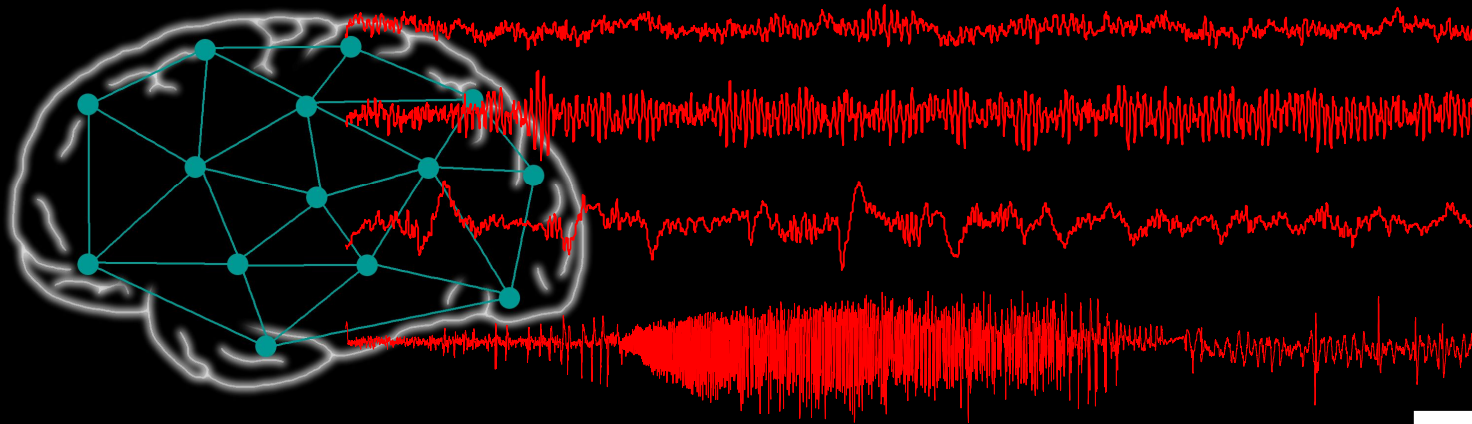


# Long-term Dynamics of Large-scale Epileptic Brain Networks

Klaus Lehnertz

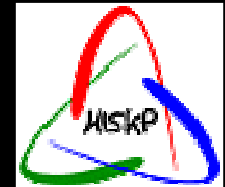


Interdisciplinary Center  
for Complex Systems



Dept. of Epileptology  
Neurophysics Group

**University of Bonn, Germany**



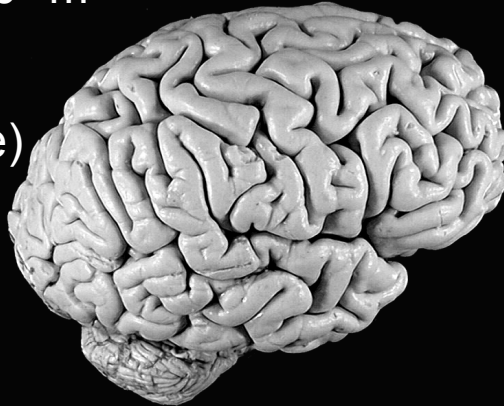
Helmholtz-Institute  
for Radiation- and  
Nuclear Physics



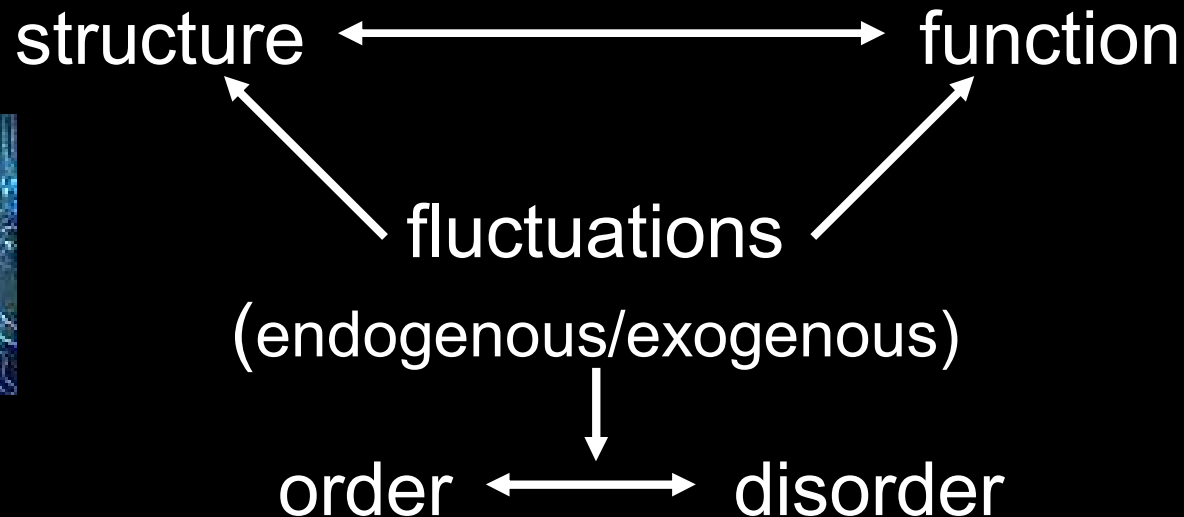
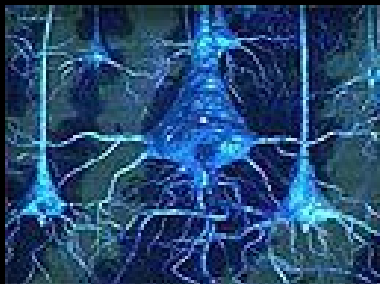
First International Summer Institute on Network Physiology (ISINP)

# Complex Network Brain

# neurons:  $\sim 10^{10}$   
# synapses/neuron:  $\sim 10^3 - 10^4$   
length of all connections:  $\sim 10^7 - 10^9$  m  
( $\sim 2.5$  x distance earth-moon)  
connectivity factor:  $\sim 10^{-6}$  (adult)  
connectivity factor:  $\sim 10^{-4}$  (juvenile)  
ion channels / neuron:  $\sim 10^2 - 10^3$   
neurotransmitter &  
other active substances:  $\sim 50$   
# glia cells:  $\sim 3$ -fold # neurons



control; movement;  
perception; attention;  
learning; memory;  
knowledge; emotions;  
motivation; language;  
thinking; planning;  
personality; self-identity;  
consciousness; ...;  
**dysfunctions**



# Epilepsy

- Greek term for *seizure*; disease first mentioned ~ 1750 BC
- ~ 1 % of world population suffers from epilepsy
- famous people suffering from epilepsy:  
Sokrates, Alexander the Great, Julius Caesar, Lenin,  
Flaubert, Dostojevski, Carroll, Poe, Berlioz, Paganini,  
Händel, van Gogh, Newton, Pascal, Helmholtz, Nobel

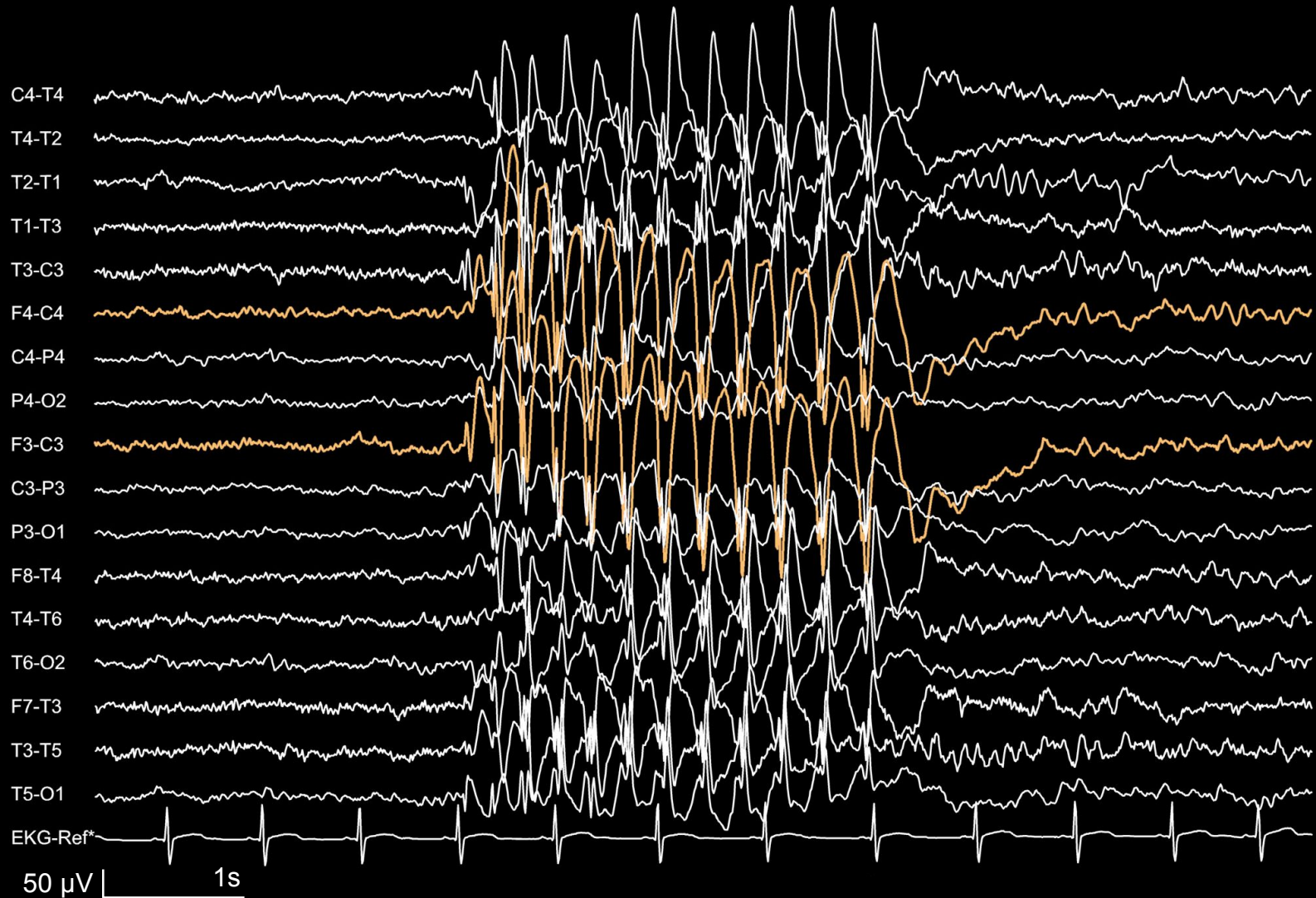
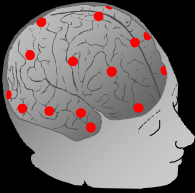


# Extreme Event Epileptic Seizure

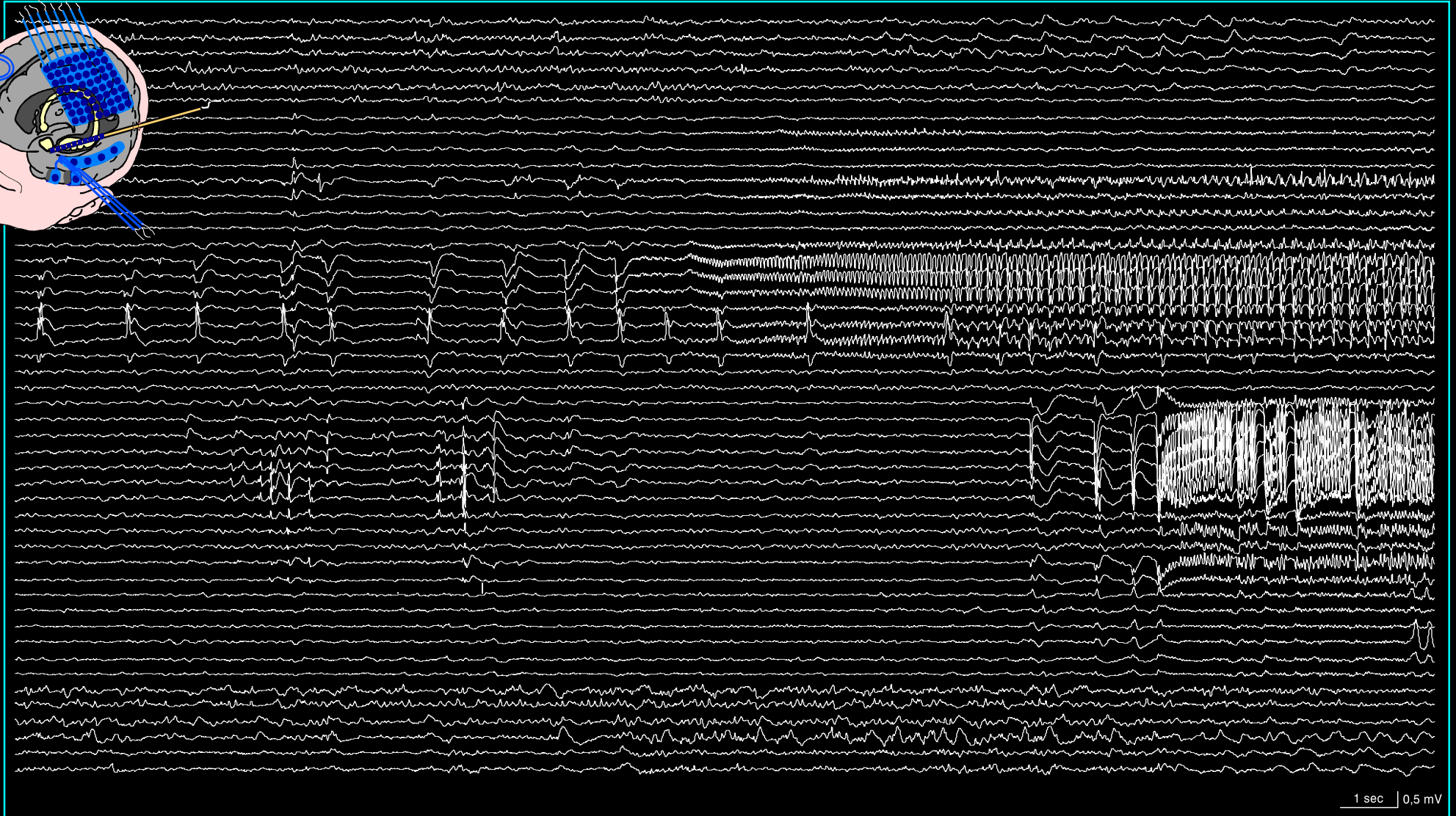
- frequency: ~ 3 szrs/mon (max.: several 100 szrs/day)
- (apparently) non-predictable (exception: reflex epilepsies)
- duration: 1 – 2 min (exception: status epilepticus > 5 min)
- during the seizure: impaired mental functions, altered consciousness, loss of consciousness, involuntary movements, ...
- after the seizure: neurologic dysfunctions, depression, ...
- main seizure types:
  - focal seizure (with/without generalization)
  - generalized seizure (apparently instantaneous)



# Epilepsy: Primary Generalized Seizure

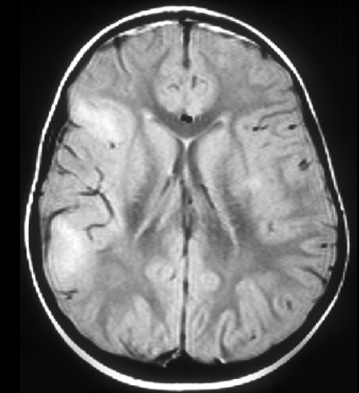
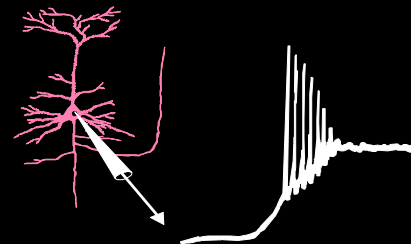
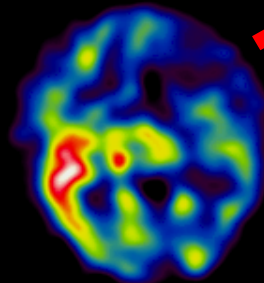
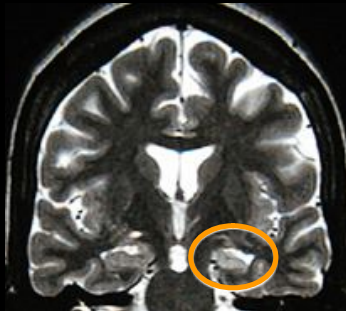
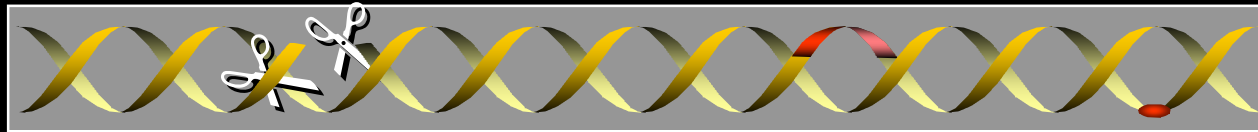


# Epilepsy: Focal Seizure with spreading



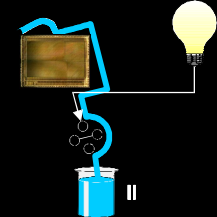
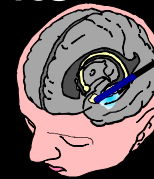
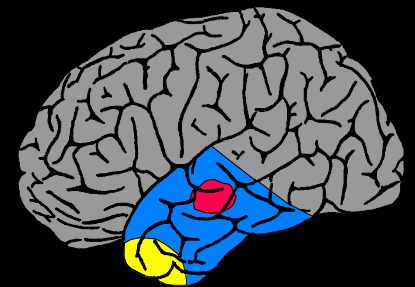


# Epilepsy is network disease !



# Treatment of Epilepsy

- **antiepileptic drugs**; primary therapy; success: ~ 70 %  
side effects, long-term treatment
- **epilepsy surgery**; option for ~ 5 – 10 % of patients  
requirement: localize and delineate epileptic focus  
from functionally relevant brain areas  
success: ~ 60 % (15 % – 85 %)  
long-term outcome, surgery-induced alterations?
- **alternative therapies**; for ~ 22 % of patients  
seizure prediction, seizure control  
success: ?





# Epilepsy --- Unsolved Issues

- basic mechanisms in humans
- where in the brain and when and why do seizures start ?
- seizure precursors ?
- where and why do seizures spread ? consistency ?
- when and why do seizure end ? consistency ?
- seizure-free interval: normal? pathologic?
- interactions epilepsy  $\leftrightarrow$  normal brain functioning (cognition)
- long-term (yrs) dynamics
- epileptic focus vs. epileptic network



# Epileptic Focus vs. Epileptic Network

## traditional concept: *epileptic focus*

- circumscribed area of the brain
- critical amount of neurons → epileptic seizures



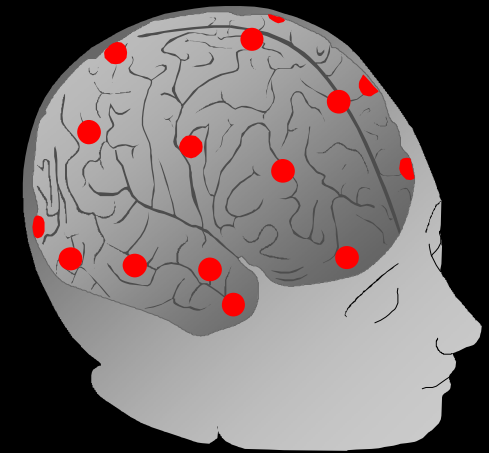
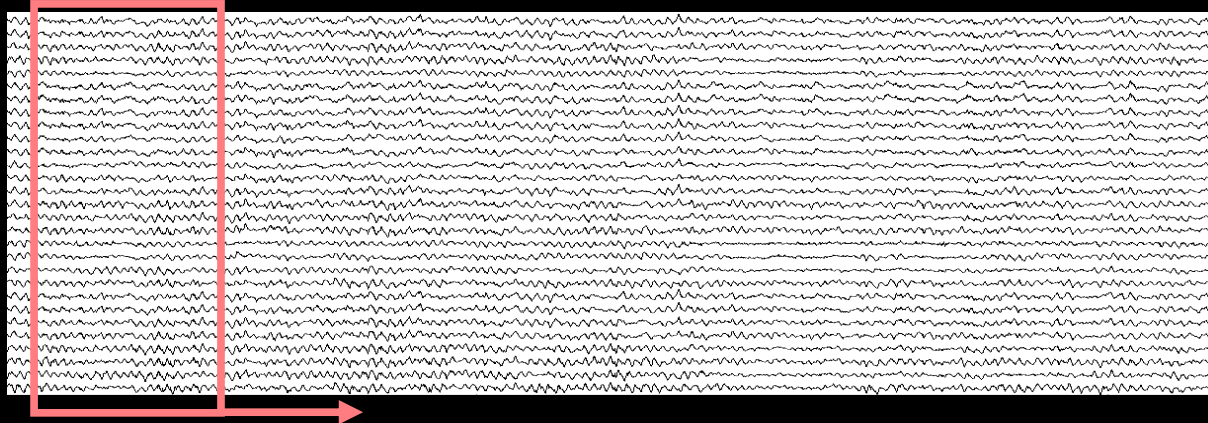
## recent evidence: *epileptic network*

- functionally and anatomically connected brain structures
- activity in any one part affects activity in all the others
- vulnerability to seizures in any one part of the network influenced by activity everywhere else in the network
- seizures may entrain large neural networks from any given part
- growing evidence from imaging, electrophysiological, and modeling studies

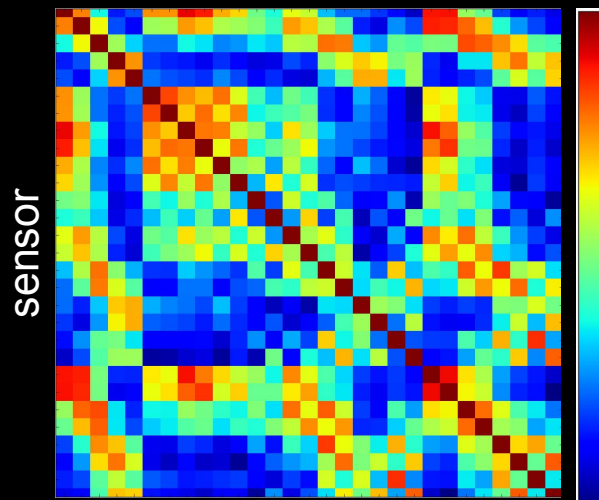


# Inferring Functional (Interaction) Brain Networks

recordings of brain dynamics (EEG, MEG, fMRI, ...)



interaction matrix  $I$

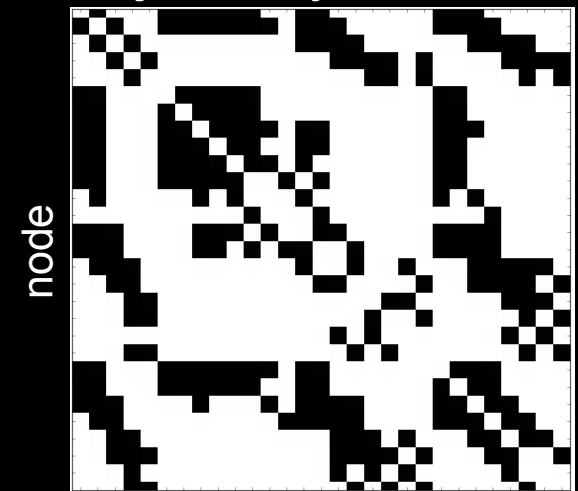


$$A = f(I)$$



- thresholding
- significance testing
- ...

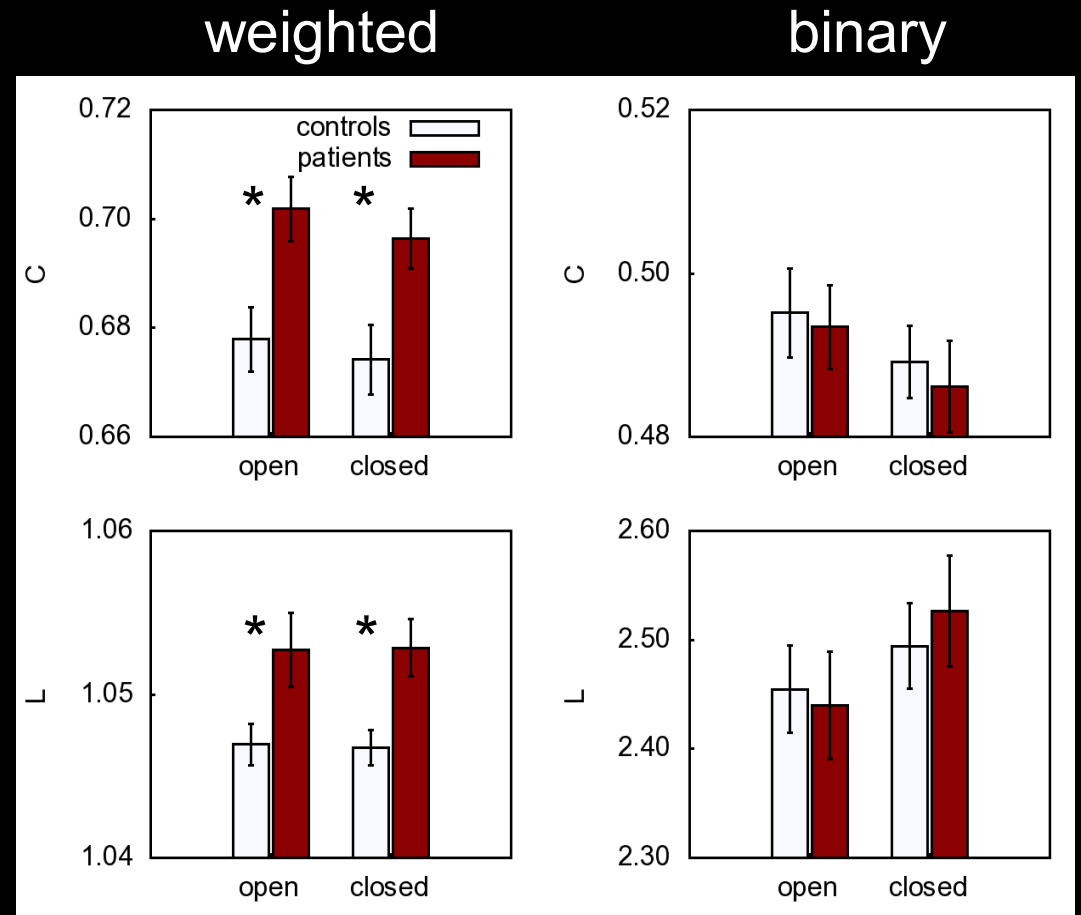
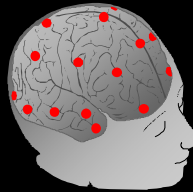
adjacency matrix  $A$



# Functional Brain Networks: Epilepsy vs. Controls

*epileptic networks are more regular than healthy ones*

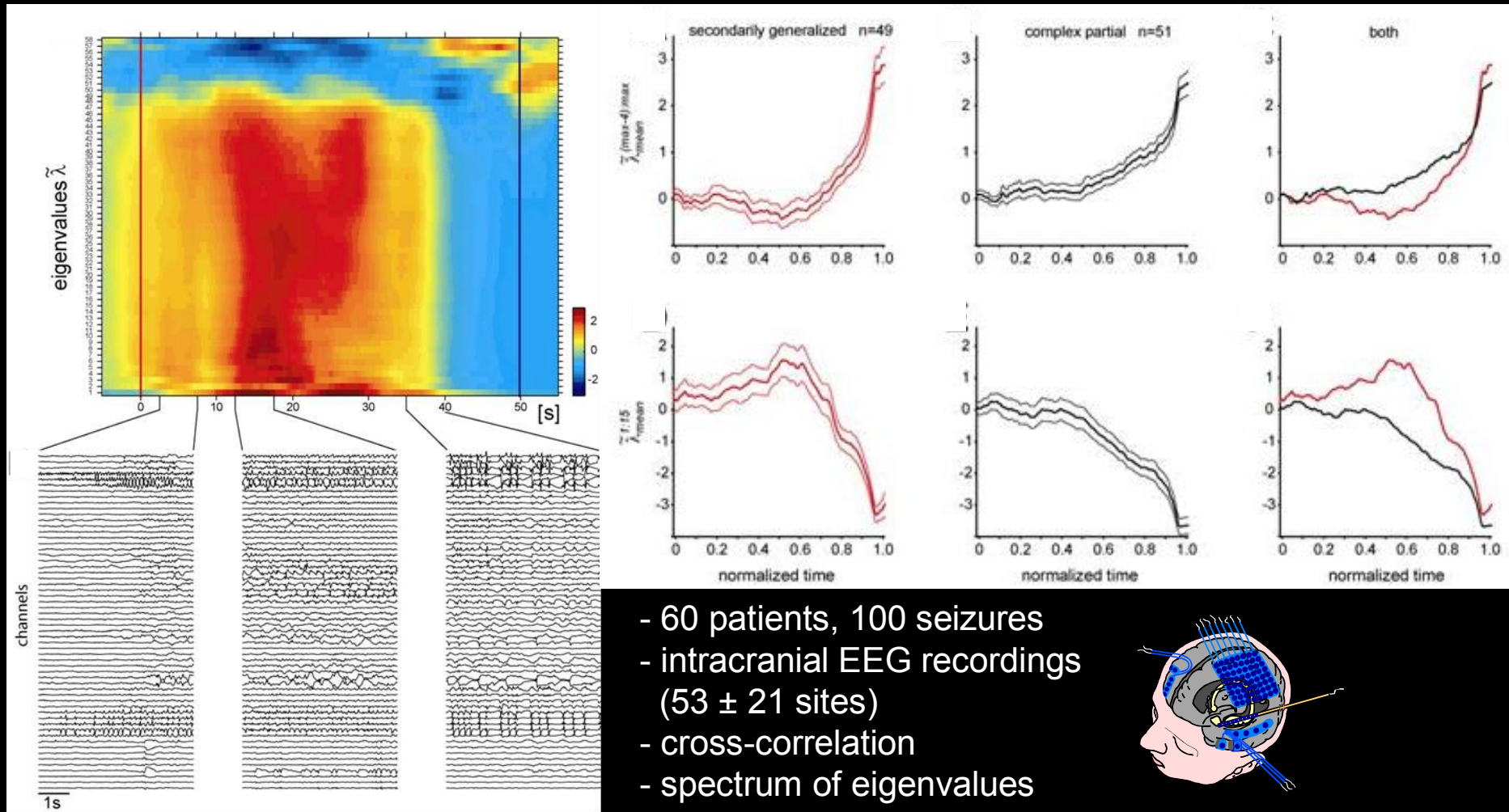
- 21 patients, 23 controls
- scalp EEG recordings (29 sites)
- eyes-open (15 min)
- eyes-closed (15 min)
- mean phase coherence (frequency-adaptive; -selective)
- binary networks (fixed mean degree, thresholding)
- weighted networks (different normalizations)
- clustering coefficient  $C$
- average shortest path length  $L$



0.5 – 5 Hz ( $\delta$ -band) \*  $p < 0.05$

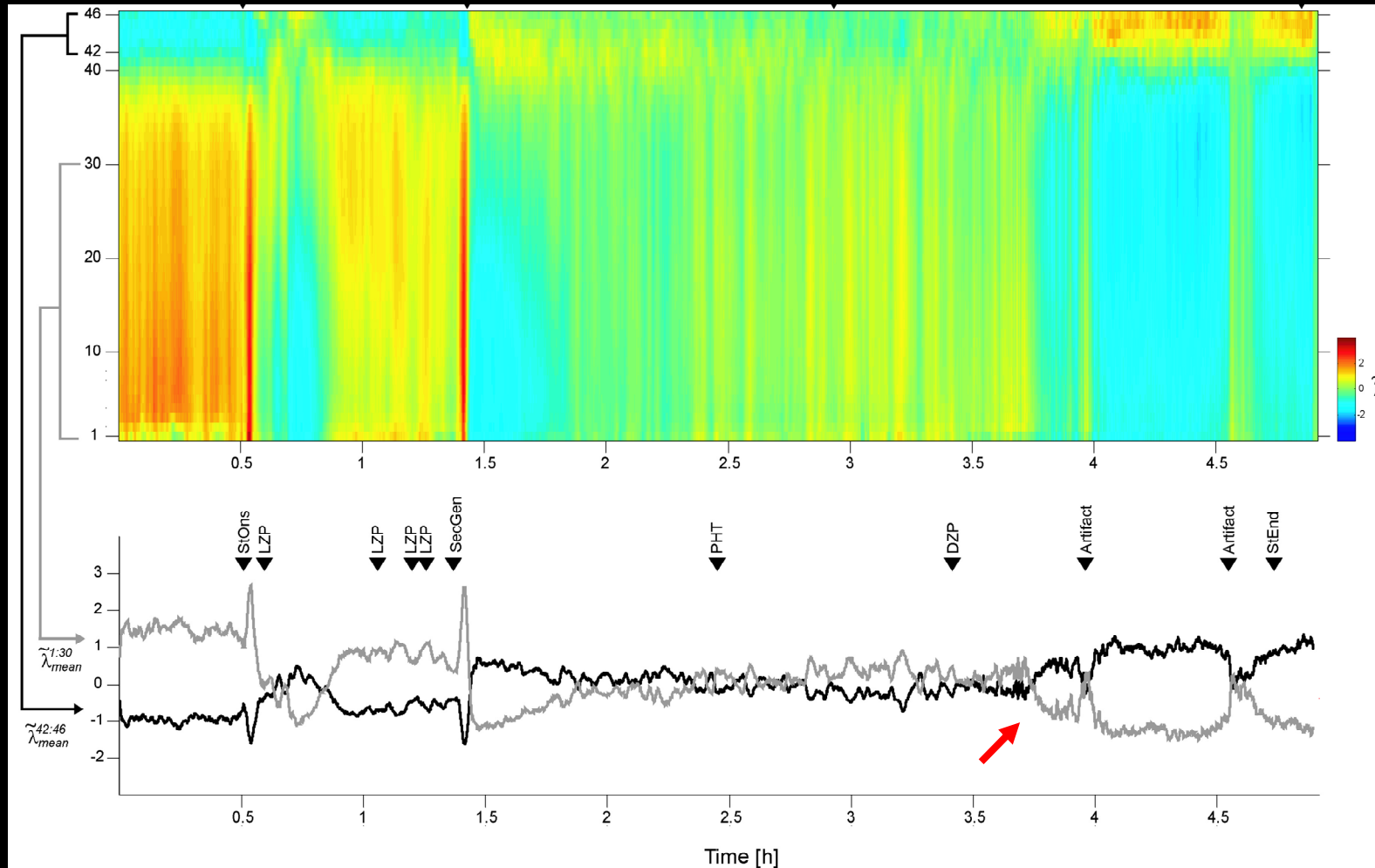
# Epileptic Networks during Seizures

*network sync: a mechanism for seizure termination?*



# Epileptic Networks during Status Epilepticus

*network sync: a mechanism for seizure termination?*

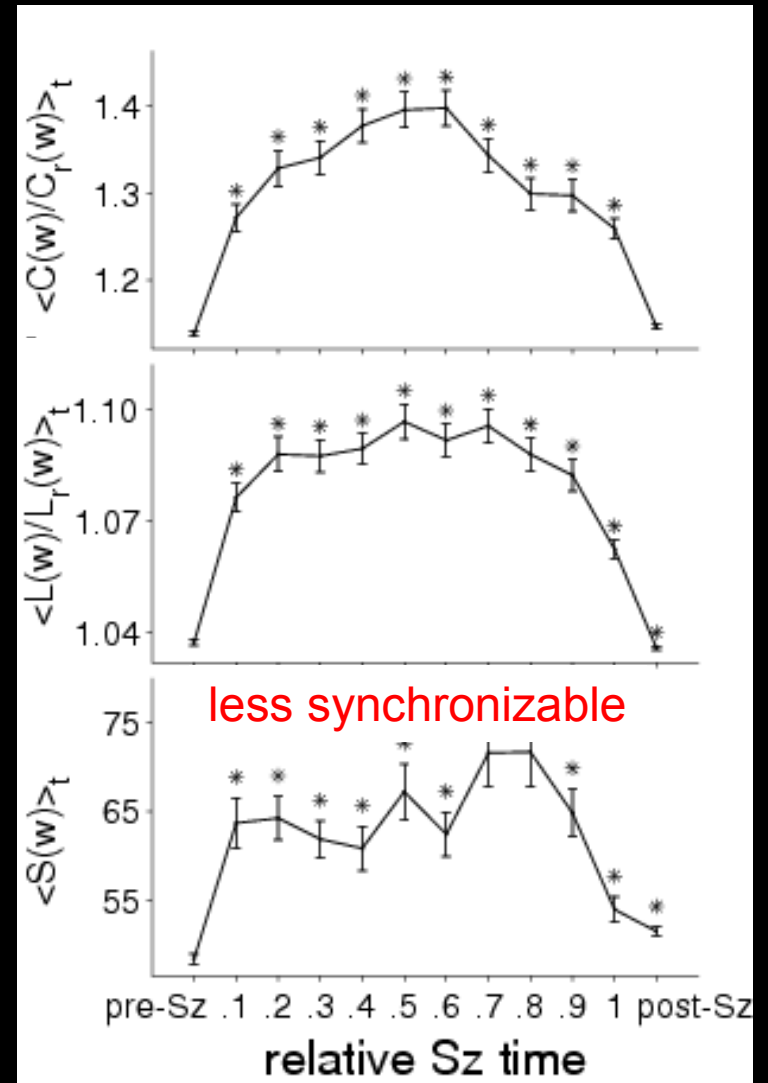
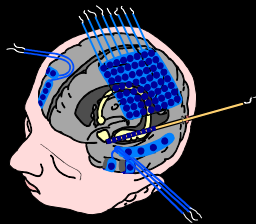




# Epileptic Networks during Seizures

from **functional topology**  
 to **more random**  
 to **more regular**  
 back to **more random**

- 60 patients, 100 seizures
- intracranial EEG recordings (53 ± 21 sites)
- max. cross-correlation fct.
- thresholding ( $A$  fully connected)
- clustering coefficient  $C$
- average shortest path length  $L$
- **synchronizability**  $S = \lambda_{\max} / \lambda_{\min}$  from Laplace matrix
- comparison with random networks (prescribed degree sequence)

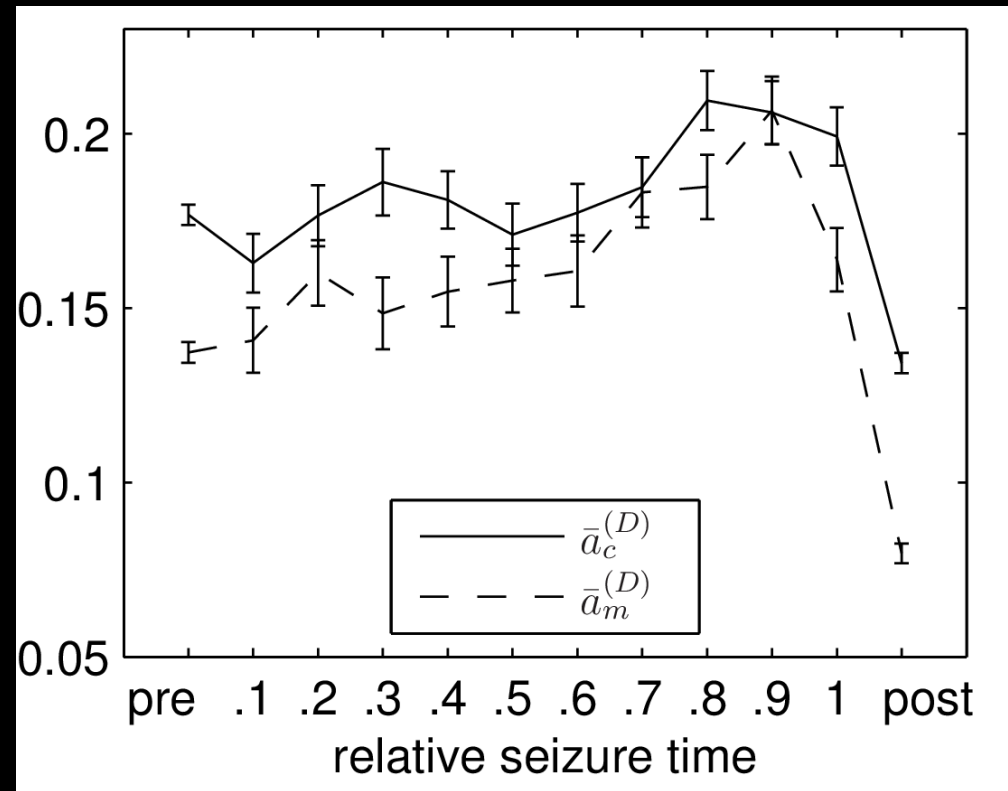
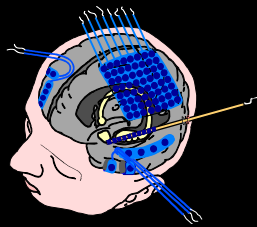


# Epileptic Networks during Seizures

**networks are assortative**

- **harder to synchronize**
- **network disintegration**
- **less vulnerable to attacks**

- 60 patients, 100 seizures
- intracranial EEG recordings ( $53 \pm 21$  sites)
- correlation coefficient
- max. of cross-correlation fct
- thresholding ( $A$  fully connected)
- assortativity coefficient  $a$
- comparison with surrogate networks (based on IAAFT time series surrogates)

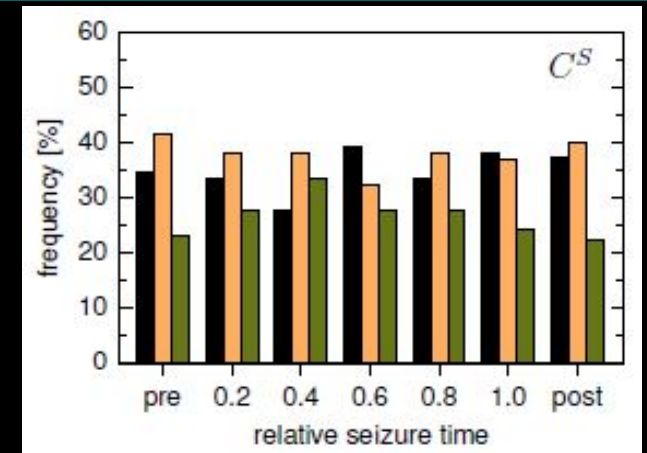
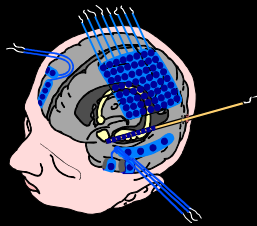


# Epileptic Networks during Seizures

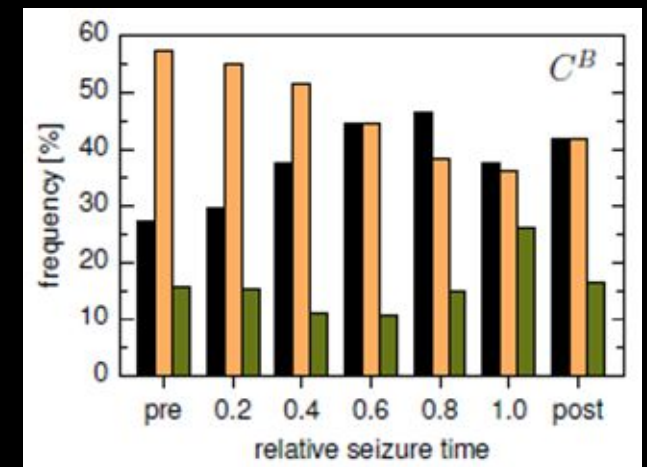
*how important is the epileptic focus?*

- *important in only 35 % of cases*
- *neighborhood more important (>50%)*
- *neighborhood → bridge*
- *improved prevention techniques?*

- 52 patients, 86 seizures
- intracranial EEG recordings (53 ± 21 sites)
- correlation coefficient
- max. of cross-correlation fct
- weighted networks ( $A$  normalized)
- various centrality indices: strength ( $C^S$ ), eigenvector, closeness, betweenness ( $C^B$ )
- comparison with surrogate networks (based on IAAFT time series surrogates)



*similar findings with eigenvector centrality*

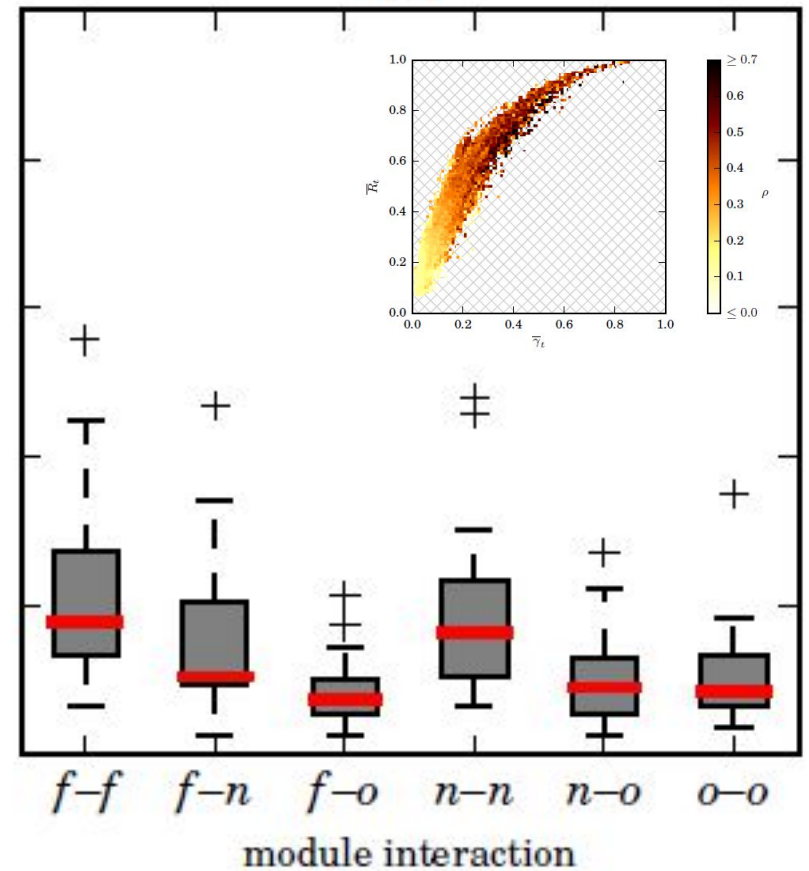
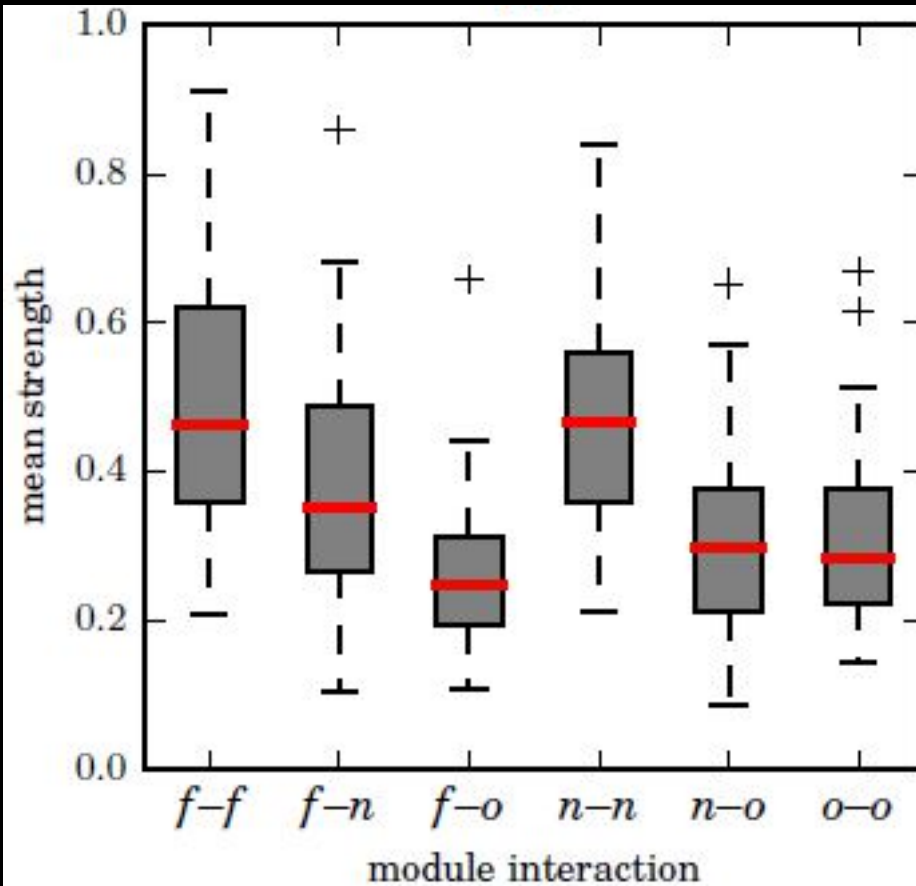


*similar findings with closeness centrality*

# Strength of Interactions in Epileptic Networks

phase-based approach

information-theoretic approach

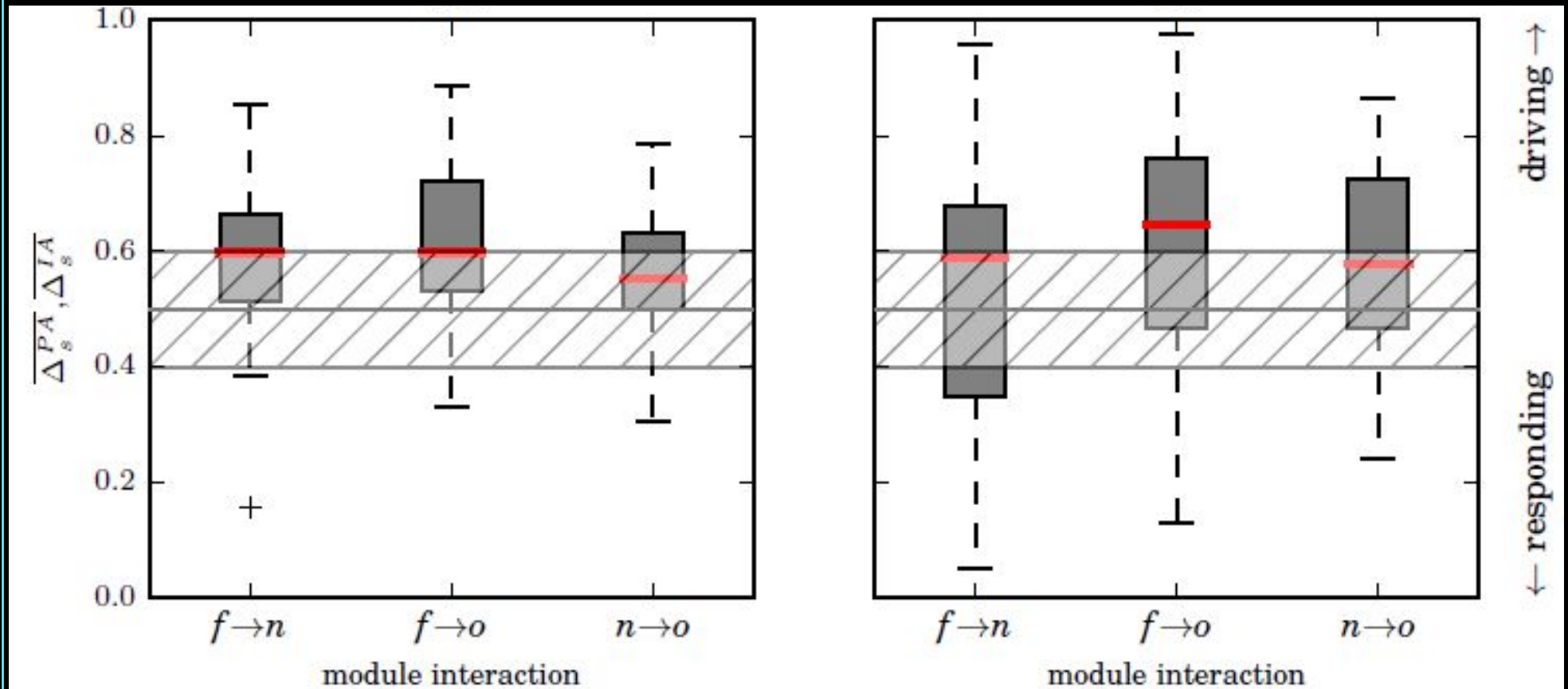


35 patients;  $\emptyset$  51 sites;  $\emptyset$  114 hrs iEEG recording; szr-free interval only

# Direction of Interactions in Epileptic Networks

phase-based approach

information-theoretic approach



35 patients; Ø 51 sites; Ø 114 hrs iEEG recording; szr-free interval only

# Strength and Direction of Interactions

patient group:

- highest strength of interactions within the epileptic focus (gradually declines with increasing distance)
- epileptic focus “drives” all other brain areas
- largely unaffected by physiological activities (e.g. circadian rhythms)

single patient

- very high variability (... reasons?)

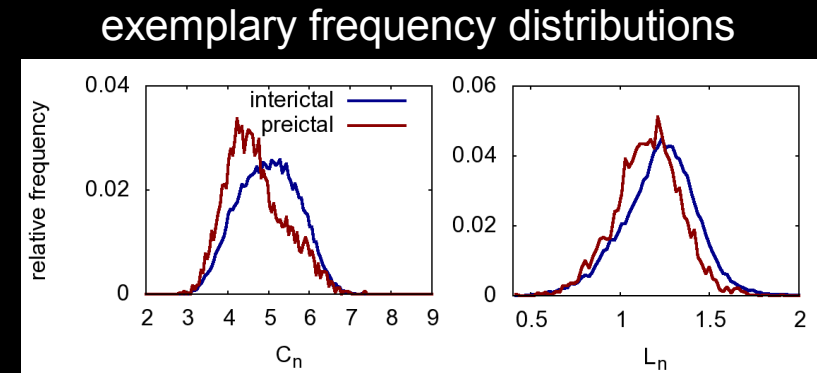
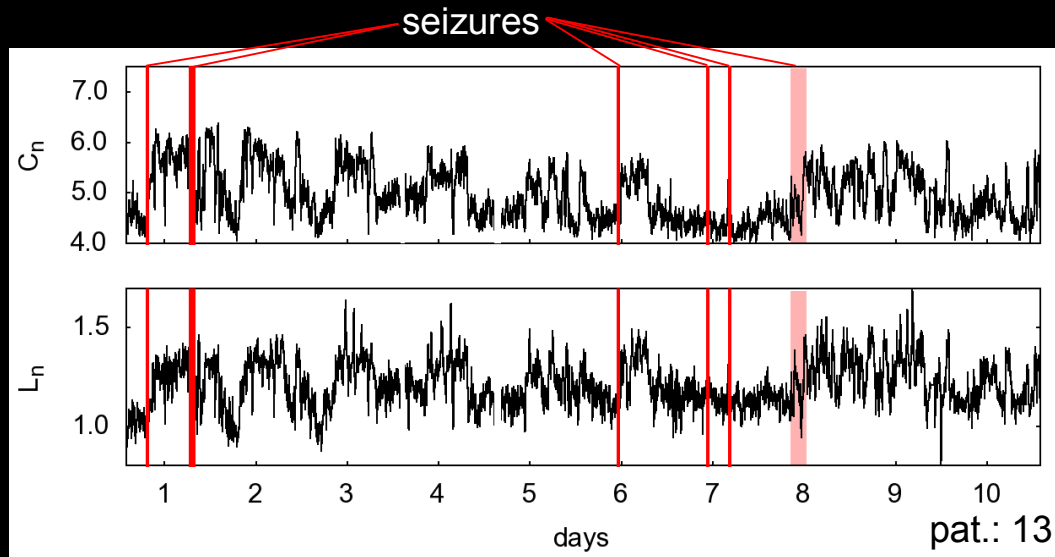
similar findings (phase-based vs information-theoretic approaches)

- what kind of synchronization phenomena ?  
(phase, generalized, ...) ?
- confounding variables ?

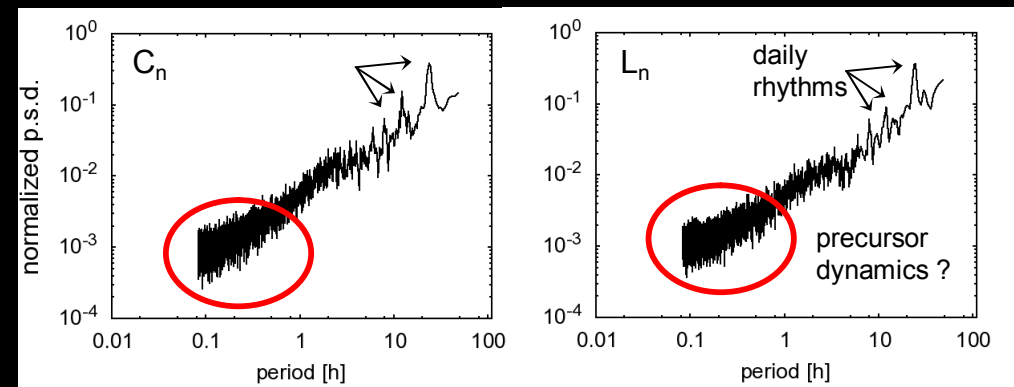


# Long-Term Dynamics of Epileptic Networks ( $C$ , $L$ )

*mainly reflects daily rhythms, epileptic process only marginally*



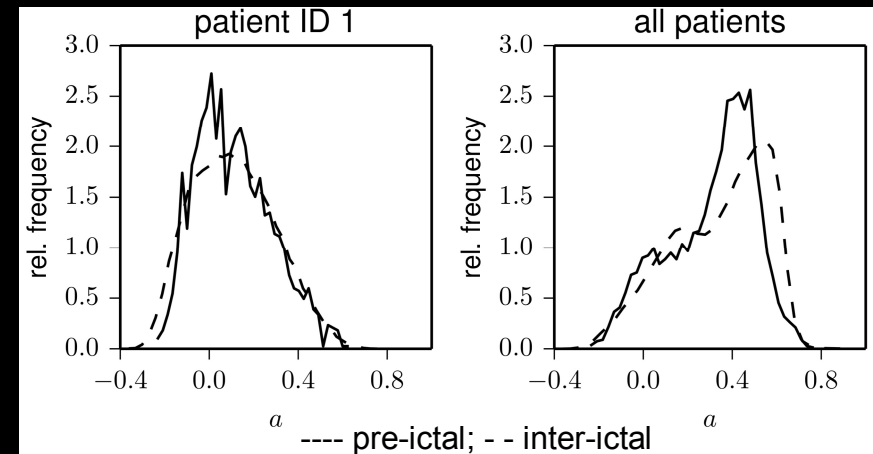
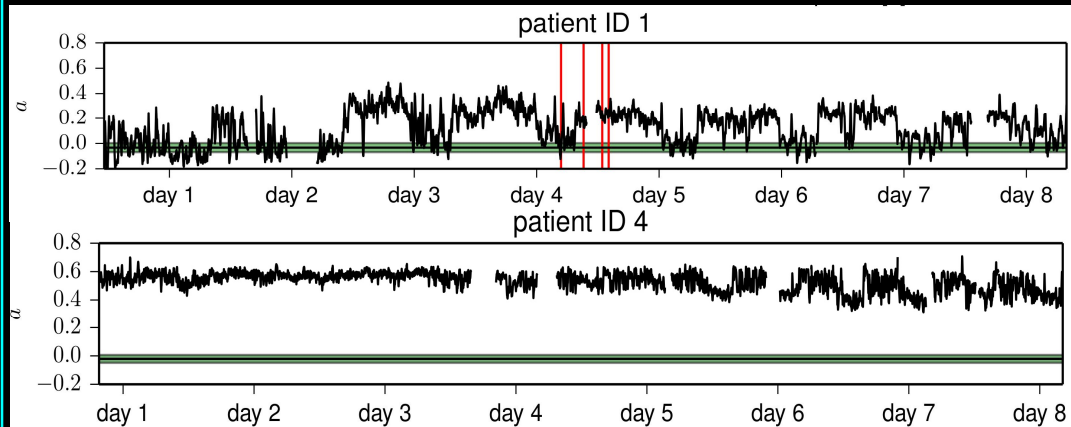
power spectral density estimates  
(grand average)



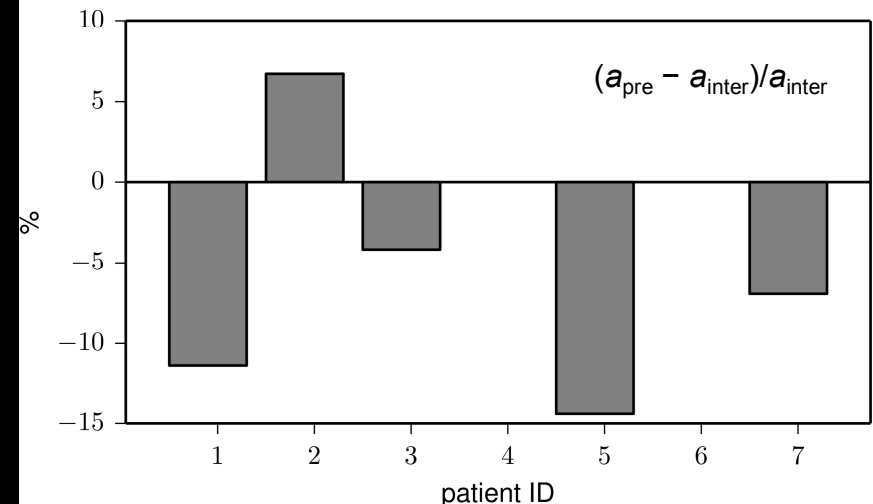
- 13 patients, 75 seizures
- intracranial EEG recordings (> 2100 h)  
(56 sites, range: 24-72)
- mean phase coherence (frequency-adaptive)
- thresholding (fixed mean degree)
- clustering coefficient  $C$
- average shortest path length  $L$

# Long-Term Dynamics of Epileptic Networks (a)

*mainly reflects daily rhythms, easier to synchronize pre-ictally?*

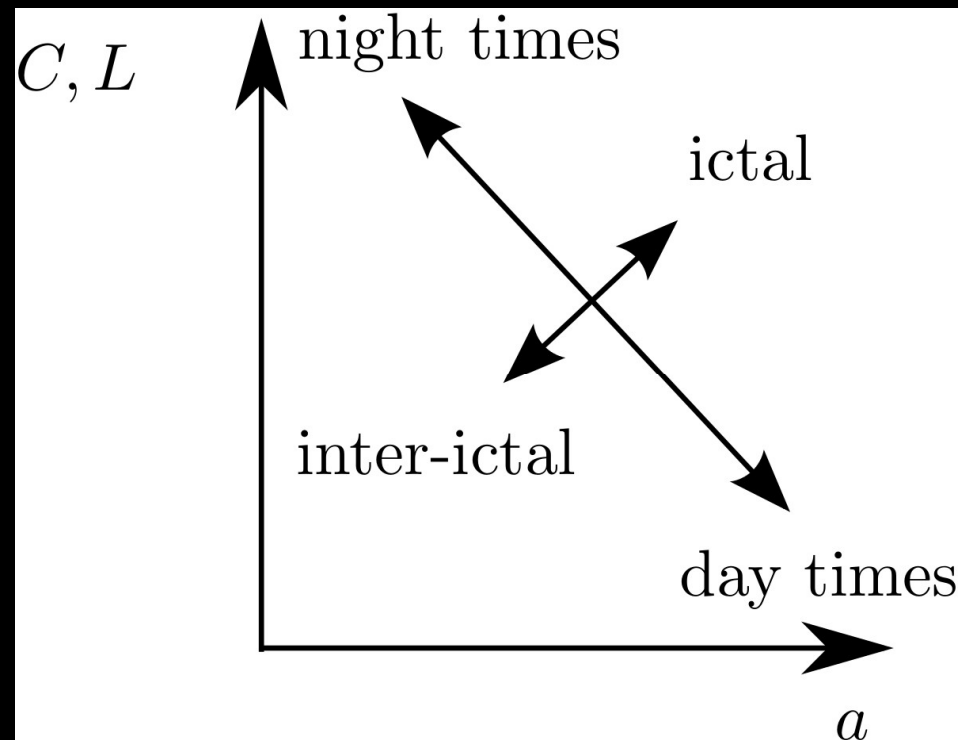


- 7 patients, 16 seizures
- intracranial EEG recordings (> 1000 h)  
(90 sites, range: 44-90)
- mean phase coherence (frequency-adaptive)
- thresholding (pre-def. link density)
- assortativity  $a$
- comparison with surrogate networks



# Long-Term Dynamics of Epileptic Networks

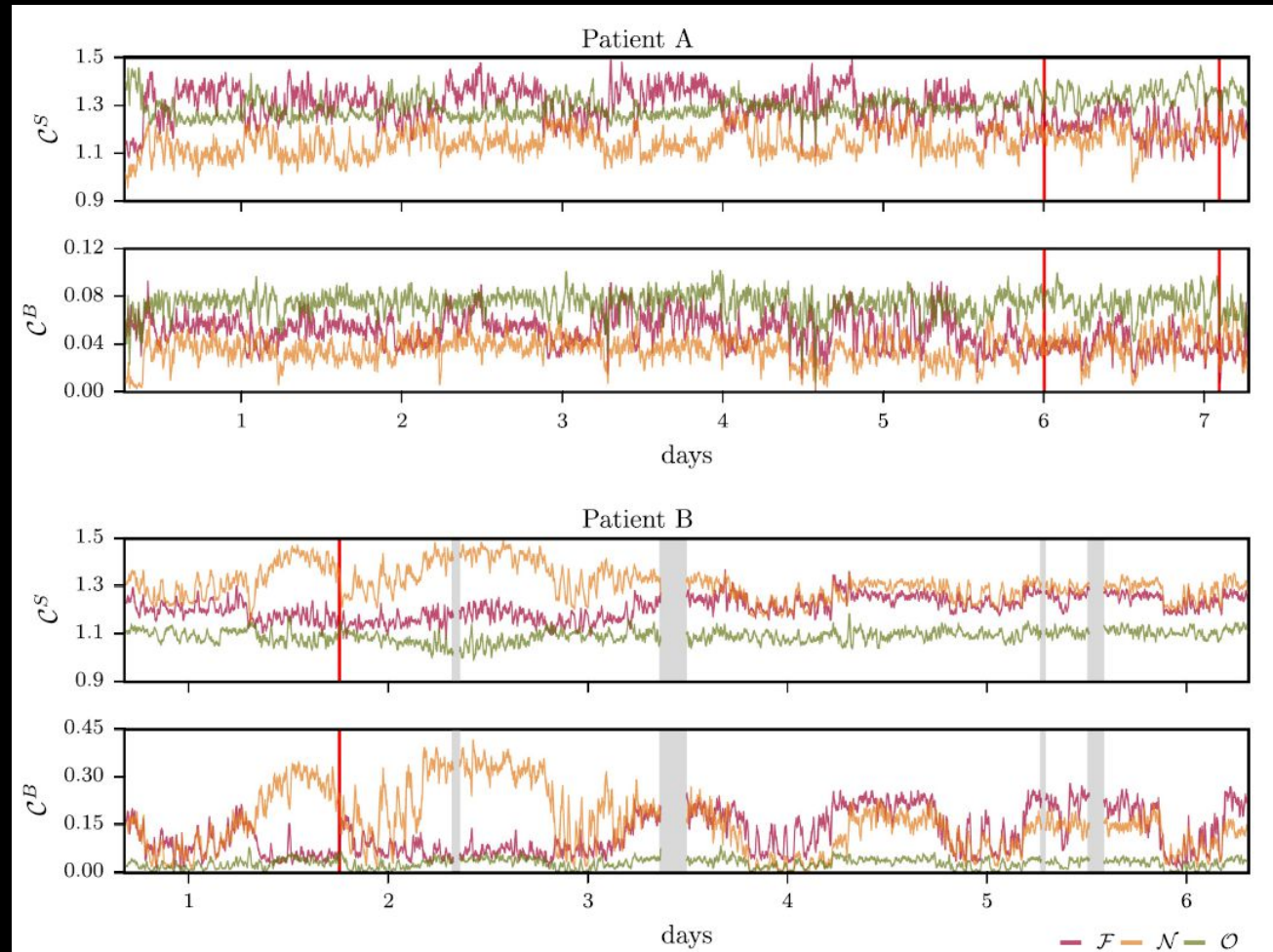
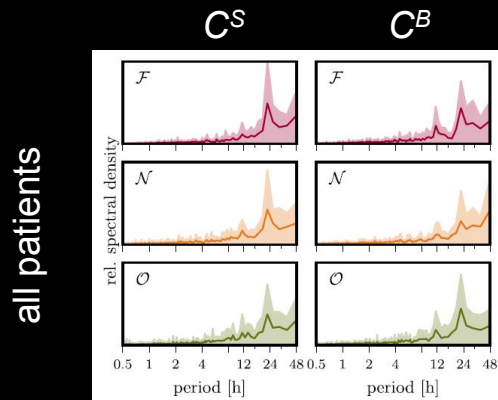
*how epileptic brain networks explore the space  $(a, C, L)$  of accessible network topologies*



# Long-Term Node Importance in Epileptic Networks

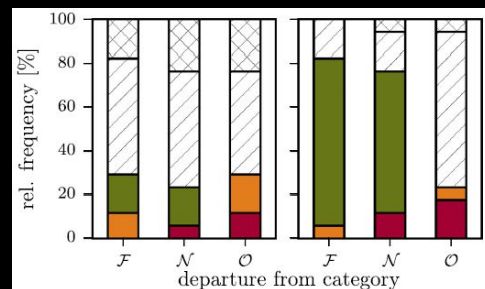
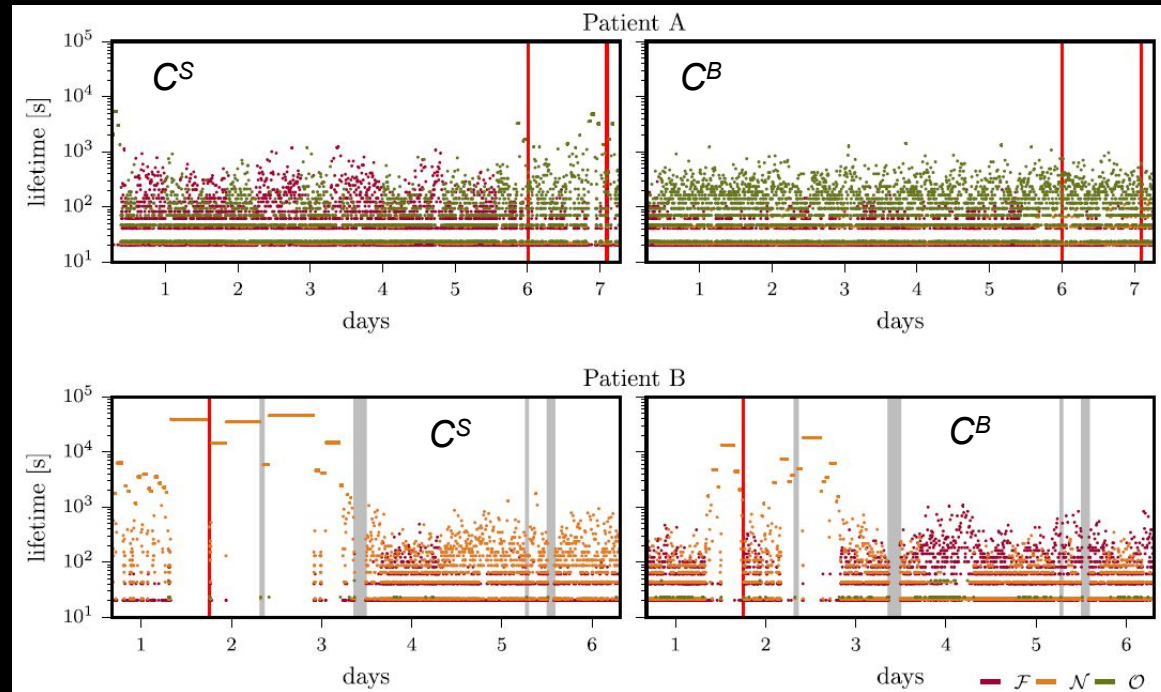
*importance of brain regions is highly variable*

- 17 patients, 83 seizures
- intracranial EEG recordings (> 2100 h; sites range: 16-64)
- mean phase coherence (frequency-adaptive)
- normalized weighted networks
- strength and betweenness centrality ( $C^S$ ,  $C^B$ ) and relationship to focus (F), neighborhood (N), other brain areas (O)

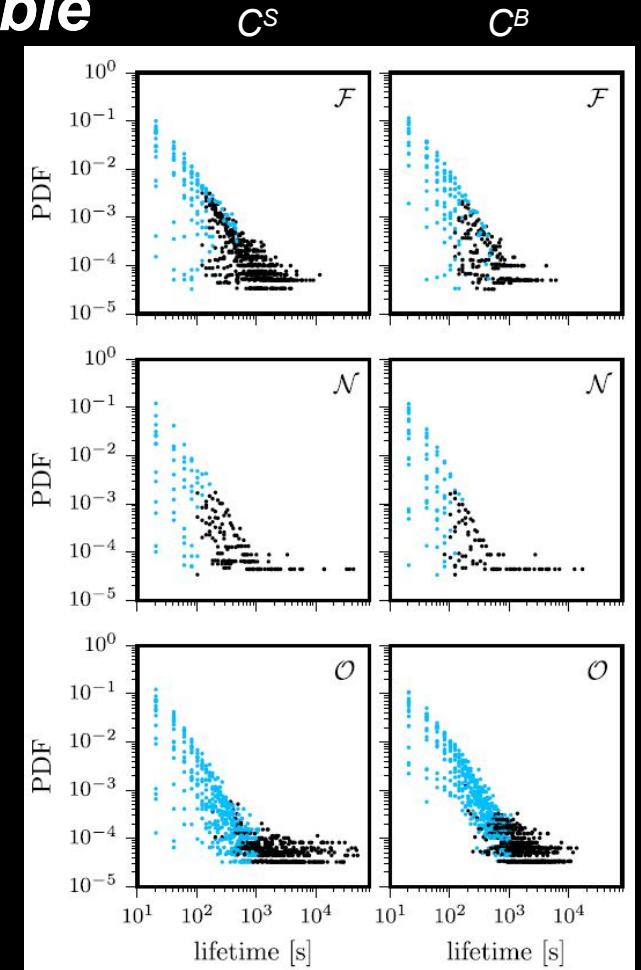


# Long-Term Node Importance in Epileptic Networks

*importance of brain regions is highly variable*



left:  $C^S$   
 right:  $C^B$   
 hatched bars: patients with no significant alterations  
 cross-hatched bars: patients with no alterations



blue dots: epochs with lifetimes shorter than expected under null hypothesis: occurrence probabilities determined by population densities of  $F, N, O$

# Seizure Prediction and Prevention

**prediction feasible**, but ...

... not in all patients

... not in all seizures

unsolved issues:

- **when to prevent**
- **where to prevent**
- **how to disturb**

**an adaptive system?**

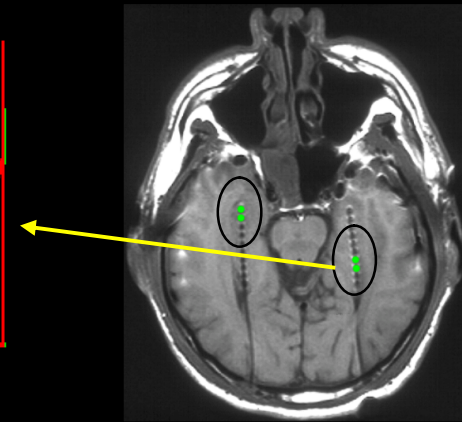
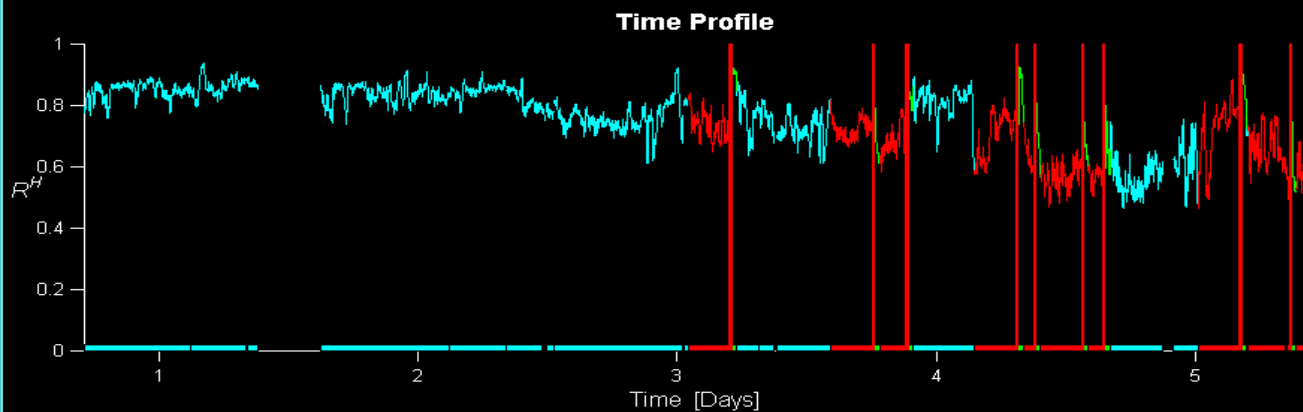


from: Cook et al., *Lancet Neurol* 2013; 12: 563



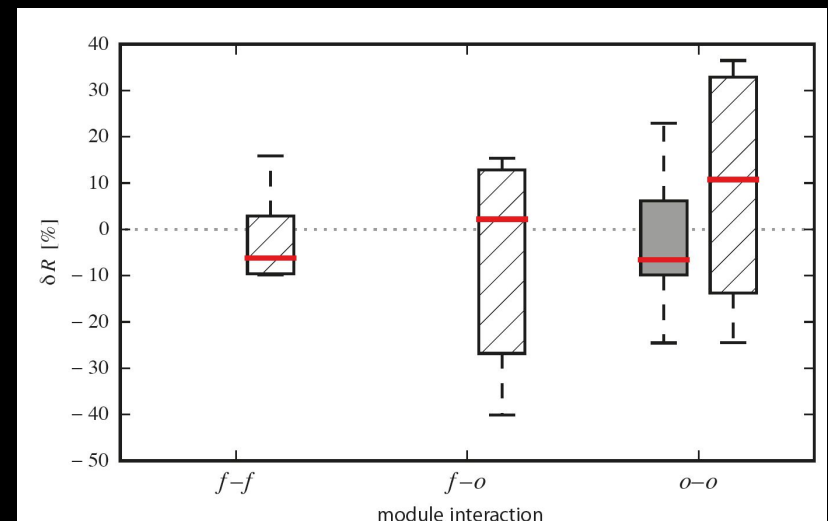


# Searching for Seizure Precursors



## **seizure precursors**

- best identifiable from interaction measurements
- synchronization vs. de-synchronization
- when: up to hours before onset
- where: mostly far off epileptic focus
- dependent on epilepsy type
- targeted interventions

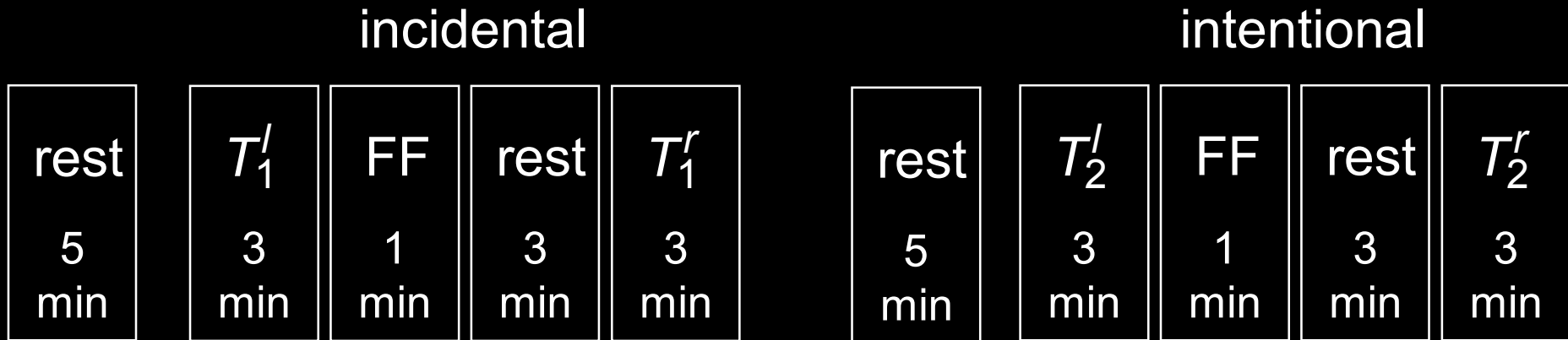


$f$  = focus,  $n$  = neighborhood,  $o$  = other

 unifocal epilepsies (N=20)  multifocal epilepsies (N=16)

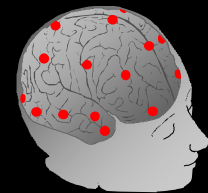


# Cognition modifies Functional Brain Networks

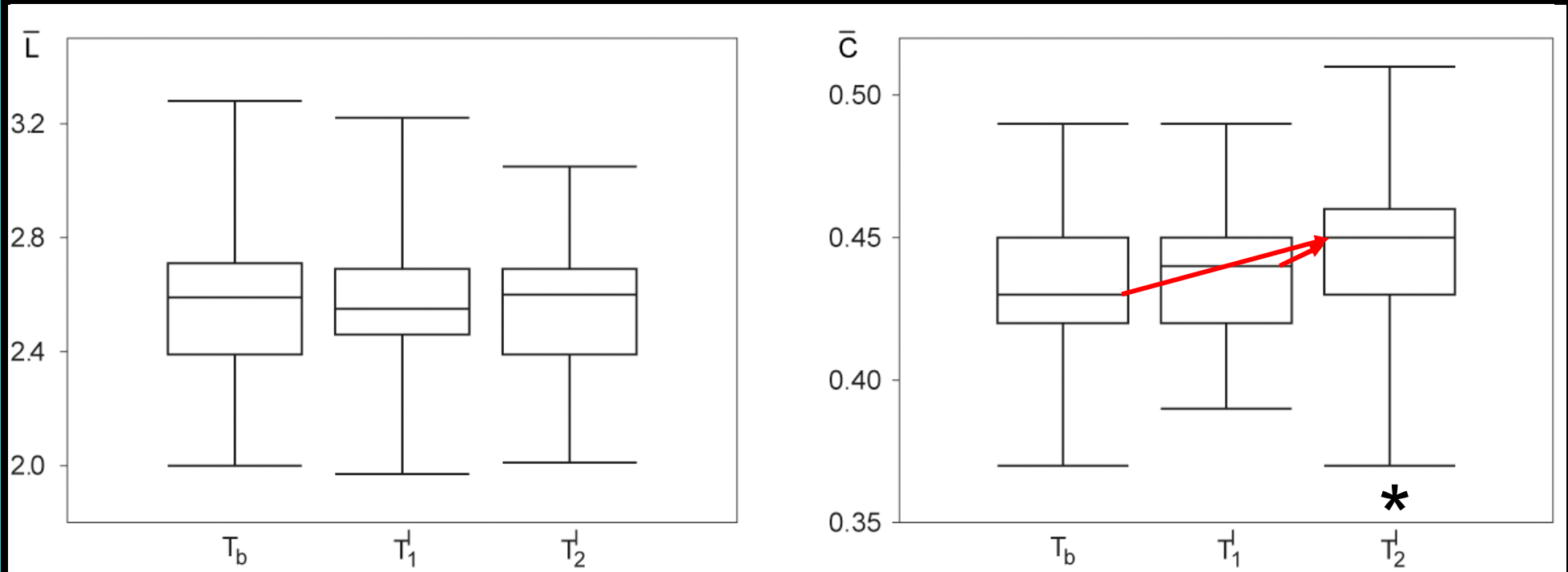


## Learning- and memory-related processes

- incidental vs. intentional learning; free recall of learned material
- number of recalled words  $N_1, N_2$
- 13 patients, 20 healthy controls; non-invasive EEG, 29 sites
- mean phase coherence
- binary networks (thresholding)
- clustering coefficient  $C$
- average shortest path length  $L$



# Cognition modifies Functional Brain Networks



group statistics:

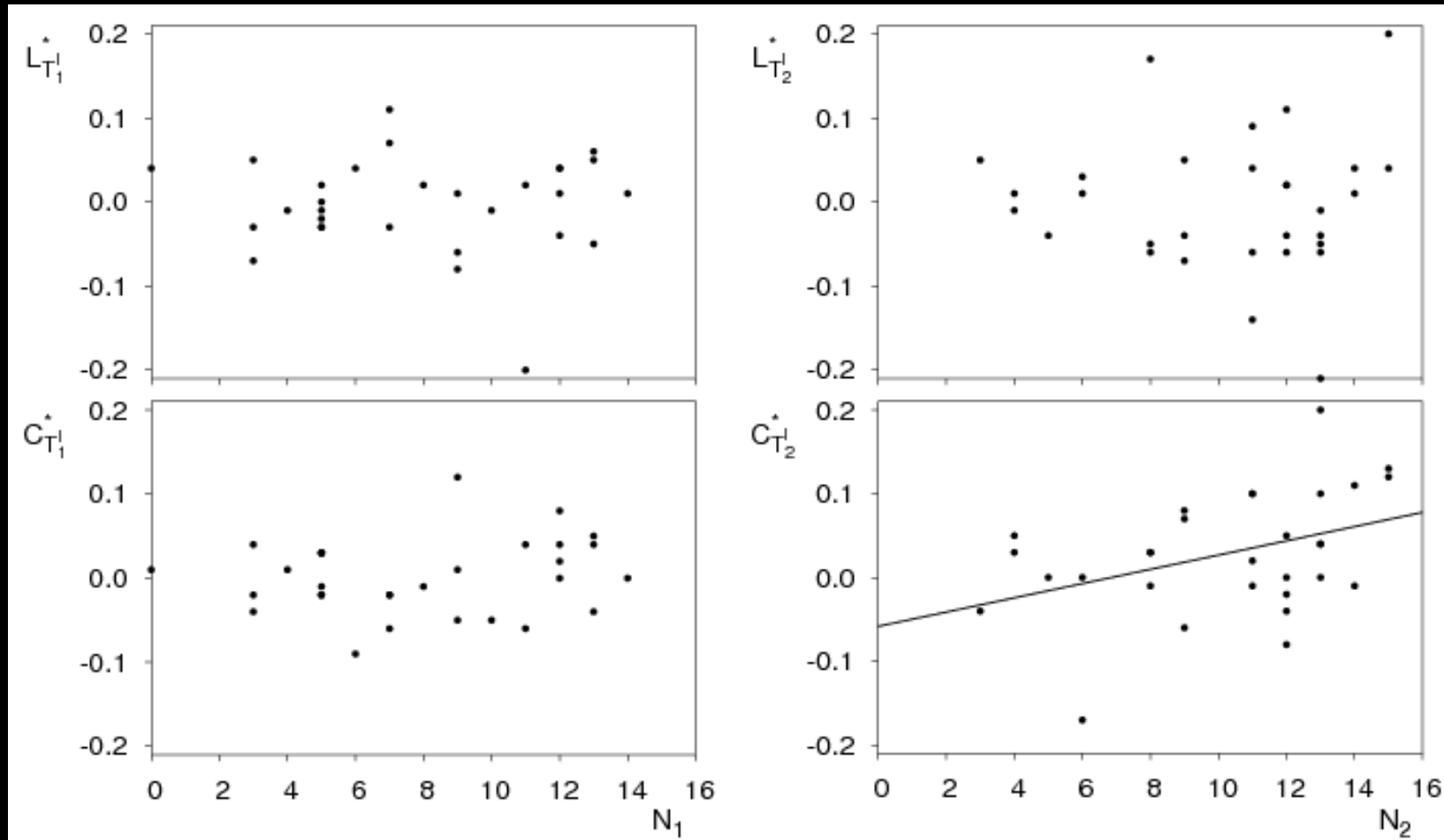
- clustering coefficient: slightly larger ( $p < 0.05$ ) during intentional learning  $T_2$  than during incidental learning  $T_1$  or during baseline  $T_b$
- average shortest path length: no significant change

# Cognition modifies Functional Brain Networks

rel. deviation from baseline

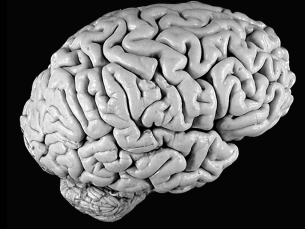
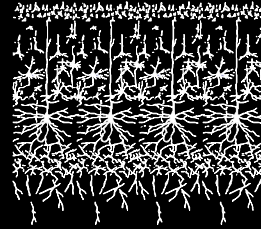
incidental

intentional



recall performance

# Modeling the Epileptic Process: On which Scales ?



integrate-and-fire  
FitzHugh-Nagumo  
Morris-Lecar  
Hodgkin-Huxley

ion channels  
neurotransmitter  
synapses  
branching structure

single cell models  
distributed neuronal  
networks

network size ( $\sim 10^5$ )  
connectivity

inhibition/excitation  
feed back/ feed forward  
coupling

interneurons / glia cells

neuronal population models

NDE, SDE, coupled ODEs,  
(s)PDE, NODE,  
lumped parameter,  
mean field approaches

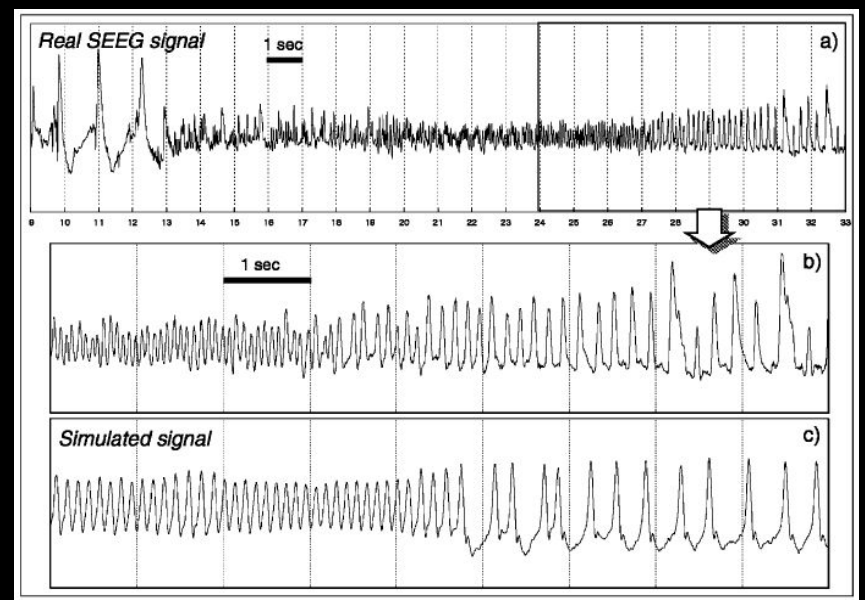
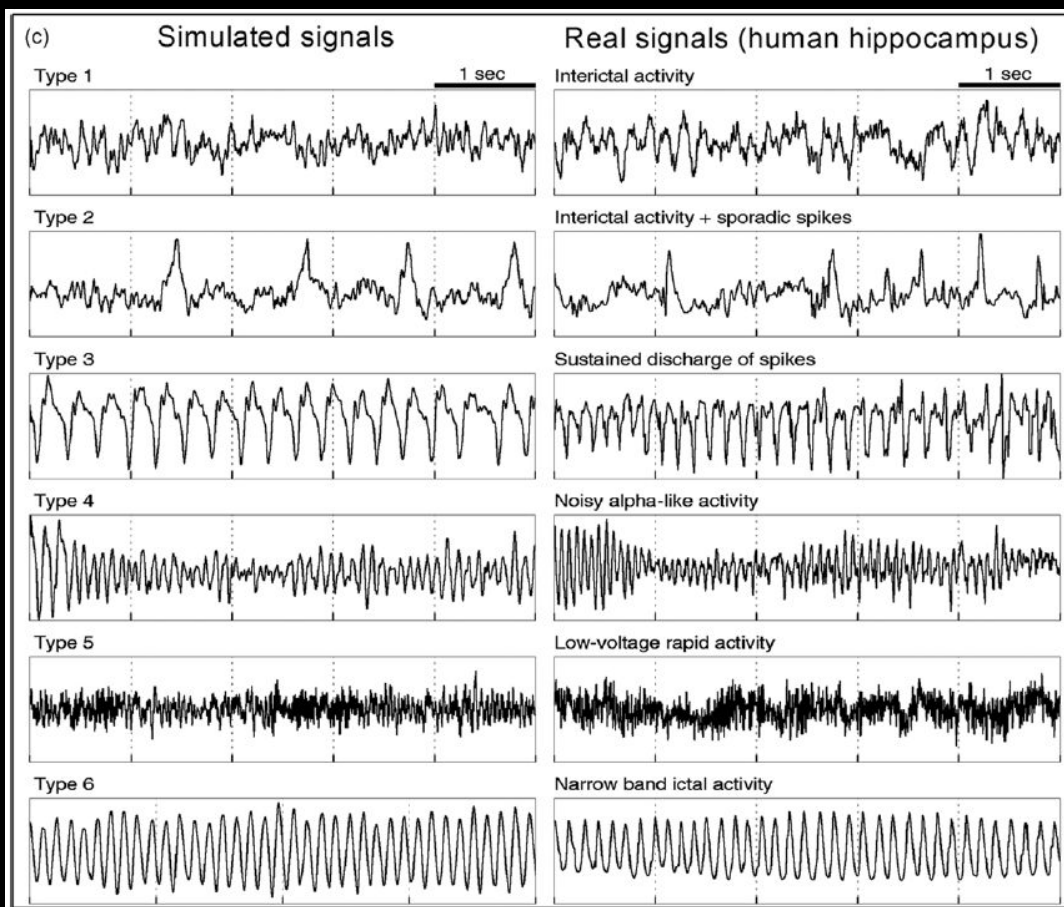
EEG phenomena

transitions

- bistability  
- parameter changes, noise



# Modeling the Epileptic Process: Neural Mass Models



- + models able to “seize”
- + transition to seizure-like activity
- + spread of seizure-like activity
- no self-termination of activity
- mostly noise driven
- time dependent control parameter



# Modeling Epileptic Network Dynamics

The Journal of Neuroscience, September 15, 2004 • 24(37):8075–8083 • 8075

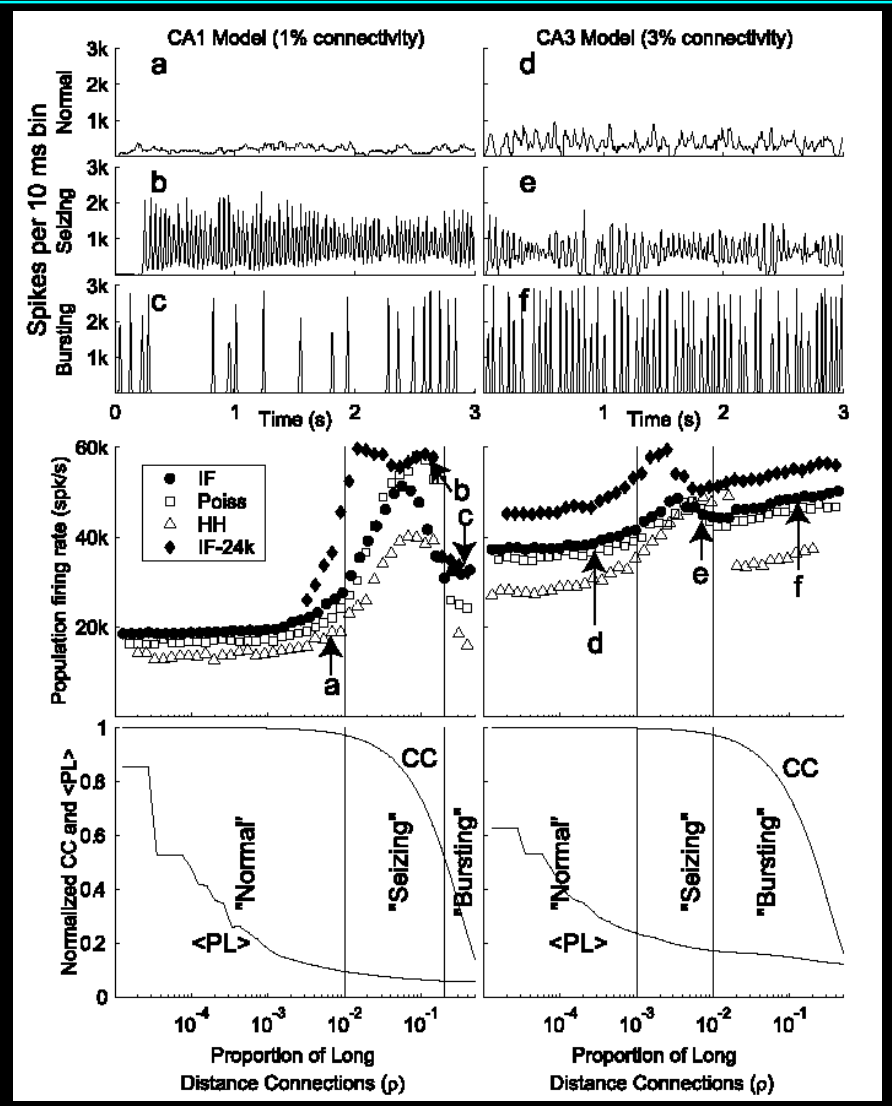
Neurobiology of Disease

## Epilepsy in Small-World Networks

Theoden I. Netoff,<sup>1,3</sup> Robert Clewley,<sup>2,3</sup> Scott Arno,<sup>1,3</sup> Tara Keck,<sup>1,3</sup> and John A. White<sup>1,3</sup>

<sup>1</sup>Department of Biomedical Engineering, <sup>2</sup>Department of Mathematics and <sup>3</sup>Center for BioDynamics and Center for Memory and Brain, Boston University, Boston, Massachusetts 02215

“By *changing parameters* such as the synaptic strengths, number of synapses per neuron, proportion of local versus long-distance connections, we induced normal, seizing, and bursting behaviors. [...] explains how *specific changes in the topology or synaptic strength* in the model *cause transitions from normal to seizing and then to bursting*. These behaviors appear to be general properties of excitatory networks.”



# Modeling Epileptic Network Dynamics

PHYSICAL REVIEW E 76, 021920 (2007)

## Internetwork and intranetwork communications during bursting dynamics: Applications to seizure prediction

S. Feldt,<sup>1,\*</sup> H. Osterhage,<sup>2,3</sup> F. Mormann,<sup>2,4</sup> K. Lehnertz,<sup>2,3,5</sup> and M. Żochowski<sup>1,6</sup>

<sup>1</sup>Department of Physics, University of Michigan, Ann Arbor, Michigan 48109, USA

<sup>2</sup>Department of Epileptology, University of Bonn, Bonn, Germany

<sup>3</sup>Helmholtz-Institute for Radiation and Nuclear Physics, University of Bonn, Bonn, Germany

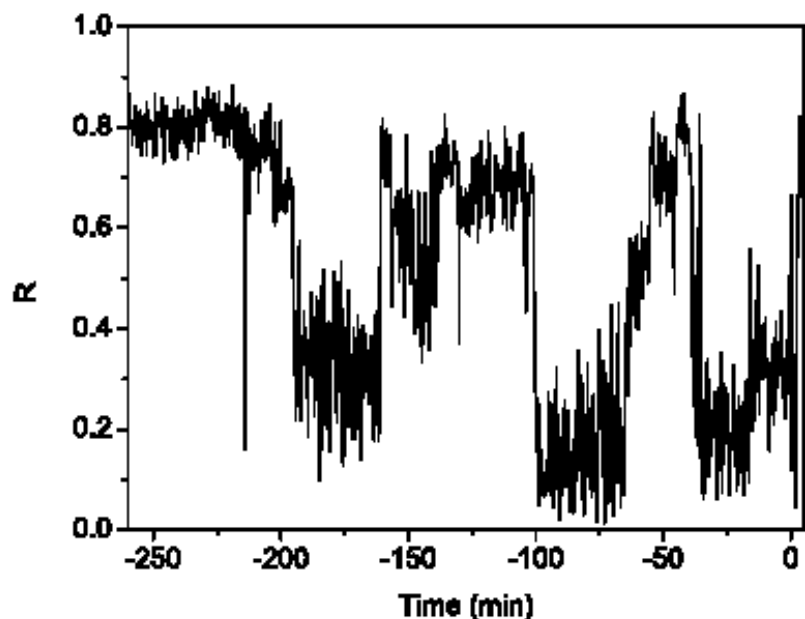
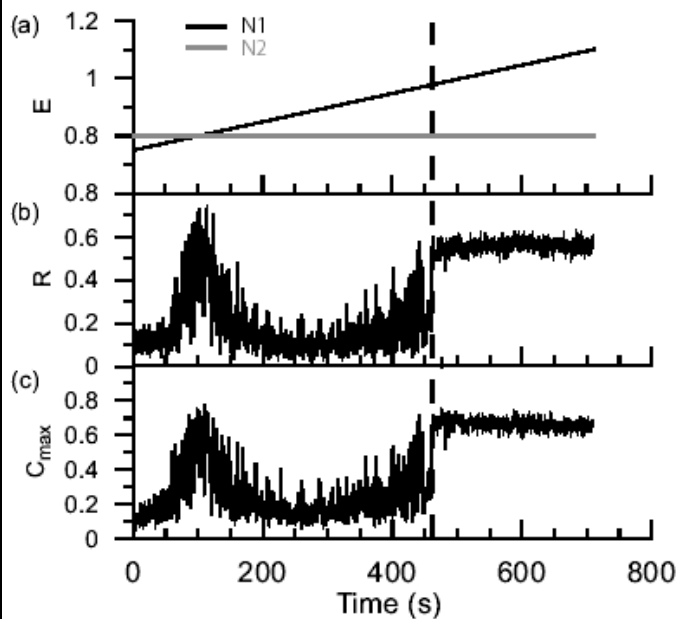
<sup>4</sup>California Institute of Technology, Division of Biology, 216-76, Pasadena, CA 91125, USA

<sup>5</sup>Interdisciplinary Center for Complex Systems, University of Bonn, Bonn, Germany

<sup>6</sup>Biophysics Research Division, University of Michigan, Ann Arbor, Michigan 48109, USA

(Received 9 March 2007; revised manuscript received 23 May 2007; published 20 August 2007)

- two interacting networks
- IF neurons (N=225)
- small-world topology

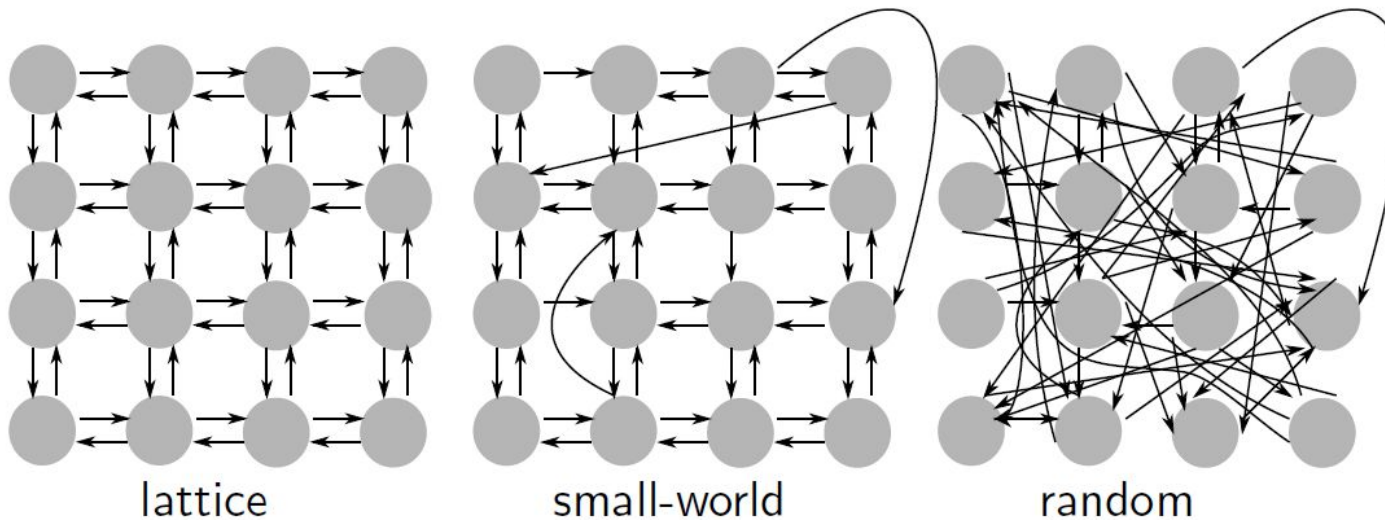


- EEG data
- MTL patient



# Self-Initiation and -Termination of Sz-like Events

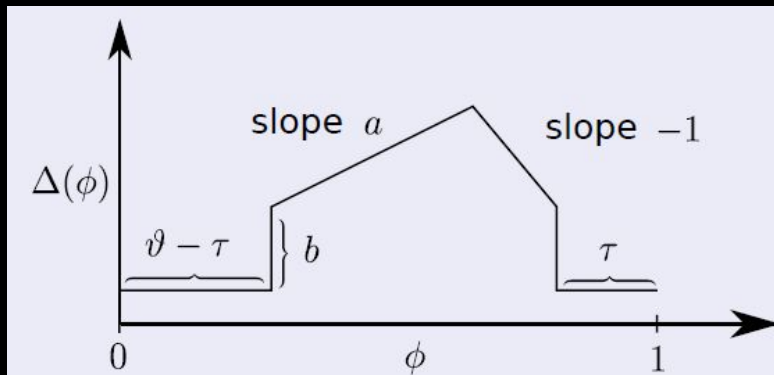
- $N \times N$  oscillators
- connect each oscillator to its  $m$  nearest neighbors
- cyclic boundary conditions (torus)
- replace fraction  $p$  of connections by connections between randomly chosen oscillators



# Self-Initiation and -Termination of Sz-like Events

## *pulse-coupled phase oscillators (IF neurons)*

- intrinsic dynamics:  $\dot{\phi}_n = 1, \phi_n \in (0, 1]$
- oscillator  $n$  fires ( $\phi_n(t_f) = 1$ )
  - ▶ excite all oscillators  $n'$  connected to  $n$   
 $\phi_j(t_f^+) = R(\phi_{n'}(t_f)) = \Delta(\phi_{n'}(t_f)) + \phi_{n'}(t_f)$
  - ▶ reset oscillator  $n$ :  $\phi_n(t_f^+) = 0$



integrate-and-fire oscillators

$\tau$  time delay

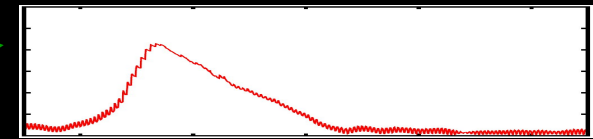
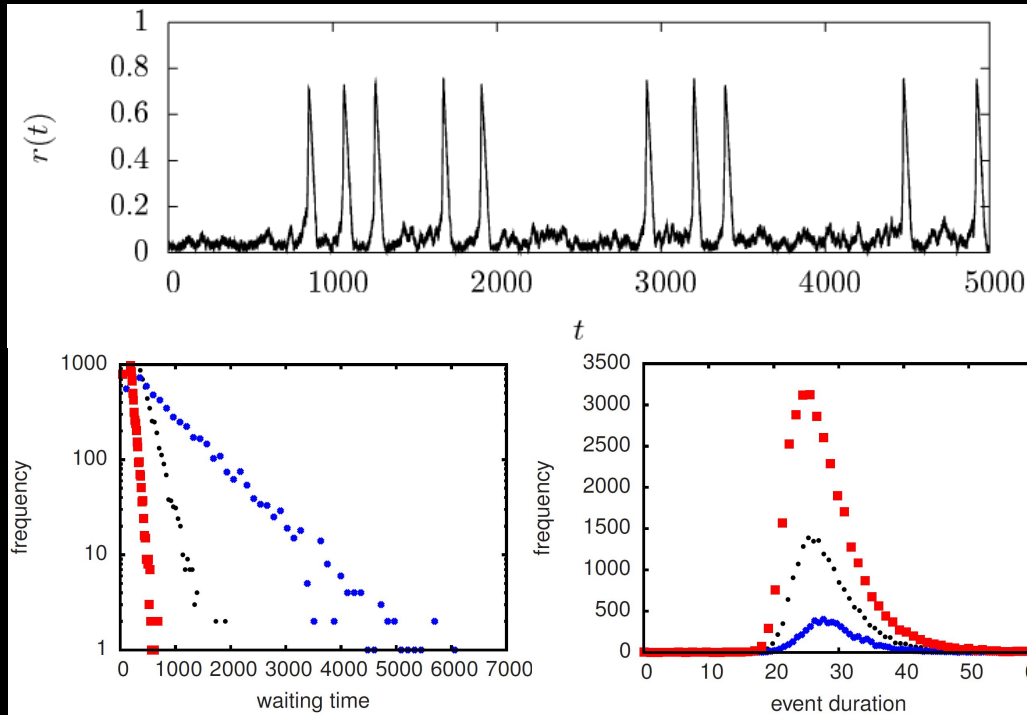
$\vartheta$  refractory period

$b$  coupling strength

Measuring synchrony with Kuramoto's order parameter:  $r(t) = 1/|N| \left| \sum_{n \in N} e^{2\pi i \phi_n(t)} \right|$

# Self-Initiation and -Termination of Sz-like Events

$N = 500 \times 500$ ,  $m = 50$ ,  $\tau = 0.01$ ,  $b = 0.01$ , various  $\nu$



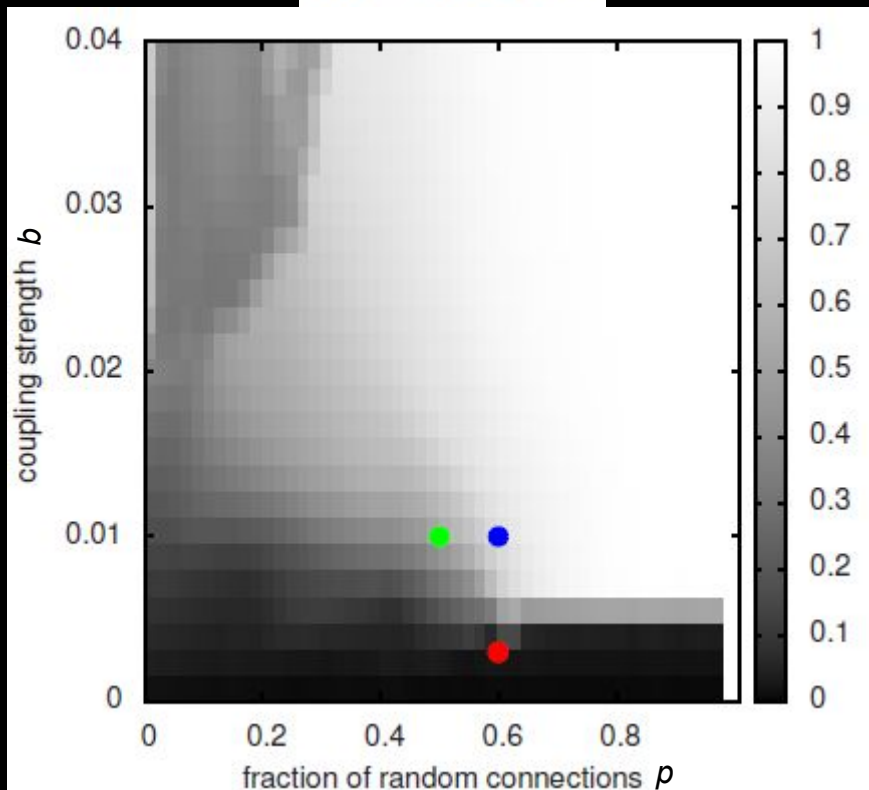
$N = 500 \times 500$ ,  $m = 50$ ,  $\tau = 0.01$ ,  $b = 0.01$ ,  $\nu = 0.05$



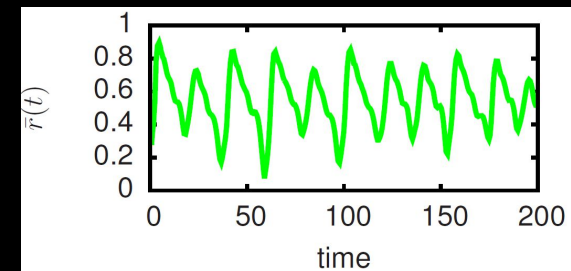
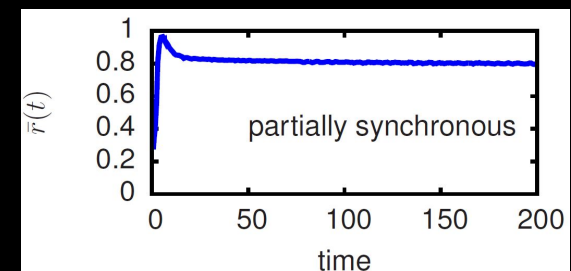
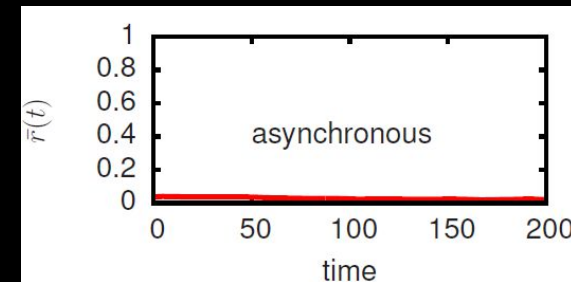
# Self-Initiation and -Termination of Sz-like Events

$$r(t) = 1/N \left| \sum_n e^{2\pi i \phi_n(t)} \right|, \quad \bar{r}(t) \text{ local maxima of } r(t)$$

mean of  $\bar{r}$



$N = 500 \times 500, m = 50, \tau = 0.01, \vartheta = 0.05;$

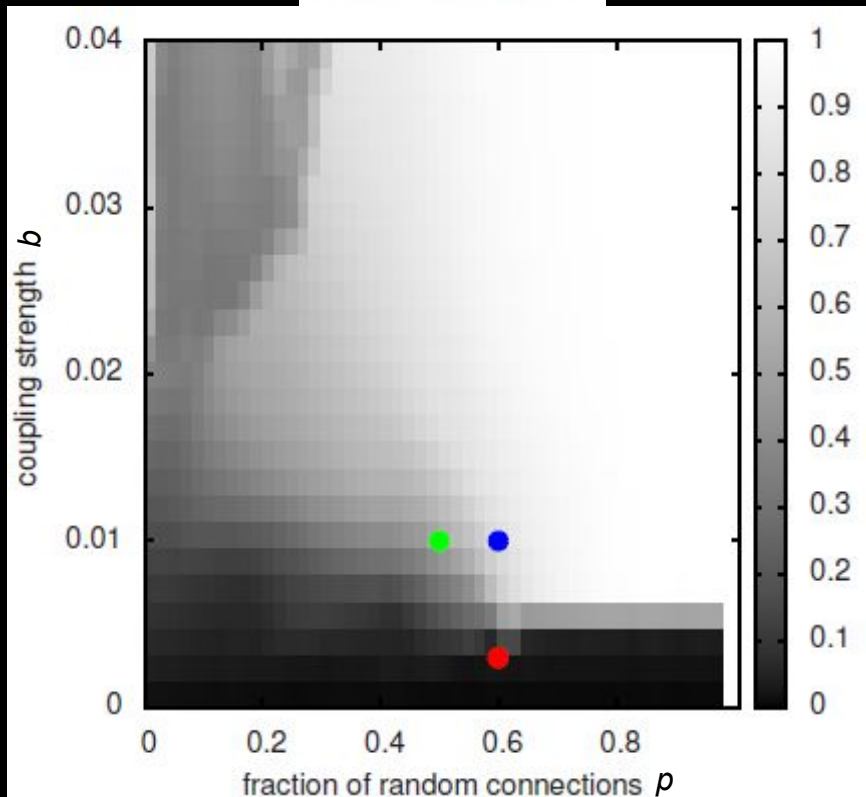




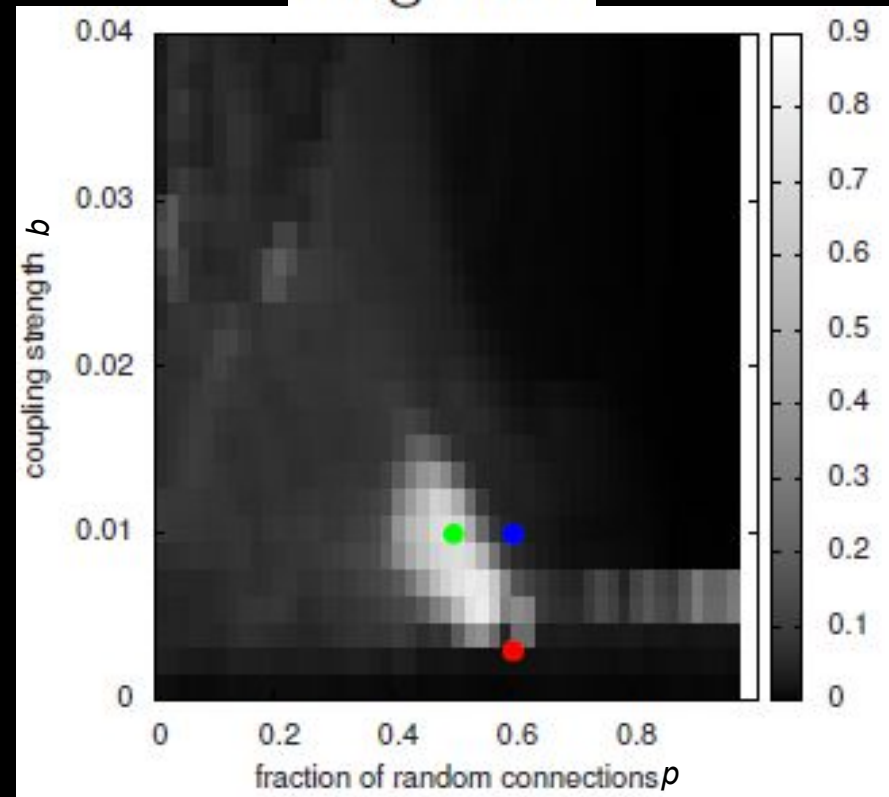
# Self-Initiation and -Termination of Sz-like Events

$$r(t) = 1/N \left| \sum_n e^{2\pi i \phi_n(t)} \right|, \quad \bar{r}(t) \text{ local maxima of } r(t)$$

mean of  $\bar{r}$



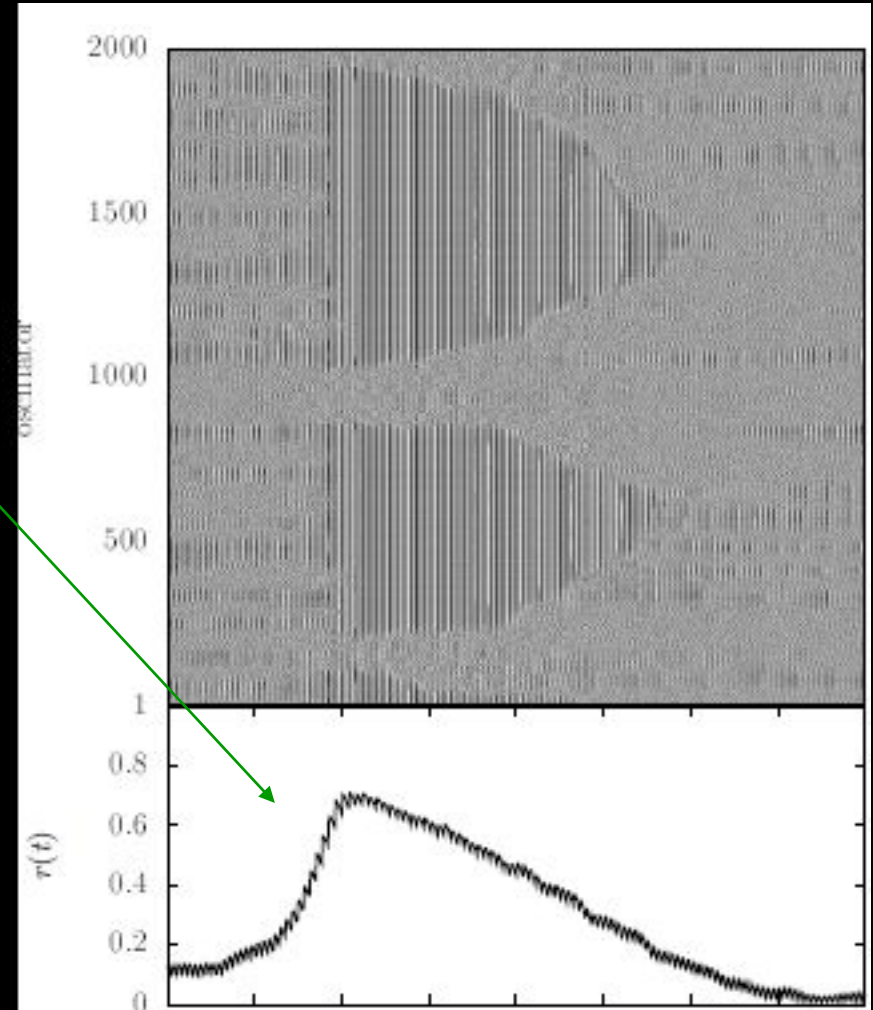
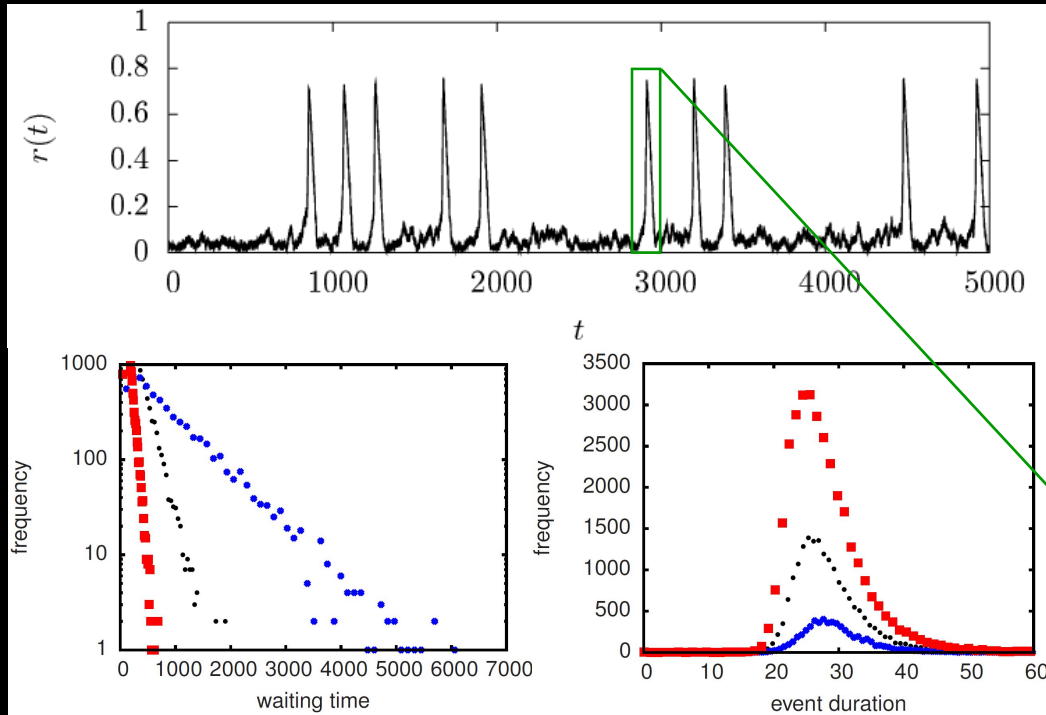
range of  $\bar{r}$



$N = 500 \times 500, m = 50, \tau = 0.01, \vartheta = 0.05;$

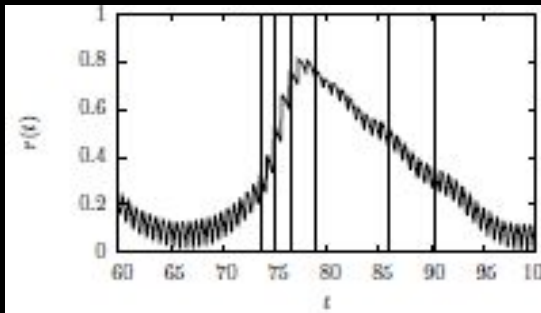
# Self-Initiation and -Termination of Sz-like Events

$N = 500 \times 500$ ,  $p = 0.5$ ,  $m = 50$ ,  $\tau = 0.01$ ,  $b = 0.01$ , various  $\nu$

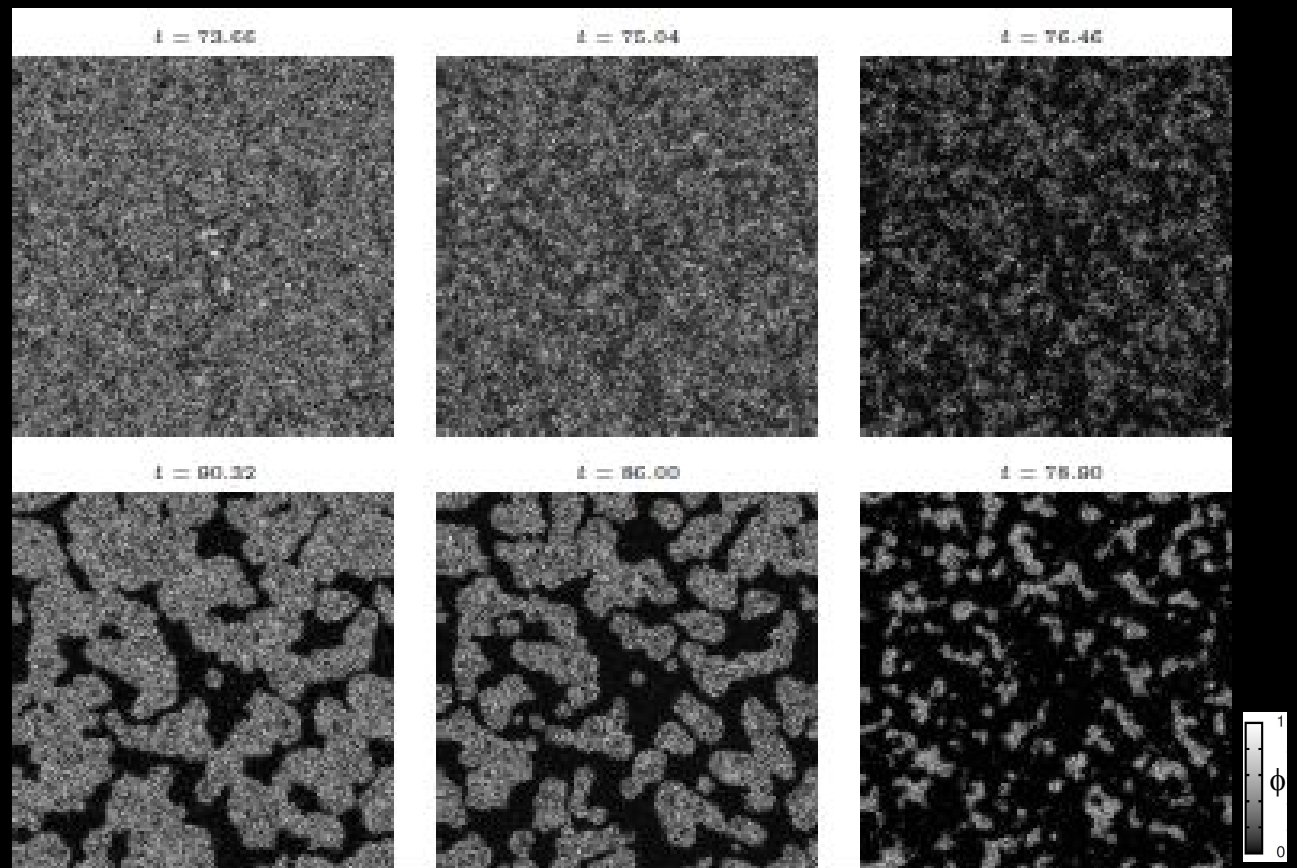


- small-amplitude oscillations with average phase velocity of oscillators
- non-converging macroscopic behavior, network-generated rhythms

# Self-Initiation and -Termination of Sz-like Events

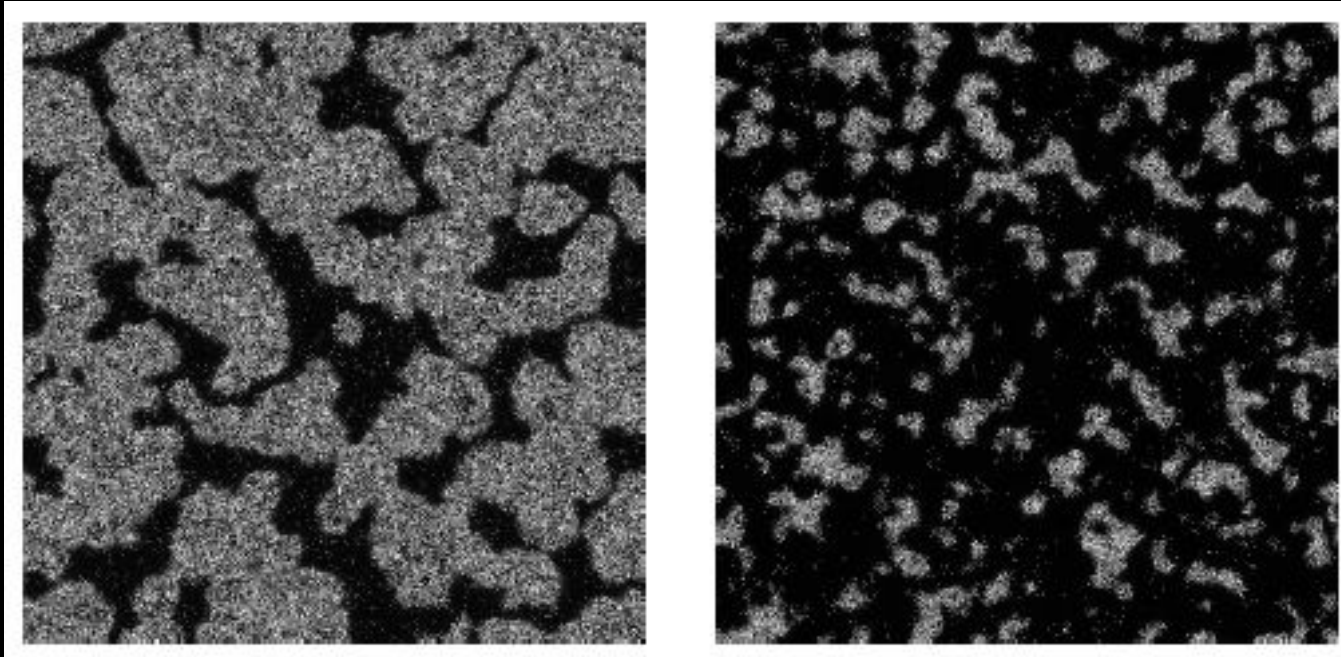


$N = 500 \times 500$ ,  $m = 50$ ,  $\tau = 0.01$ ,  $b = 0.01$ ,  $\nu = 0.05$



- comparable values of  $r(t)$  during ascending and descending part of event
- distributed asynchronous regions during ascending part
- connected asynchronous regions during descending part

# Self-Initiation and -Termination of Sz-like Events



mechanisms:

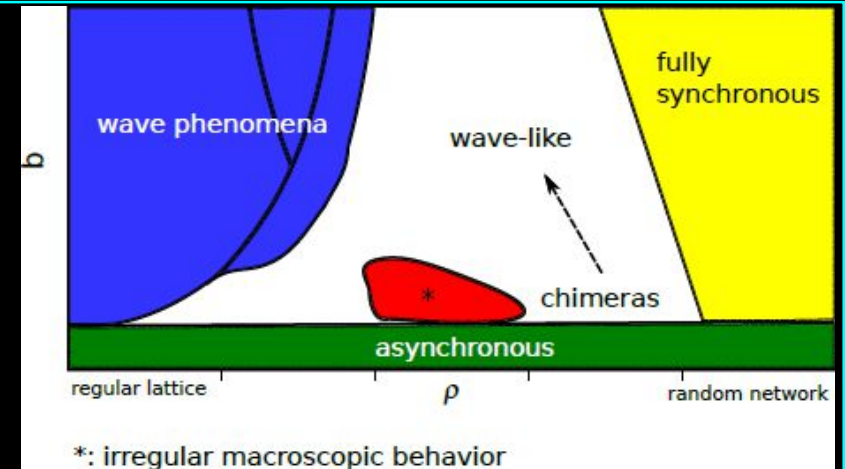
- stability of asynchronous regions
- stability of synchronous regions
- growing of asynchronous regions
- shrinking of asynchronous regions

long-range connections

short-range connections

# Self-Initiation and -Termination of Sz-like Events

- *no inhibition*
- *no pacemaker*
- *rhythm is network phenomenon*



- irregular macroscopic dynamics and sz-like events due to self-organized generation of chimera states
- cumulative size of asynchronous regions determined by control parameters
- event initiation via long-range connections
- even termination via short-range connections
- importance of complex coupling topology

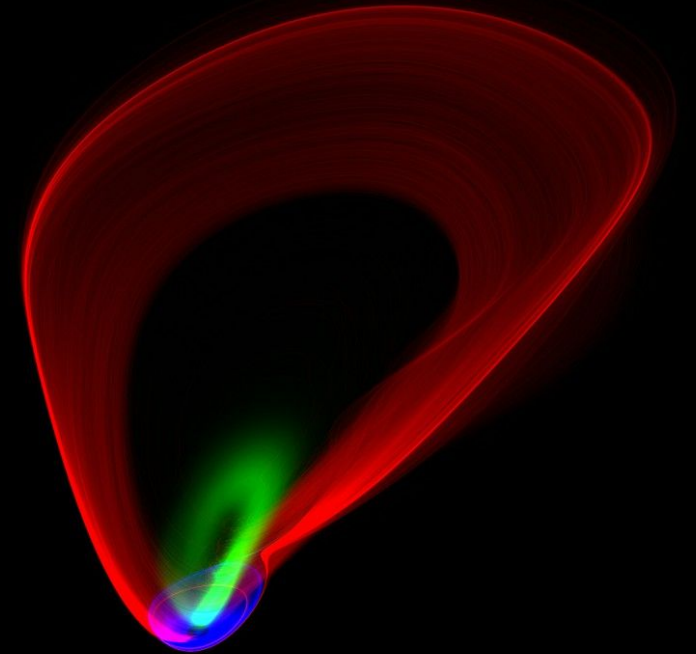


# Self-Initiation and -Termination of Sz-like Events

## *FitzHugh-Nagumo oscillators*

$$\begin{aligned}\dot{x}_i &= x_i(a - x_i)(x_i - 1) - y_i + k \sum_{j=1}^n A_{ij}(x_j - x_i), \\ \dot{y}_i &= b_i x_i - c y_i.\end{aligned}\quad (1)$$

- small-world network based on  $n = 100 \times 100$  lattice
- weak coupling ( $k \sim 10^{-3}$ )
- cyclic boundary conditions
- 60 nearest neighbors
- rewiring probability of  $p = 0.2$
- $a, b_j, c$  fixed
- observable: spatial mean of  $x$



- “critical mass”
- channel-like structures
- mixed-mode oscillations



# Conclusions

- epilepsy: disorder of large-scale neuronal networks  
(structure & function)
- paradigm shift: epileptic focus → epileptic network
- seizure self-termination through synchronization  
→ new therapeutic options?
- characterization of individual epileptic network  
→ individualized treatment?

