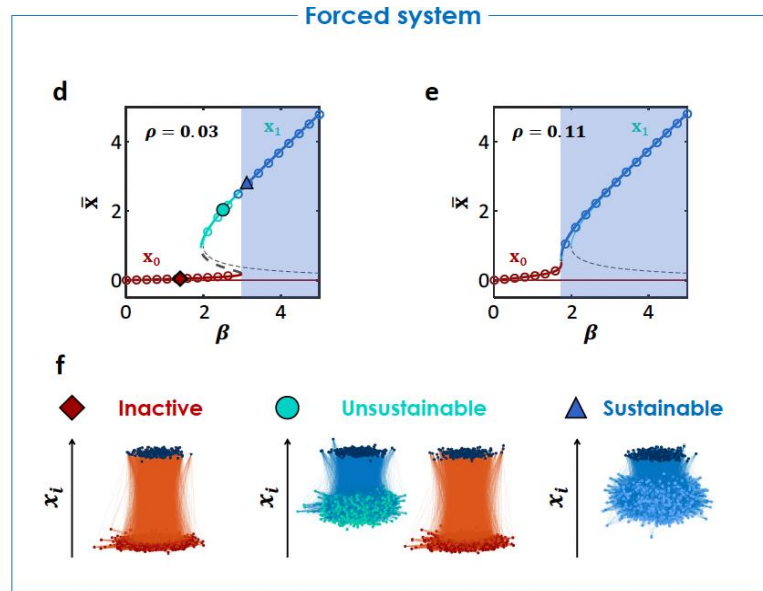
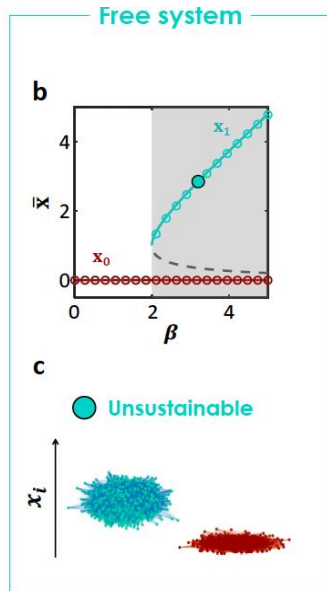
# Sustaining Dynamics on Networks

$$\frac{dx_i}{dt} = M_0(x_i) + \lambda \sum_{j=1}^N A_{ij} M_1(x_i) M_2(x_j)$$

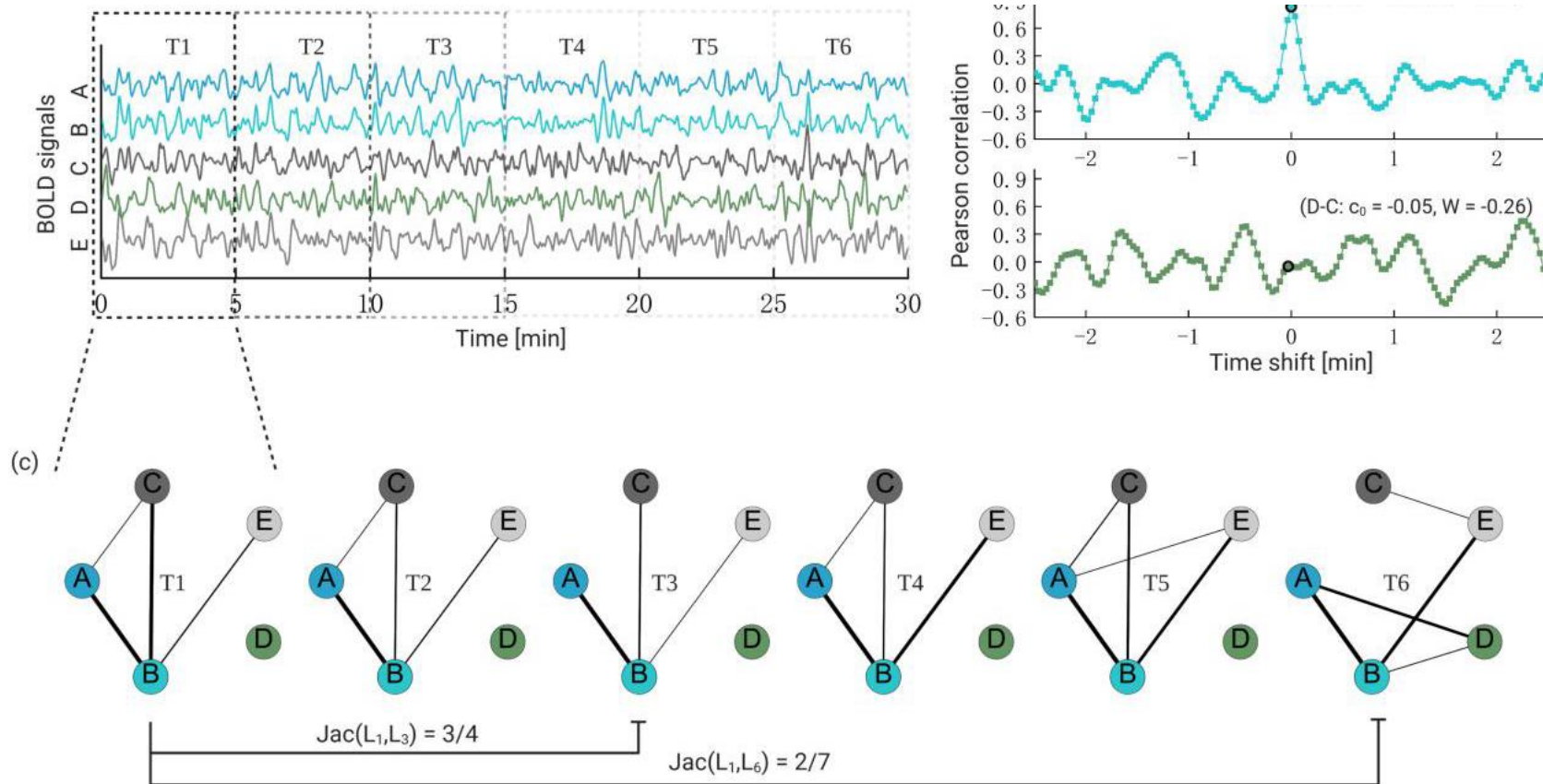
$$\begin{cases} x_i = \Delta & i \in \mathcal{F} \\ \frac{dx_i}{dt} = M_0(x_i) + \lambda \sum_{j=1}^N A_{ij} M_1(x_i) M_2(x_j) & i \in \mathcal{D} \end{cases}$$



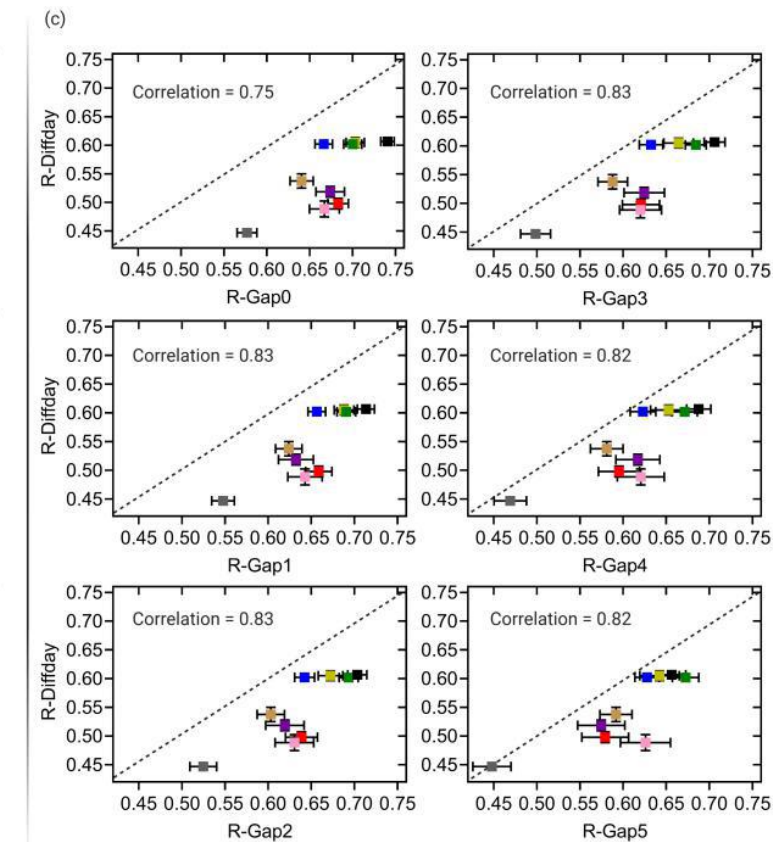
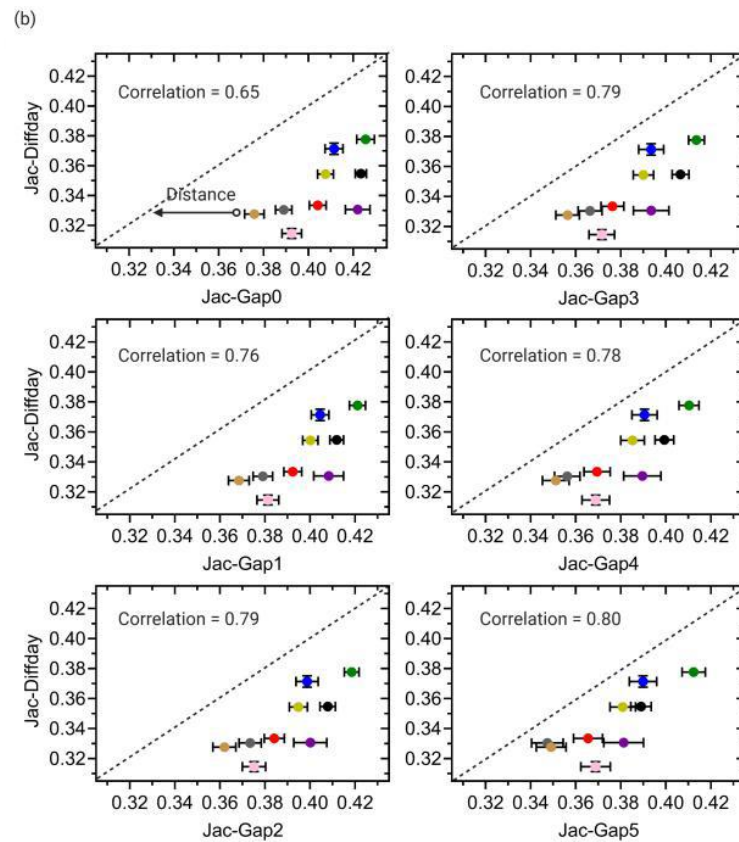
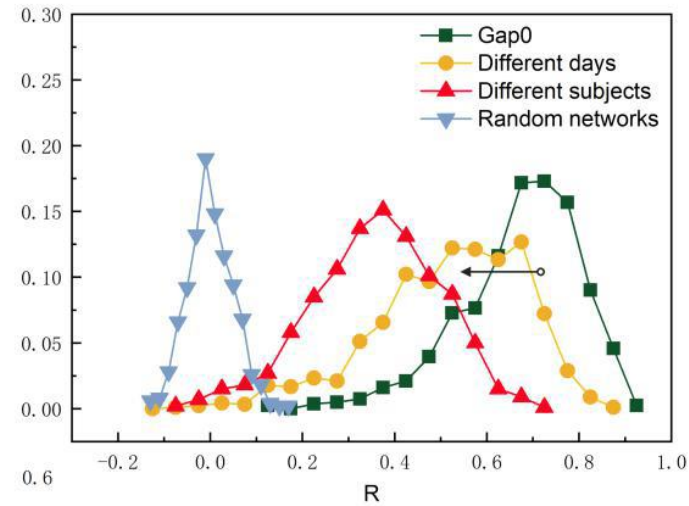
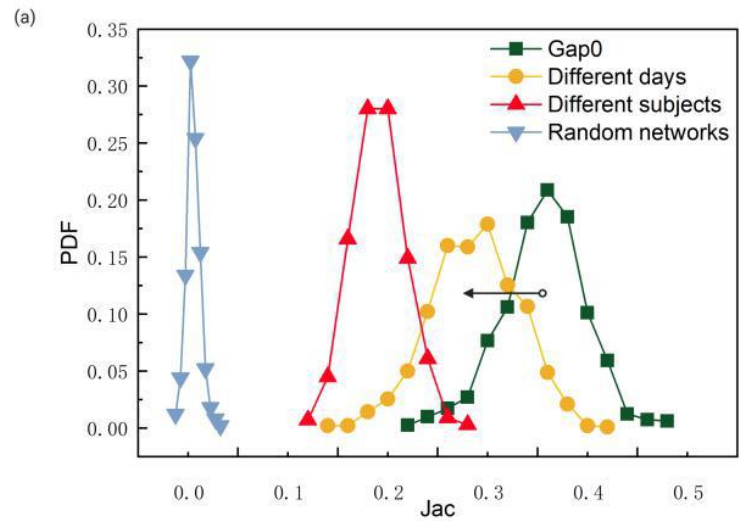
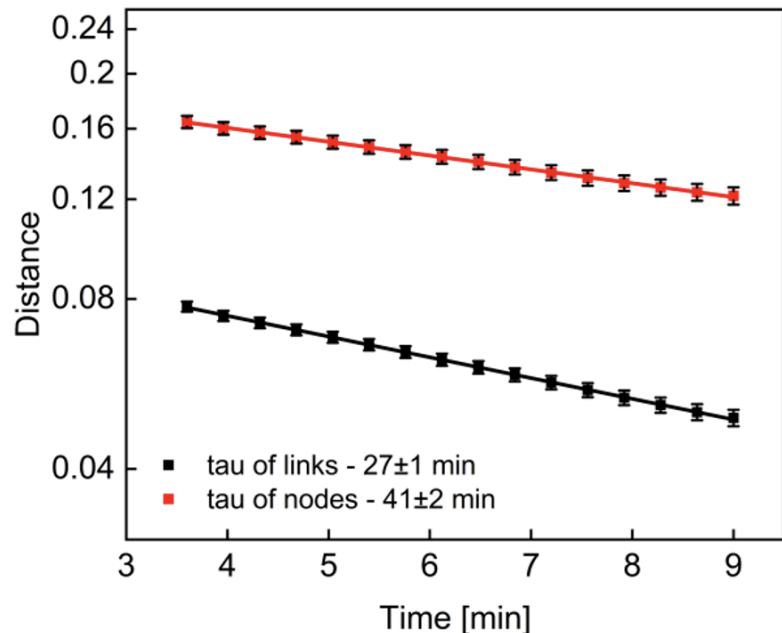
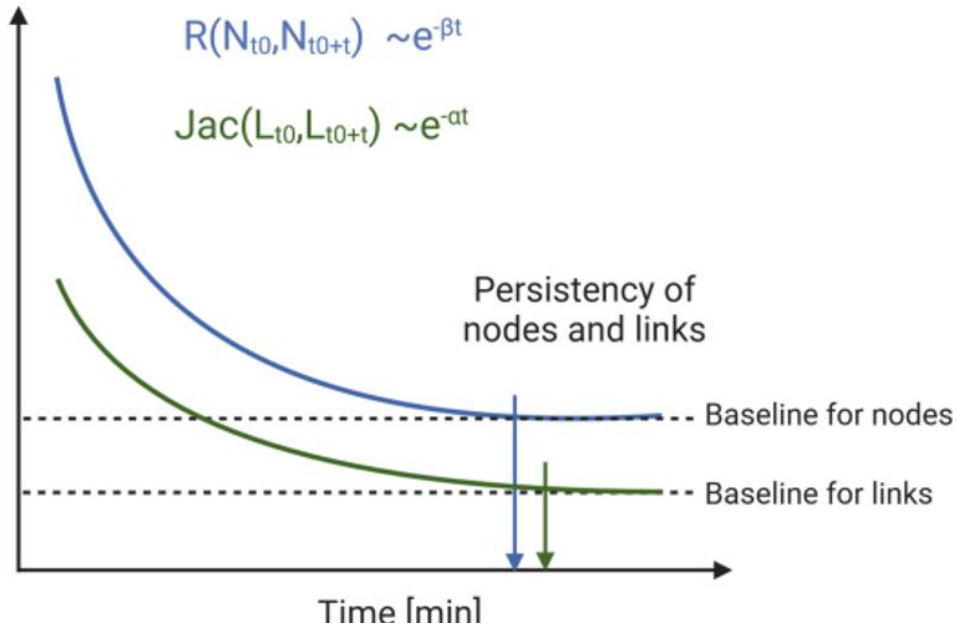
Cellular  $\frac{dx_i}{dt} = -Bx_i^a + \lambda \sum_{j=1}^N A_{ij} \frac{x_j^h}{1+x_j^h}$



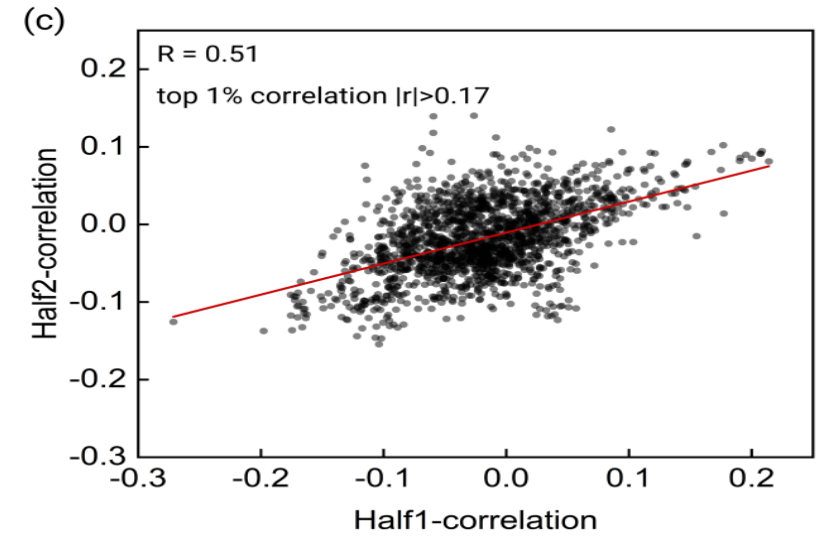
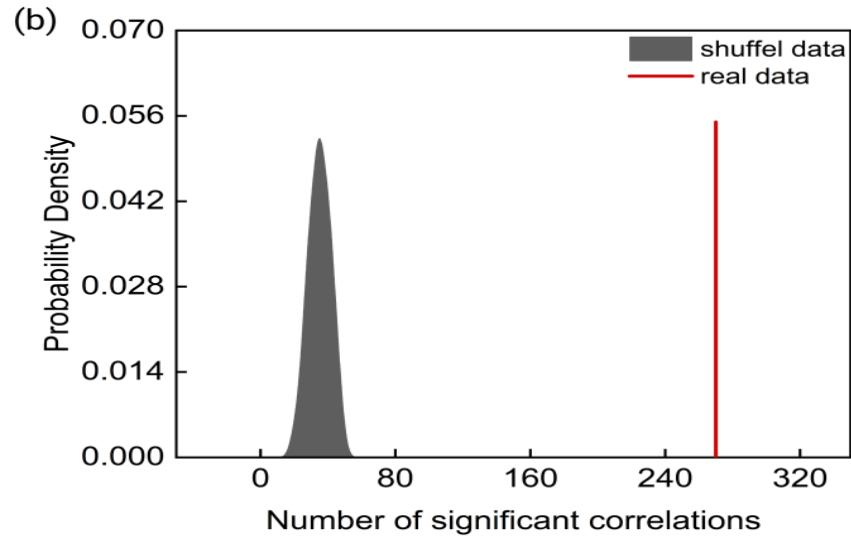
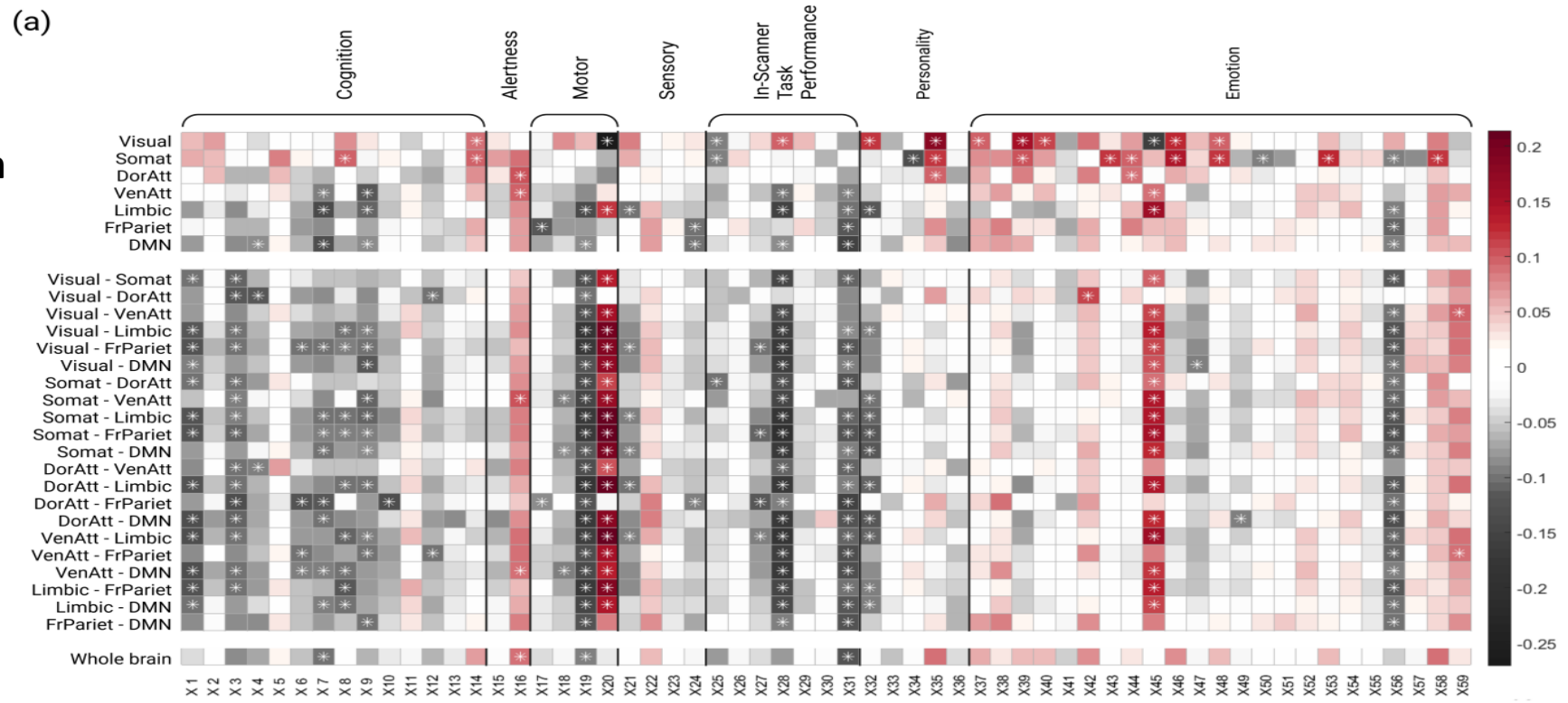
# Evolving Brain Networks (Shu et al, preprint 2022)



Network Similarity



# Network persistency of different brain regions in REST is associated with performance



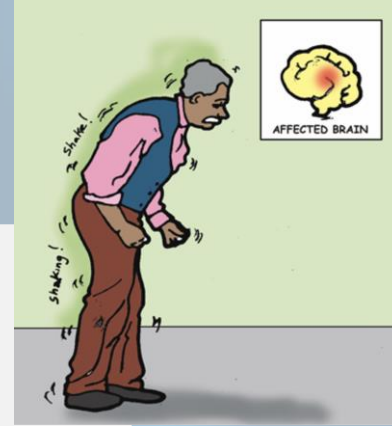


Connectivity of EEG  
synchronization networks  
increases with severity of  
Parkinson's disease and  
freezing of gait

E. Asher, R. Bartcsh et al  
Comm. Physics 4, 1017  
(2021)



Data consists of EEG  
recordings of 4 groups,  
according to disease  
severity.



1. *Elderly Control*
2. *PD – FoG*
3. *PD + FoG<sup>-</sup>*
4. *PD + FoG<sup>+</sup>*



# Summary:

## Network applications in physiology and biology

[1] [Reviving a failed network through microscopic interventions](#)

Sanhedrai, J Gao, A Bashan, M Schwartz, S Havlin, B Barzel

Nature Physics 18 (3), 338-349 (2022)

[2] [Sustaining a network by controlling a fraction of nodes](#). H Sanhedrai, S Havlin

arXiv preprint arXiv:2205.13377 (2022)

[3] [Connectivity of EEG synchronization networks increases for Parkinson's disease patients with freezing of gait](#)

E. Asher, R. Bartcsch, S. Havlin et al

Communications Biology 4 (1), 1-10 (2021)—By **Ronny Bartsch this afternoon**

[4] Brain dynamic network during rest and personal performance

Shu Guo et al, In preparation, 2022