

Estimating resilience of evolving epileptic brain networks

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Epilepsy

Greek term for *seizure*; disease first mentioned ~ 1750 BC

~ 50 Mio people suffer from epilepsy (~ 0.8 % of world population)*

seizure: short-lasting dysfunction of central nervous system

epilepsy: recurrent ($> 2/a$) seizures without acute cause

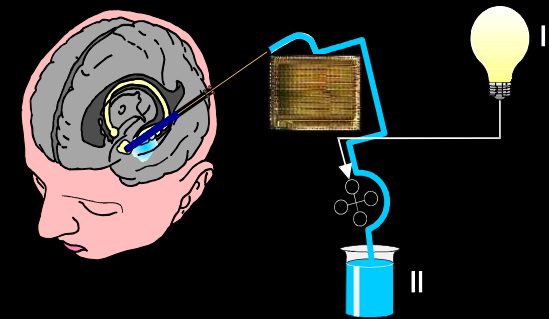
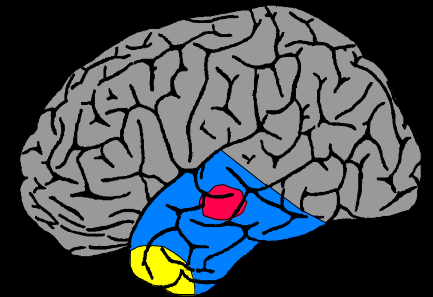
famous people suffering from epilepsy:

Sokrates, Alexander the Great, Julius Caesar, Lenin,
Flaubert, Dostojevski, Carroll, Poe, Berlioz, Paganini,
Händel, van Gogh, Newton, Pascal, Helmholtz, Nobel

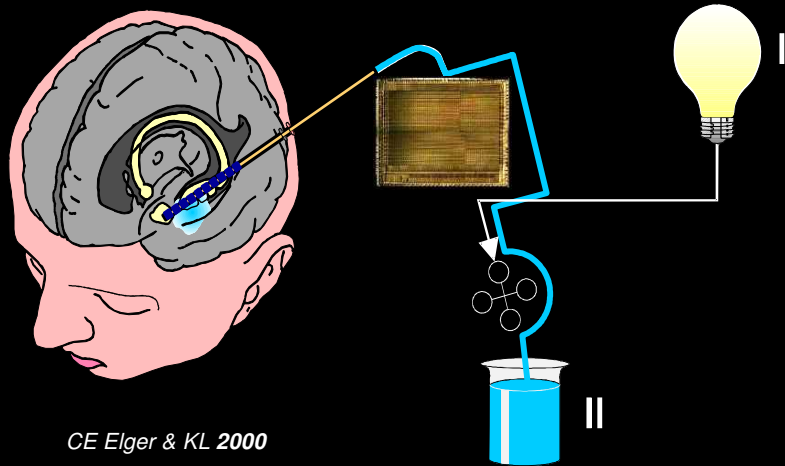
* WHO fact sheet, Feb 2017

Treatment of Epilepsy

- **antiepileptic drugs**; primary therapy
success: ~ 70 %
side effects, long-term treatment
- **epilepsy surgery**; option for ~ 5 – 10 % of patients
requirement: localize and delineate epileptic focus
from functionally relevant brain areas
success: ~ 60 % (15 % – 85 %)
long-term outcome, surgery-induced alterations?
- **alternative therapies**; for ~ 22 % of patients
seizure prediction, seizure control
success: ?



New Treatment Options through Seizure Prediction



CE Elger & KL 2000

on demand:

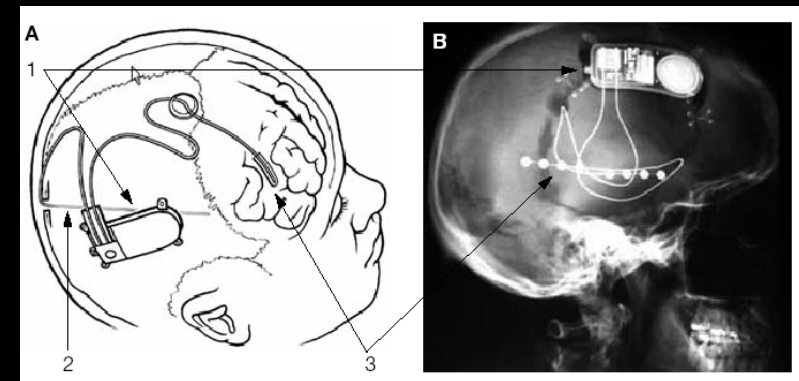
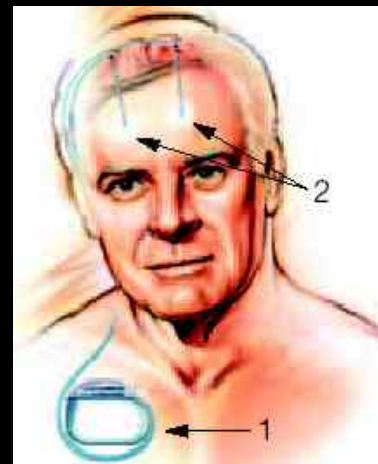
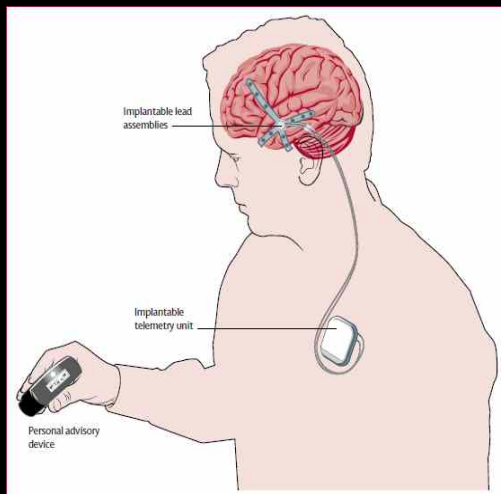
warning / self-control

local drug administration

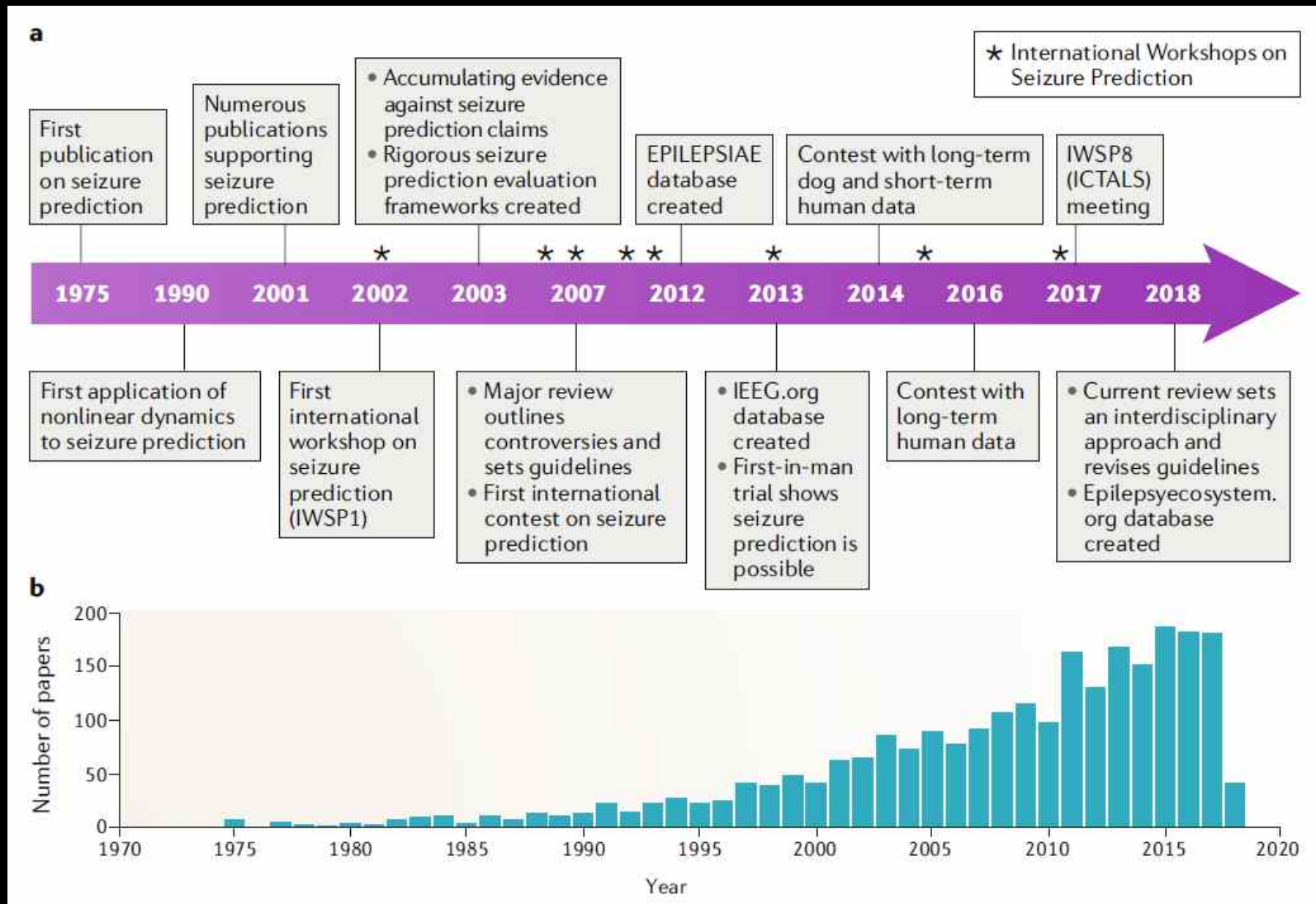
local cooling

stimulation

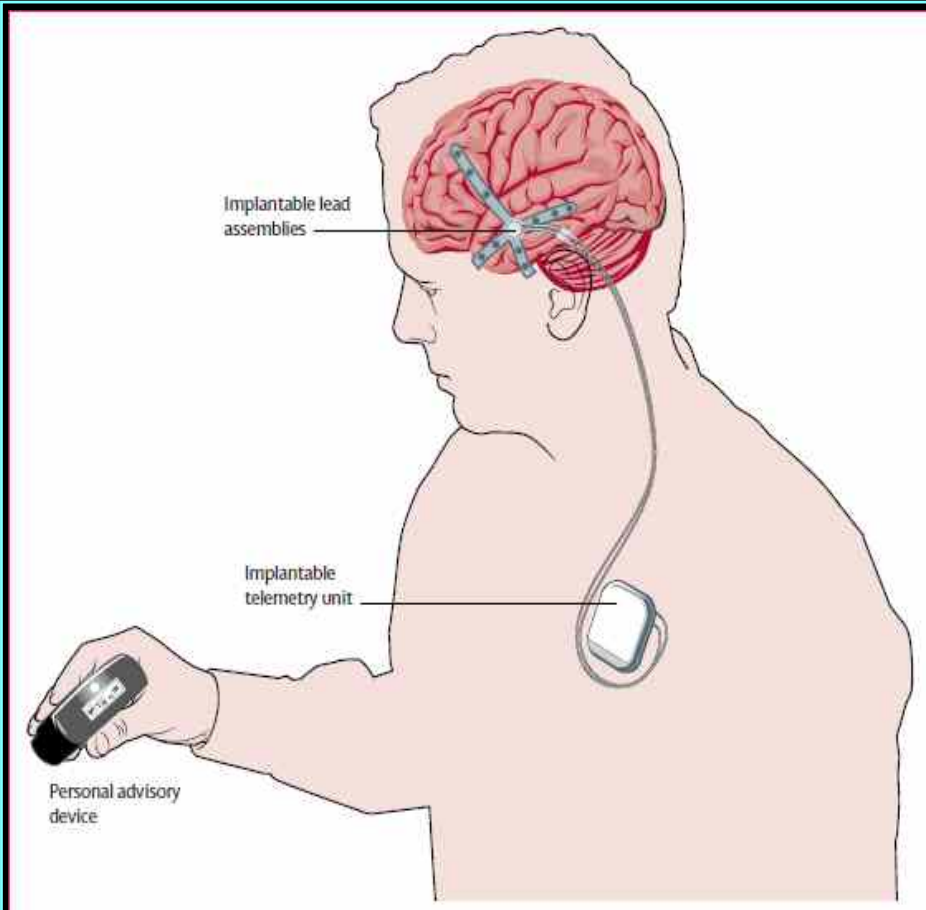
...



Evolution of Seizure Prediction



Implantable Seizure Prediction System



- 15 patients
- Australian feasibility study
- NeuroVista Corp. (USA)
“Seizure Advisory System”
- up to 3 yrs of continuous recording (16 channels @ 400 Hz)

prediction is feasible, but ...
... not in all patients
... not in all seizures

Cook et al., Lancet Neurol 2013; 12: 563

reasons ?

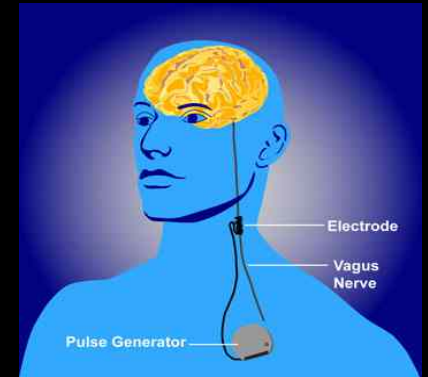


Neuromodulation in Epilepsy

not better than drugs

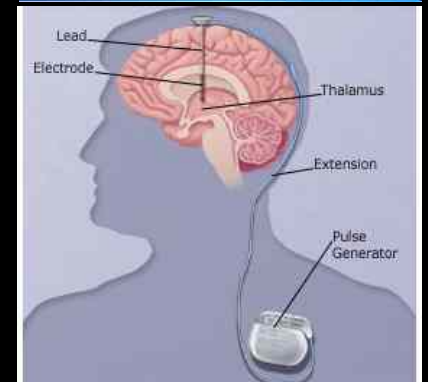
Vagal Nerve Stimulation (VNS)

unspecific activation of N. vagus
seizure reduction ~35 % (1. yr) – ~ 43% (3. yr)



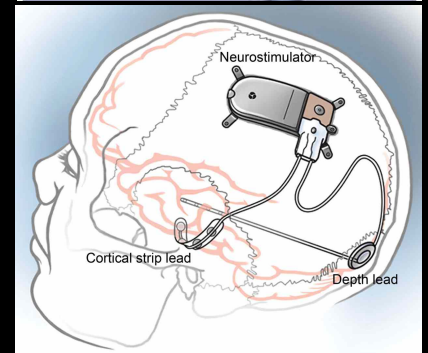
Deep Brain Stimulation (DBS)

targeted stimulation of thalamic nuclei
seizure reduction ~ 41 % (1. yr) – ~ 56% (2. yr)



Responsive Neurostimulation (RNS)

targeted elect. stimulation of epileptic focus at seizure onset
seizure reduction: ~ 44 % (1. yr) – 48-66 % (3-6 yr)



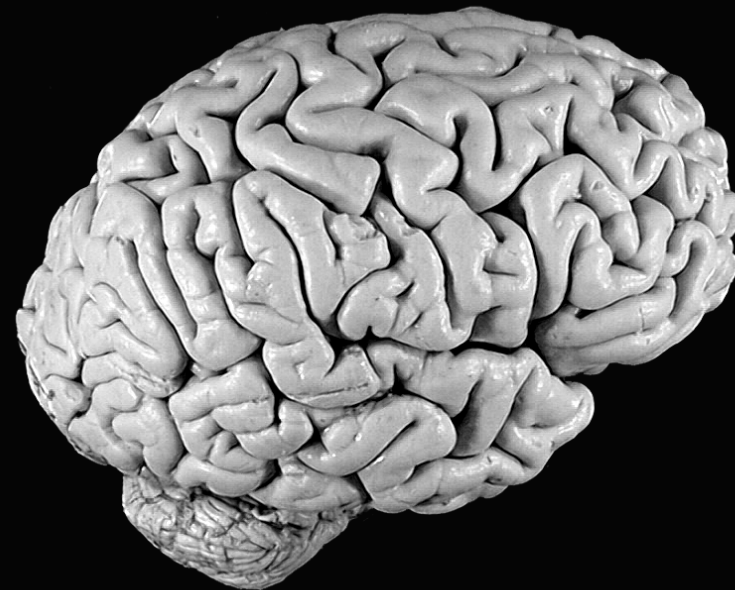
side effects, long-term success ?



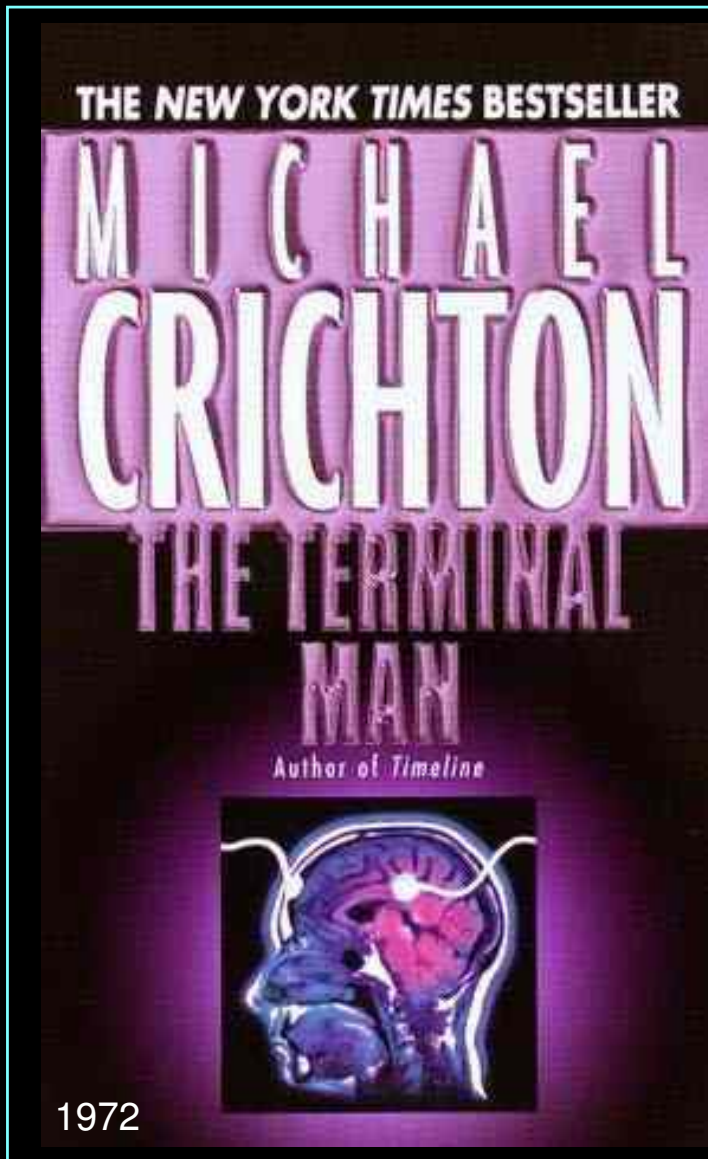
Seizure Prediction and Prevention

nonlinear, open, dissipative

adaptive
plasticity



can the epileptic brain be controlled?
(or: does it want to be controlled?)



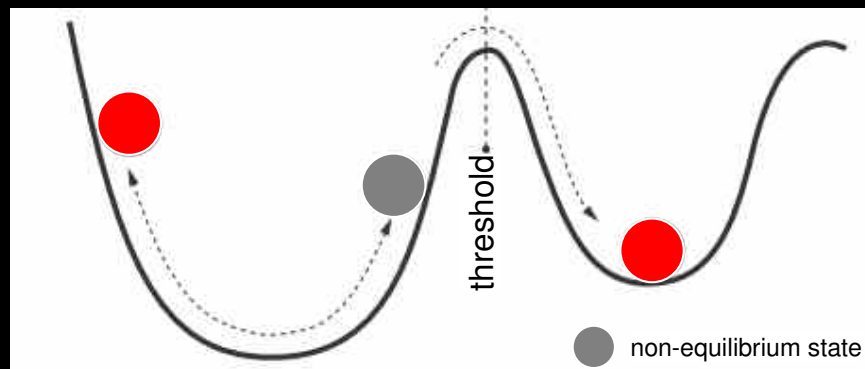
Resilience and Dynamical Systems

“the capacity of a system to absorb disturbance and reorganize while undergoing change so as to still retain essentially the same function, structure, identity, and feedbacks”

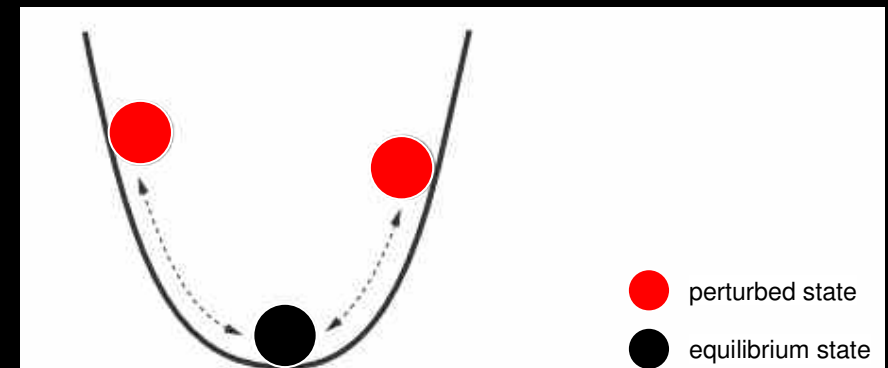


Crawford S. Holling: *Resilience and stability of ecological systems.*
In: *Annual Review of Ecology and Systematics* (1973)

ecological resilience (Holling)



engineering resilience (Pimm)



Resilience in Different Domains

engineering resilience

Pimm (1984)

system's speed of **return to equilibrium** following a **shock**

ecological resilience

Holling (1973, 1996)

ability of system to **withstand shock** and **maintain** critical relationships and functions

social-ecological resilience

Carpenter et al. (2001)

(i) amount of **disturbance** a system can **absorb and remain** within a domain of attraction;
(ii) capacity for learning and adaptation, (iii) degree to which system can self-organize

social resilience

Adger (2000)

ability of groups or communities to **cope with external stresses and disturbances** as a result of social, political and environmental **change**

development resilience

Pasteur (2011); Barrett & Constan (2014)

capacity of a person, household or other aggregate unit **to avoid poverty** in the face of various **stressors** and in the wake of myriad **shocks over time**

socio-economic resilience

Mancini et al. (2012)

refers to the policy-induced ability of an economy to **recover from or adjust to** the negative impacts of adverse exogenous **shocks** and to benefit from positive **shocks**

community resilience

Norris et al. (2008)

process linking a set of adaptive capacities to a positive trajectory of **functioning** and **adaptation** after a **disturbance**

psychological resilience

Tugade, Fredrickson &
Feldman Barrett (2004)

an individual's ability to **adapt to stress and adversity**; resilience is a process and can be learned by anyone using positive emotions

e.g. Quinlan et al., J Appl Ecol 2016



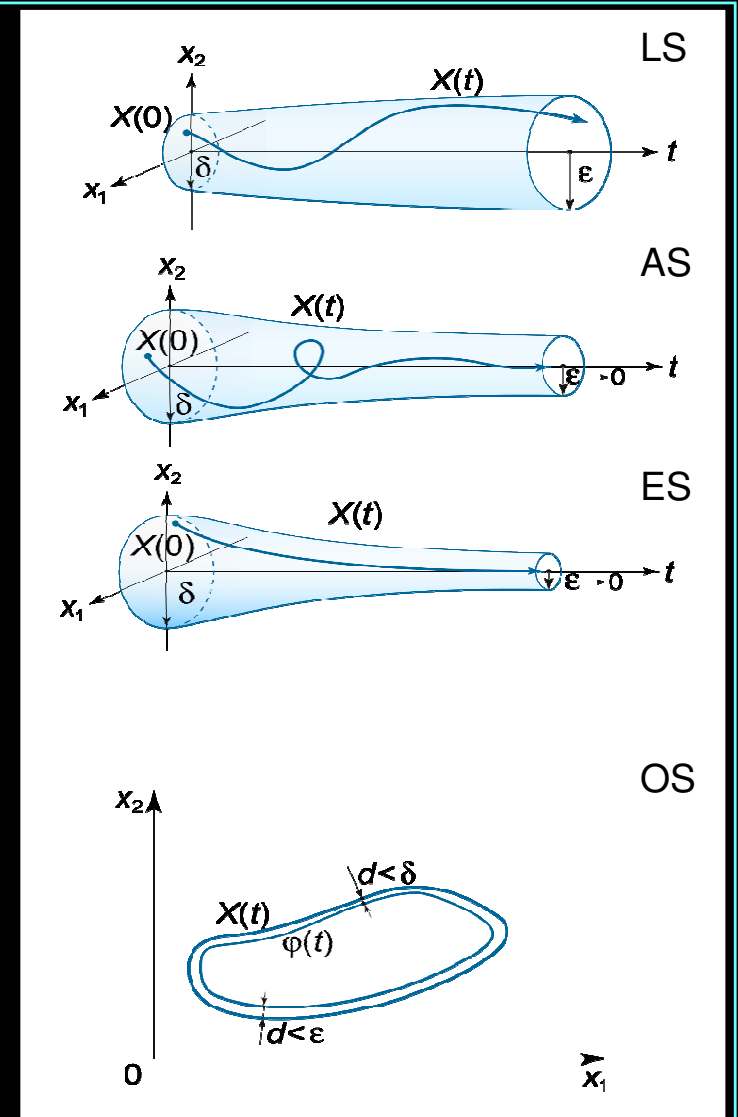
Stability of Dynamical System (I)

- differential (or difference) equations describing dynamical system
- infinitesimal (**small**) perturbations

stability of system near equilibria
 Lyapunov stability (LS)
 asymptotic stability (AS)
 exponential stability (ES)

stability of trajectory
 orbital stability (OS)

stability of system itself
 structural stability



adopted from: math24.net

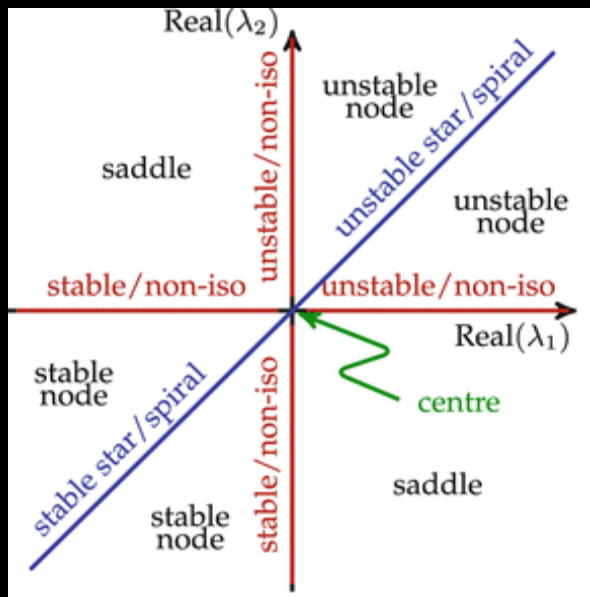
Stability of Dynamical System (II)

Methods and Extensions

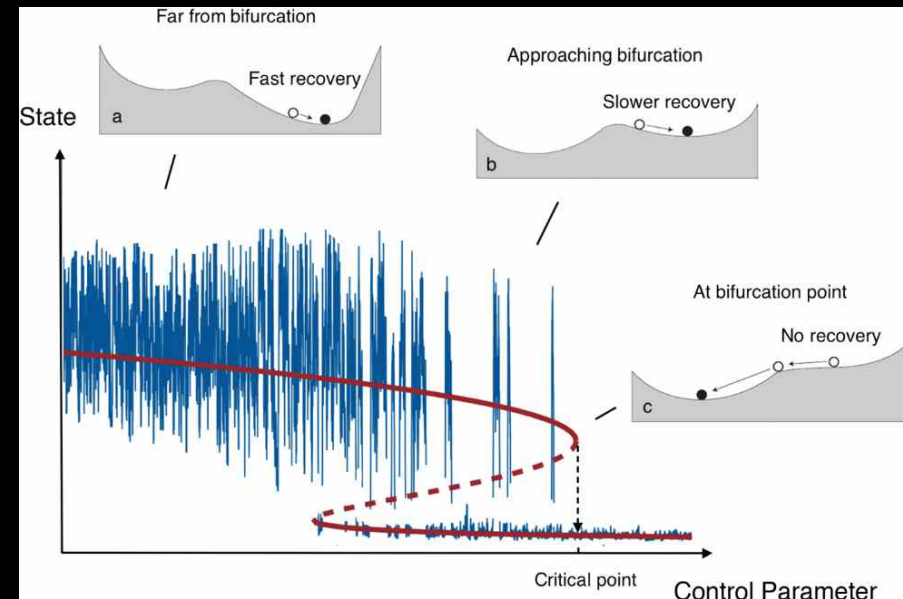
small perturbations

- linear stability analysis
- evaluate eigenvalues of Jacobian at equilibrium

- tipping (bifurcation) points
- critical slowing down (not universal)
- relevance for epilepsy unclear



from: P. Fieguth: An Introduction to Complex Systems, 2017



from: C. Diks et al., Emp Econ., 2018

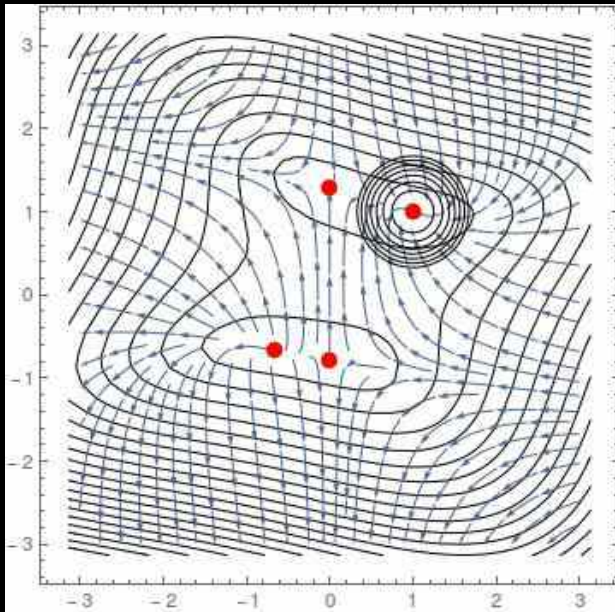
Stability of Dynamical System (III)

Methods and Extensions

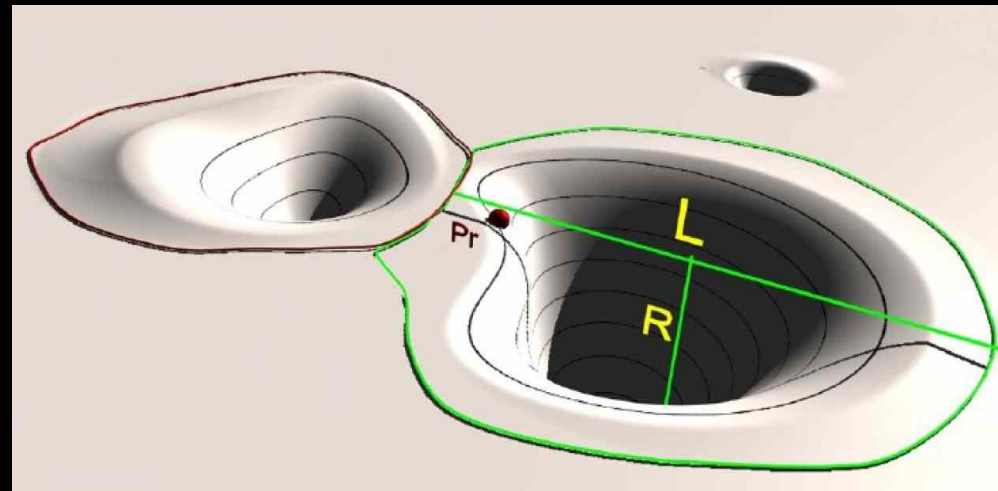
large, non-local perturbations, multistable systems

- Lyapunov stability criterion
- Lyapunov functions
- LaSalle invariance principle

- basin of attraction
- volume
- prob. to return to attractor, return time
- latitude, resistance, precariousness



from: math.stackexchange.com



from: Leuteritz & Ekbia, 2008

e.g. Walker et al., 2004, Menck et al. 2014

Stability of Dynamical System (IV)

most methods require exact knowledge of equations of motion

perturbations:

small vs. large

local vs. non-local

control parameter vs. state variables

data-driven methods rare; strong claims



Network Resilience

complex system → complex network

- robustness against attacks (micro → macro), mostly endogenous*
- multi-dimensional system → effective one-dimensional dynamics: **resilience patterns & functions**, impact of topology, (ongoing research)

$$\dot{x}_i = F(x_i) + \sum_{j=1}^N A_{ij} G(x_i, x_j)$$

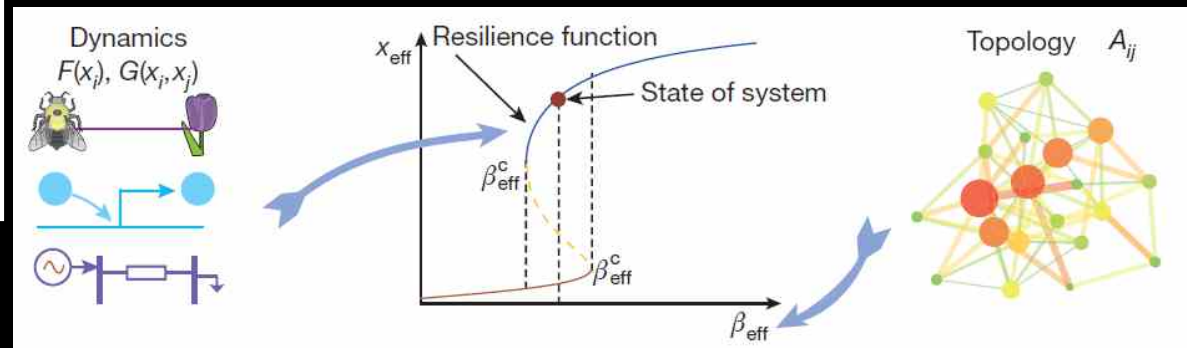
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$$\dot{x}_{\text{eff}} = F(x_{\text{eff}}) + \beta_{\text{eff}} G(x_{\text{eff}}, x_{\text{eff}})$$

where $x_{\text{eff}} = \frac{\sum_{ij} A_{ij} x_j}{\sum_{ij} A_{ij}}$

and $\beta_{\text{eff}} = \frac{\sum_{ij} A_{ij} A_{ji}}{\sum_{ij} A_{ij}}$

perturbations affect network structure only



from: Gao et al., Nature 530, 307, 2016

*e.g., S. Havlin, R Cohen: Complex Networks: Structure, Robustness and Function, 2010

Data-driven Estimation of Resilience

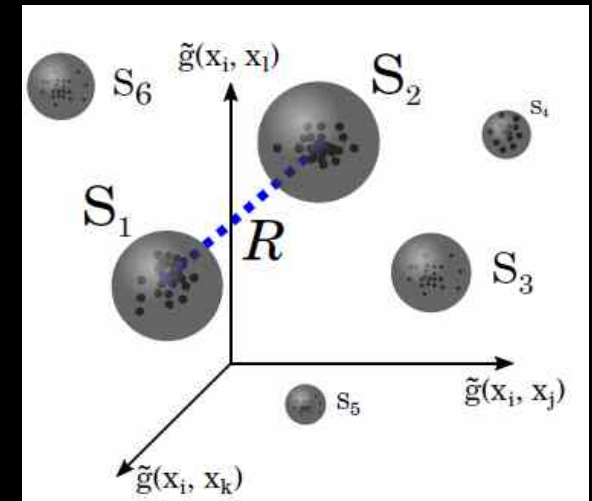
system representation: $\dot{x}_i = F(x_i) + \sum_{j=1}^N A_{ij}g(x_i, x_j; t)$

ansatz:

- estimate time-resolved coupling structure $\tilde{g}(t)$ (e.g., via pairwise estimations of strength of interaction)
- recurring coupling structures* indicate dynamical regimes

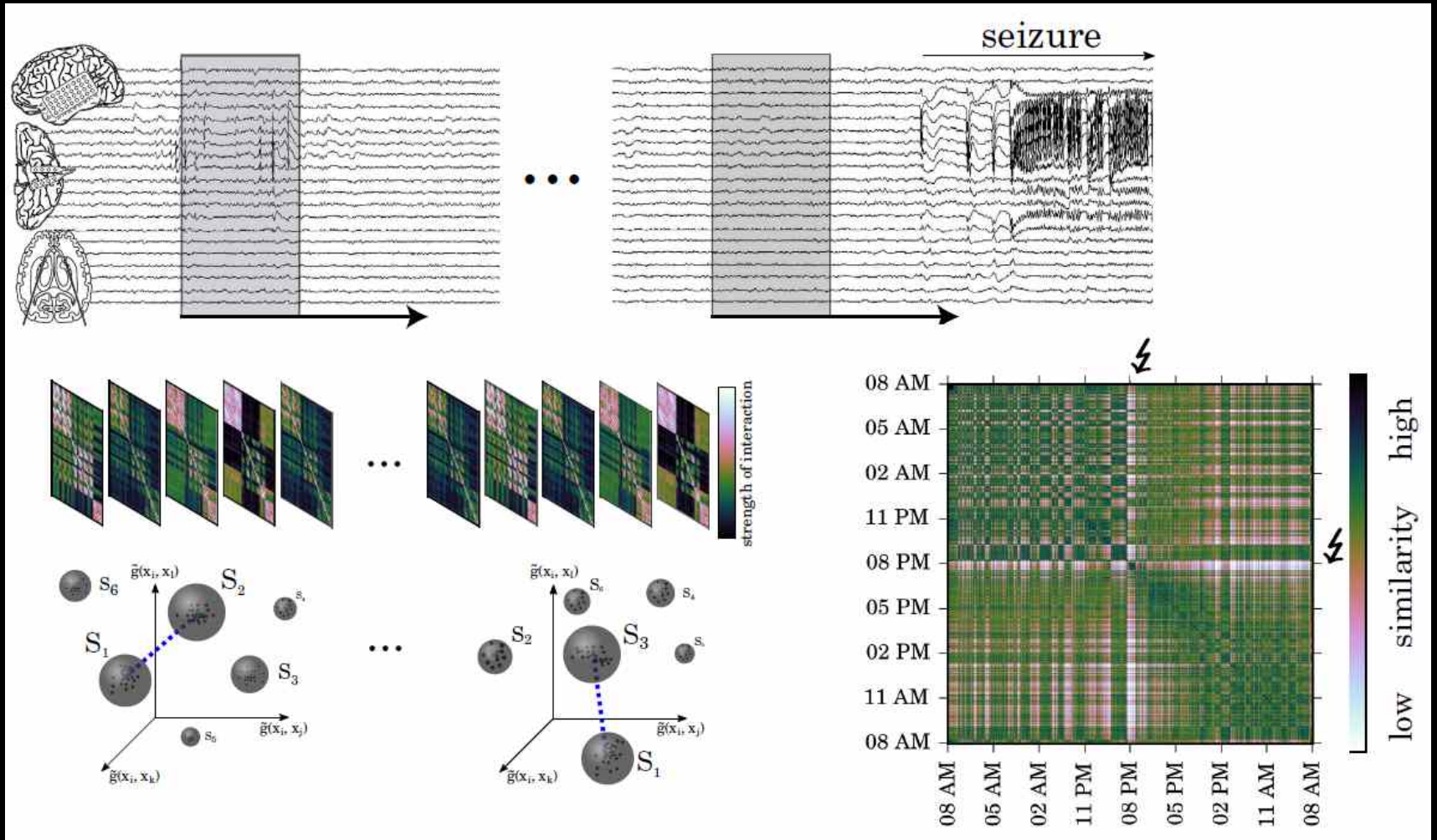
$$\xi(t_1, t_2) = \|\tilde{g}(t_1) - \tilde{g}(t_2)\|_2$$

- identify dynamical regimes with hierarchical clustering
- minimum distance R between dynamical regimes as proxy for resilience



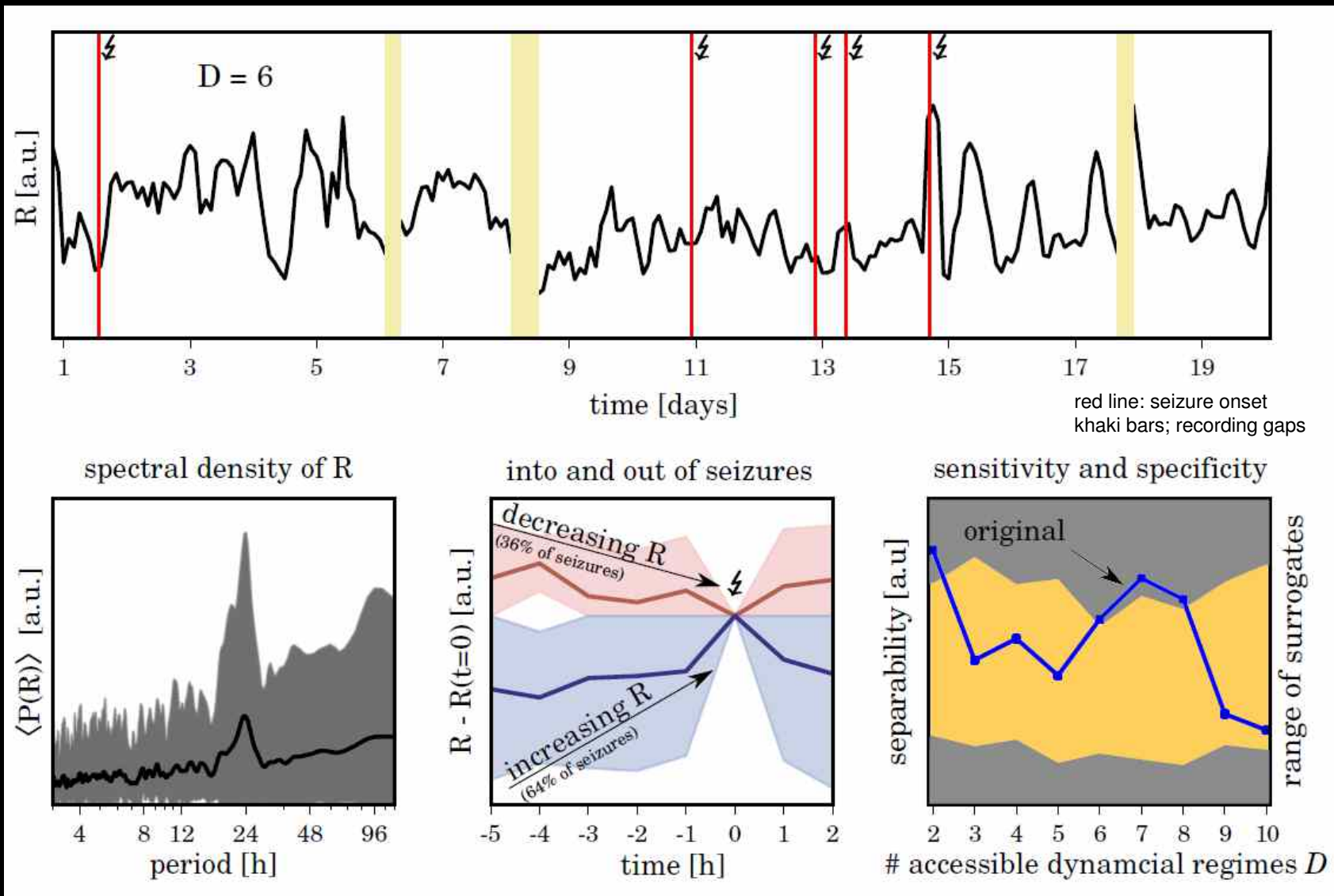
Data-driven Estimation of Brain Resilience

43 subjects, 109 seizures, drug-resistant epilepsies, 4000 h iEEG recording



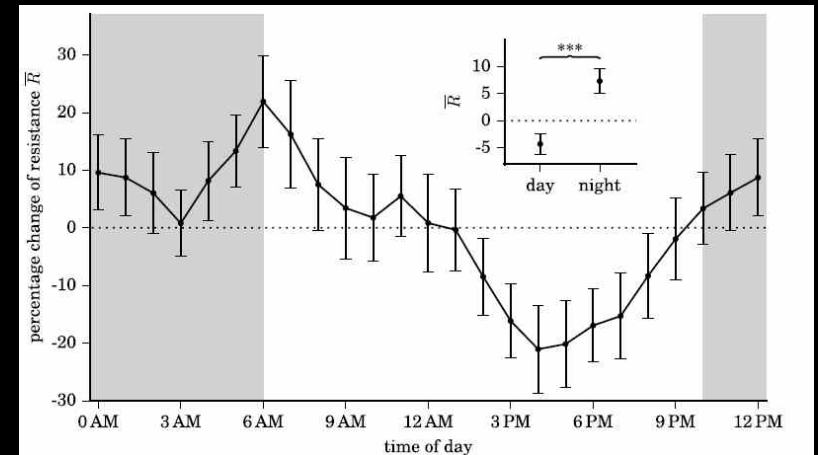
temporal resolution for clustering: 1 h

Data-driven Estimation of Brain Resilience



Summary and Outlook

- brain resilience is higher during night times
- brain resilience increases prior to seizures
 - unexpected !
 - more than two thirds of cases



- pre-seizure increase possibly reflects drug-resistance
- pre-seizure increase possibly reflects an abnormal learned response of the brain to certain repeated provocations*
- tracking brain resilience
 - improve understanding of seizure-generating mechanisms
 - improve control strategies

